

Objective ① 16/30 —

Range Min $30 - 16 = 14$

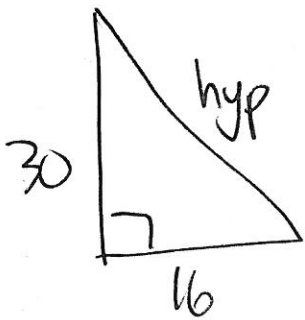
Range Max $30 + 16 = 46$

Range 14 to 46

third side $\in (14, 46)$

$$14 < \text{third side} < 46$$

Objective ② 16/30/hyp



$$\begin{aligned} \text{hyp} &= \sqrt{30^2 + 16^2} \\ &= \sqrt{900 + 256} \end{aligned}$$

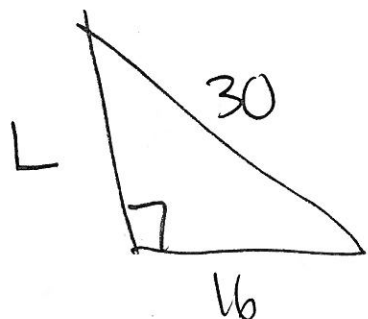
$$= \sqrt{1156} \quad \text{exact}$$

$$\text{hyp}^2 = 1156 = 34^2 = 2^2 \cdot 17^2$$

$$\text{hyp} = \sqrt{1156} = \textcircled{34}$$

$$= \sqrt{2^2 \cdot 17^2} = 2 \cdot 17 = \textcircled{34}$$

Objective ③ leg / 16 / 30



$$\begin{aligned} L &= \sqrt{30^2 - 16^2} \\ &= \sqrt{900 - 256} \quad \leftarrow \text{exact} \\ &= \sqrt{644} \end{aligned}$$

$$\begin{aligned} L &= \sqrt{644} = \sqrt{4} \sqrt{161} = 2\sqrt{161} \\ &= \sqrt{2^2 \cdot 7 \cdot 23} = \sqrt{2^2} \sqrt{7 \cdot 23} = 2\sqrt{161} \\ L &\approx 25.3772 \quad \leftarrow \text{approx} \end{aligned}$$

← simpler

Range Revisited

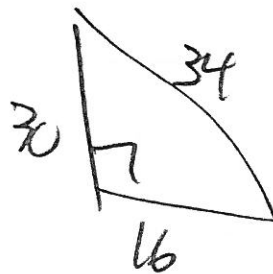
14	$\sqrt{644}$	$\sqrt{1156}$	46
14	$2\sqrt{161}$	34	46
14	25.3772	34	46
↑ not a triangle	↑ right triangle	↑ right triangle	↑ not a triangle

Objective 4

16/30/31

34 \in (14, 46)

hyp = 34 when



Since $31^2 < 34^2$

$31 < 34$

largest side $<$ hyp

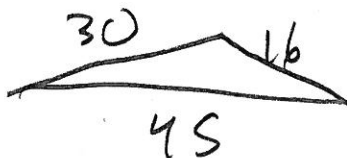
acute scalene

16/30/46

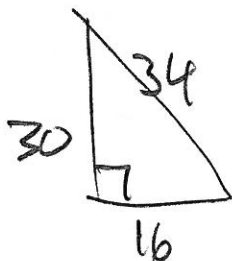
46 \notin (14, 46)

Not a triangle $16 + 30 = 46$

16/30/45



hyp = 34 when



Since $45^2 > 34^2$

$45 > 34$

largest side $>$ hyp

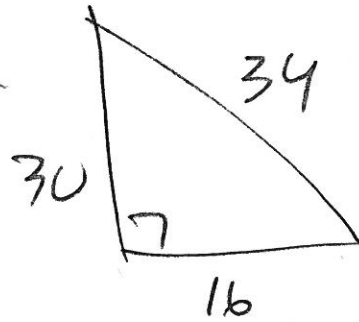
obtuse scalene

Objective 4

$37 \in (14, 46)$
it is a triangle

16/30/37

Since hyp = 34 when



$$37^2 > 34^2$$

so third side > hyp

$$37 > 34$$

obtuse scalene

20/21 / —

Objective ①

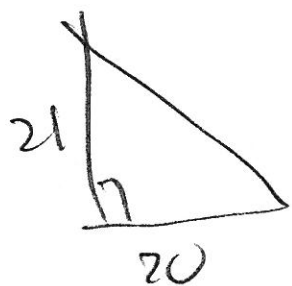
Range min $21 - 20 = 1$
max $21 + 20 = 41$

1 to 41 Range

third side $\in (1, 41)$

$$1 < \text{third side} < 41$$

Objective ② leg / leg / — \rightarrow 20/21/hyp



$$\text{hyp} = \sqrt{21^2 + 20^2} = \sqrt{441 + 400} = \sqrt{841}$$

$= 29$

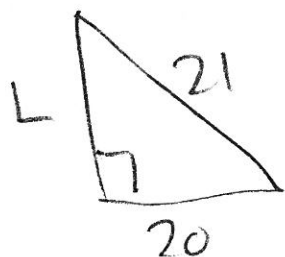
exact

$$841 = 29^2$$

$\text{hyp} = 29$

 simplified

Objective ③ — / leg / hyp \rightarrow leg / 20 / 21



$$L = \sqrt{21^2 - 20^2} = \sqrt{441 - 400} = \sqrt{41}$$

exact

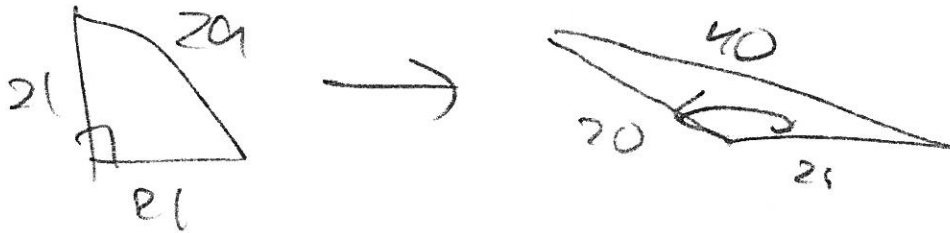
$$L \approx 6.4031$$

approximate

Objective (4)

Since hyp = 29

Range 14 to 41



third side > hyp
obtuse scalene

Objective 4

Recall Range 1 to 41

$$1 \quad \sqrt{41} \quad \sqrt{841} \quad 41$$

$$1 \quad \sqrt{41} \quad 29 \quad 41$$

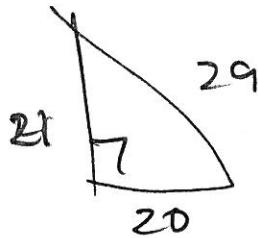
1
not a triangle

6.4031
right

29
right

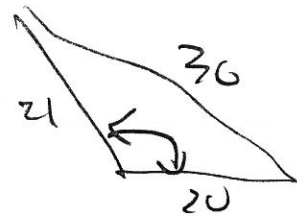
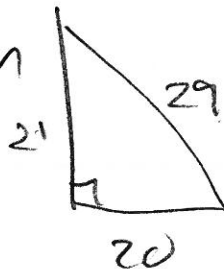
41
not a triangle

hyp = 29 when



20/21/29
Pythagorean
triple
(right scalene)

Since hyp = 29 when



third side > hyp
obtuse scalene

11/61 (this was toughest version)

Objective 1

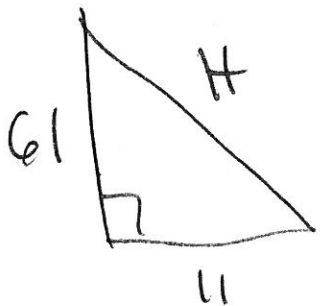
Range $\min = 61 - 11 = 50$
 $\max = 61 + 11 = 72$

50 to 72

third side $\in (50, 72)$

$$50 < \text{third side} < 72$$

Objective 2 Leg | Leg | — \rightarrow 11/61/—

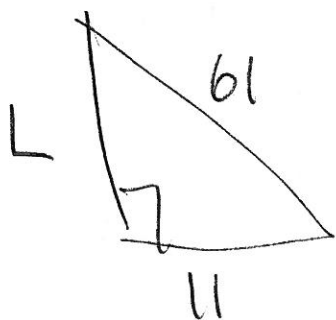


$$H = \sqrt{61^2 + 11^2} = \sqrt{3721 + 121}$$

$$H = \sqrt{3842} \approx 61.9839$$

$$H^2 = 3842 = 2 \cdot 17 \cdot 113$$

Objective 3 — | leg | hyp \rightarrow — | 11/61



$$L = \sqrt{61^2 - 11^2} = \sqrt{3721 - 121}$$

$$L = \sqrt{3600} = 60$$

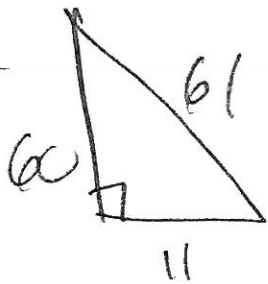
$$3600 = 100 \cdot 36 = 2^2 \cdot 5^2 \cdot 2^2 \cdot 3^2$$

$\rightarrow 4 \cdot 2 \cdot 2 \cdot 3 \cdot 3 = 6$

Objective (4) Tricky

11/60/61

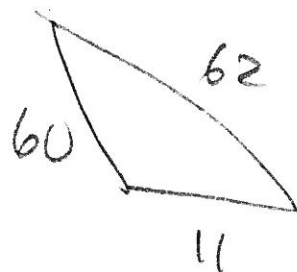
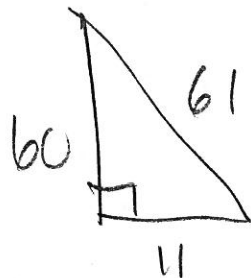
Since



$$\rightarrow \text{hyp} = 61$$

right scalene

11/60/62



Since $\text{hyp} < \text{third side}$ & $62 \in (50, 72)$
 $61 < 62$

we know 11/60/62 is obtuse scalene

$$11/60/58 \rightarrow 11/58/60$$

$$\begin{aligned} \text{hyp} &= \sqrt{58^2 + 11^2} \\ &= \sqrt{3485} \\ &\approx 59.0339 \end{aligned}$$

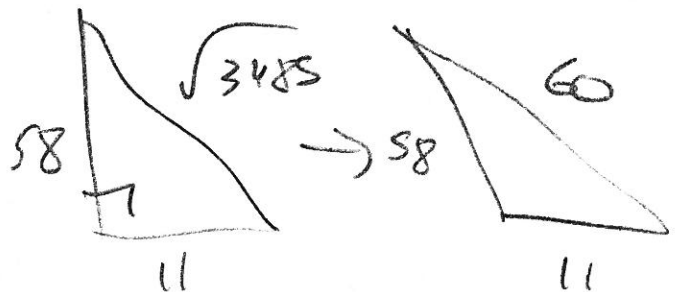
Since third side = 60

$$\text{hyp} \approx 59.0339$$

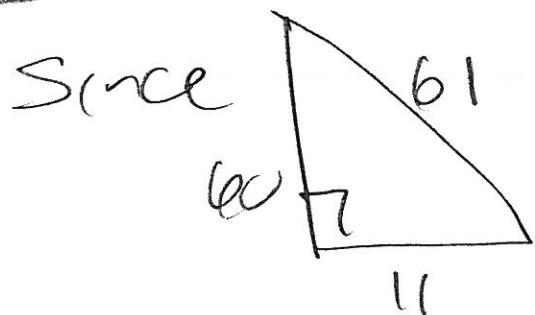
$\text{hyp} < \text{third side}$

$$59.0339 < 60$$

obtuse scalene



Objective 4

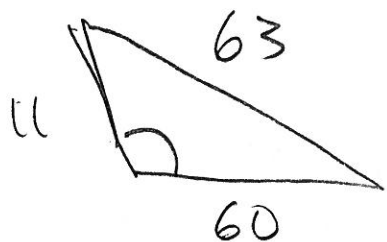


11/60/63

hyp < third side
 $61 < 61$

& $63 \in (50, 72)$

↓
obtuse scalene



21/28 version

Objective ①

Range $\min = 28 - 21 = 7$

$\max = 21 + 28 = 49$

Range 7 to 49

third side $\in (7, 49)$

$7 < \text{third side} < 49$

Objective ② leg / leg / hyp $\rightarrow 21/28/\text{hyp}$

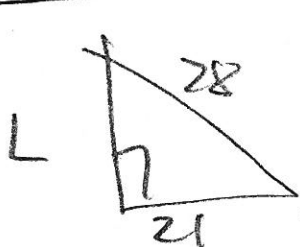


$\text{hyp} = \sqrt{21^2 + 28^2} = \sqrt{441 + 784}$

$\text{hyp} = \sqrt{1225} = 35$
exact simplified

Note $1225 = 5^2 \cdot 7^2$ $\sqrt{1225} = 5 \cdot 7 = 35$

Objective ③ - leg / hyp $\rightarrow \text{leg} / 21 / 28$



$L = \sqrt{28^2 - 21^2} = \sqrt{784 - 441} = \sqrt{343}$

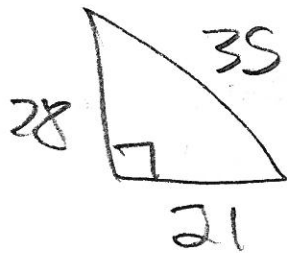
$L = \sqrt{49 \cdot 7} = \sqrt{49} \sqrt{7} = 7\sqrt{7}$

$L = \sqrt{343} = 7\sqrt{7} \approx 18.5203$

Objective ④ 21/28/47

Range 7 to 50 47 \in (7, 49)

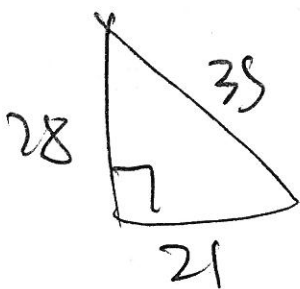
Recall



hyp < third side
 $35 < 47$
obtuse scalene

Range 21/28/50 cannot be ≥ 49
7 to 49 ← cannot be 50
cannot be ≤ 7
so 21/28/50 Not a triangle

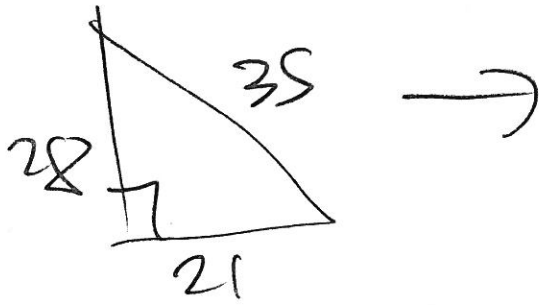
21/28/35



this is right scalene triangle

Objective (4)

21 / 28 / 32



hyp > third side

$35 > 32$

acute scalene

Name _____

2 nd hour	3 rd hour	4 th hour
5 th hour	6 th hour	7 th hour

Table 1	Table 3	Table 5	Table 7
Table 2	Table 4	Table 6	Table 8

Standard Form Line Objective 1 I understand which form of the line is called the standard form of the line I can explain it to others Not Yet	
Standard Form Line Objective 2 I understand what A, B, and C are when given the standard form of the line I can explain it to others Not Yet	
Standard Form Line Objective 3 I understand the difference between lines that have $AB > 0$ and lines that have $AB < 0$ I can explain it to others Not Yet	

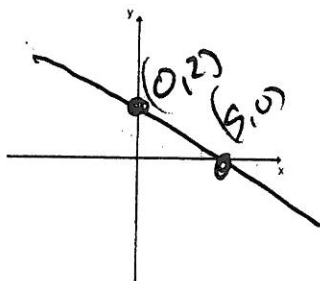
Line Objective 1 I can plot intercepts correctly (when given Standard Form Lines) I can explain it to others Not Yet	
Line Objective 2 I find intercepts correctly (when given Standard Form Lines) I can explain it to others Not Yet	
Line Objective 3 I find the slope correctly (when given Standard Form Lines) I can explain it to others Not Yet	
Line Objective 4 I can isolate y correctly (when given Standard Form Lines) I can explain it to others Not Yet	

Technology Objective 1 I can plot a standard form line on a graphing calculator I can explain it to others Not Yet	
Technology Objective 2 I can plot a slope intercept form line on a graphing calculator I can explain it to others Not Yet	
Technology Objective 3 I can plot a standard form line on the Desmos Graphing Application I can explain it to others Not Yet	
Technology Objective 4 I can plot a slope intercept form line on the Desmos Graphing Application I can explain it to others Not Yet	

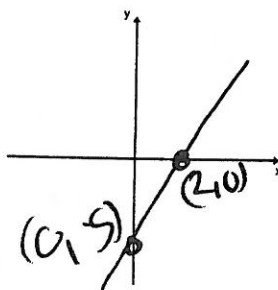
Method 1: Intercept Method <ul style="list-style-type: none"> X Intercept is $(\frac{C}{A}, 0)$ Y Intercept is $(0, \frac{C}{B})$ Slope $m = \frac{-A}{B}$ 	Method 2: Divide by B method <ul style="list-style-type: none"> Divide all terms by B first Apply the opposite of x term to both sides 	Method 3: Solve for y method <ul style="list-style-type: none"> Move x term (this will CHANGE sign) Isolate y (this means you will divide ALL terms by B) 	Method 4: Graphing Technology <ul style="list-style-type: none"> Plot line with technology Find intercepts Find slope from graph
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Directions: 1) Sketch a graph of the standard form line. 2) complete the related table. 3) confirm 1 & 2 with technology.

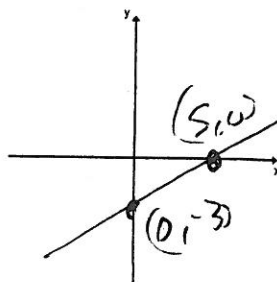
Organizer Example 1
 $2x + 5y = 10$



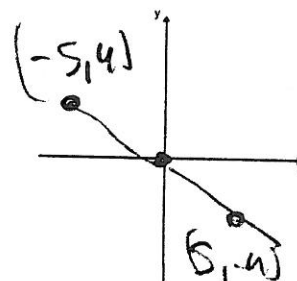
Organizer Example 2
 $5x - 2y = 10$



Organizer Example 3
 $-3x + 5y = -15$



Organizer Example 4
 $-4x - 5y = 0$



A	B	C	AB
2	5	10	10

Slope of the line
 $m = -\frac{2}{5}$

X intercept as a point	Y intercept as a point
(5, 0)	(0, 2)

$Y = mx + b$ form of line

$$y = -\frac{2}{5}x + 2$$

A	B	C	AB
5	-2	10	-10

Slope of the line
 $m = \frac{5}{2}$

X intercept as a point	Y intercept as a point
(2, 0)	(0, -5)

$Y = mx + b$ form of line

$$y = \frac{5}{2}x - 5$$

A	B	C	AB
-3	5	-15	-15

Slope of the line
 $m = \frac{3}{5}$

X intercept as a point	Y intercept as a point
(5, 0)	(0, -3)

$Y = mx + b$ form of line

$$y = \frac{3}{5}x - 3$$

A	B	C	AB
-4	-5	0	20

Slope of the line
 $m = -\frac{4}{5}$

X intercept as a point	Y intercept as a point
(0, 0)	(0, 0)

$Y = mx + b$ form of line

$$y = -\frac{4}{5}x$$

Complete these statements

- When AB is positive the slope is negative
- When AB is negative the slope is positive

Name _____

2nd hour	3rd hour	4th hour
5th hour	6th hour	7th hour

Table 1	Table 3	Table 5	Table 7
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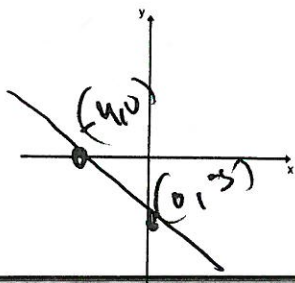
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Technology Objective 1 I can plot a standard form line on a graphing calculator I can explain it to others		Not Yet
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Technology Objective 3 I can plot a standard form line on the Desmos Graphing Application I can explain it to others		Not Yet
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Method 1: Intercept Method <ul style="list-style-type: none"> X intercept is $(\frac{C}{A}, 0)$ Y intercept is $(0, \frac{C}{B})$ Slope $m = \frac{-A}{B}$ 	Method 2: Divide by B method <ul style="list-style-type: none"> Divide all terms by B first Apply the opposite of x term to both sides 	Method 3: Solve for y method <ul style="list-style-type: none"> Move x term (this will CHANGE sign) Isolate y (this means you will divide ALL terms by B) 	Method 4: Graphing Technology <ul style="list-style-type: none"> Plot line with technology Find intercepts Find slope from graph
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Directions: 1) Sketch a graph of the standard form line. 2) complete the related table. 3) confirm 1 & 2 with technology.

Understander Example 1
 $5x + 4y = -20$



A	B	C	AB
5	4	-20	20

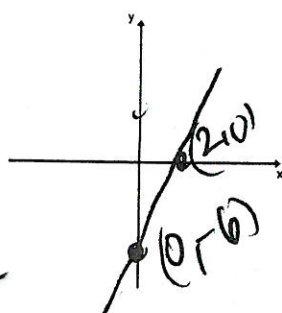
Slope of the line
 $m = -\frac{5}{4}$

X intercept as a point	Y intercept as a point
$(-4, 0)$	$(0, -5)$

Y = mx+b form of line

$$y = -\frac{5}{4}x - 5$$

Understander Example 2
 $6x - 2y = 12$



A	B	C	AB
6	-2	12	-12

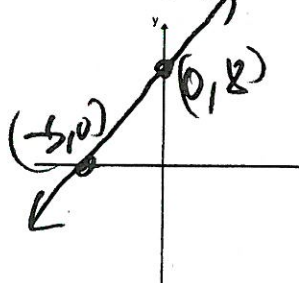
Slope of the line
 $m = \frac{6}{2} = 3$

X intercept as a point	Y intercept as a point
$(2, 0)$	$(0, -6)$

Y = mx+b form of line

$$y = 3x - 6$$

Understander Example 3
 $-8x + 5y = 40$



A	B	C	AB
-8	5	40	-40

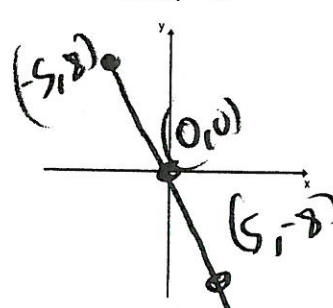
Slope of the line
 $m = \frac{8}{5}$

X intercept as a point	Y intercept as a point
$(-5, 0)$	$(0, 8)$

Y = mx+b form of line

$$y = \frac{8}{5}x + 8$$

Understander Example 4
 $-8x - 5y = 0$



A	B	C	AB
-8	-5	0	40

Slope of the line
 $m = -\frac{8}{5}$

X intercept as a point	Y intercept as a point
$(0, 0)$	$(0, 0)$

Y = mx+b form of line

$$y = -\frac{8}{5}x$$

Complete these statements

- When AB is positive the slope is negative
- When AB is negative the slope is positive

Name _____

2nd hour	3rd hour	4th hour
5th hour	6th hour	7th hour

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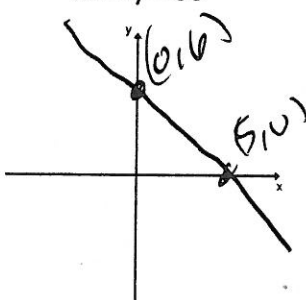
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Directions: 1) Sketch a graph of the standard form line. 2) complete the related table. 3) confirm 1 & 2 with technology.

Resourcer Example 1
 $6x + 5y = 30$



A	B	C	AB
6	5	30	30

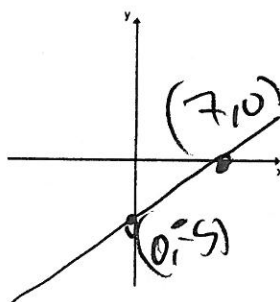
Slope of the line
 $m = -\frac{6}{5}$

X intercept as a point	Y intercept as a point
(5, 0)	(0, 6)

Y = mx+b form of line

$$y = -\frac{6}{5}x + 6$$

Resourcer Example 2
 $5x - 7y = 35$



A	B	C	AB
5	-7	35	-35

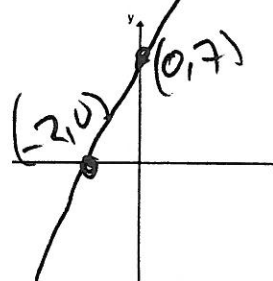
Slope of the line
 $m = \frac{5}{7}$

X intercept as a point	Y intercept as a point
(7, 0)	(0, -5)

Y = mx+b form of line

$$y = \frac{5}{7}x - 5$$

Resourcer Example 3
 $-7x + 2y = 14$



A	B	C	AB
-7	2	14	-14

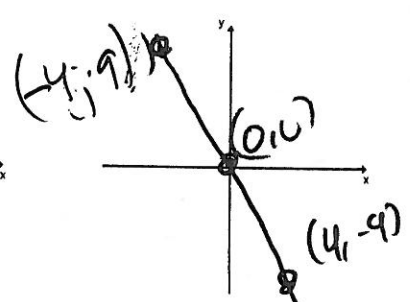
Slope of the line
 $m = \frac{7}{2}$

X intercept as a point	Y intercept as a point
(-2, 0)	(0, 7)

Y = mx+b form of line

$$y = \frac{7}{2}x + 7$$

Resourcer Example 4
 $-9x - 4y = 0$



A	B	C	AB
-9	-4	0	36

Slope of the line
 $m = -\frac{9}{4}$

X intercept as a point	Y intercept as a point
(0, 0)	(0, 0)

Y = mx+b form of line

$$y = -\frac{9}{4}x$$

Complete these statements

- When AB is positive the slope is negative
- When AB is negative the slope is positive

Name _____

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Standard Form Line Objective 1 I understand which form of the line is called the standard form of the line I can explain it to others		Not Yet
Standard Form Line Objective 2 I understand what A, B, and C are when given the standard form of the line I can explain it to others		Not Yet
Standard Form Line Objective 3 I understand the difference between lines that have $AB > 0$ and lines that have $AB < 0$ I can explain it to others		Not Yet

Line Objective 1 I can plot intercepts correctly (when given Standard Form Lines) I can explain it to others		Not Yet
Line Objective 2 I find intercepts correctly (when given Standard Form Lines) I can explain it to others		Not Yet
Line Objective 3 I find the slope correctly (when given Standard Form Lines) I can explain it to others		Not Yet
Line Objective 4 I can isolate y correctly (when given Standard Form Lines) I can explain it to others		Not Yet

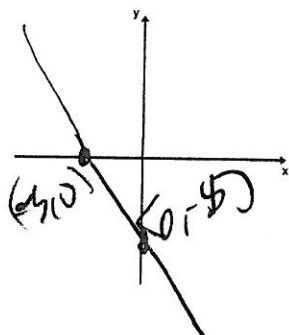
Technology Objective 1 I can plot a standard form line on a graphing calculator I can explain it to others		Not Yet
Technology Objective 2 I can plot a slope intercept form line on a graphing calculator I can explain it to others		Not Yet
Technology Objective 3 I can plot a standard form line on the Desmos Graphing Application I can explain it to others		Not Yet
Technology Objective 4 I can plot a slope intercept form line on the Desmos Graphing Application I can explain it to others		Not Yet

Method 1: Intercept Method <ul style="list-style-type: none"> X intercept is $(\frac{C}{A}, 0)$ Y intercept is $(0, \frac{C}{B})$ Slope $m = -\frac{A}{B}$ 	Method 2: Divide by B method <ul style="list-style-type: none"> Divide all terms by B first Apply the opposite of x term to both sides 	Method 3: Solve for y method <ul style="list-style-type: none"> Move x term (this will CHANGE sign) Isolate y (this means you will divide ALL terms by B) 	Method 4: Graphing Technology <ul style="list-style-type: none"> Plot line with technology Find intercepts Find slope from graph
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Directions: 1) Sketch a graph of the standard form line. 2) complete the related table. 3) confirm 1 & 2 with technology.

Includer Example 1

$$8x + 5y = -40$$



A	B	C	AB
8	5	-40	40

Slope of the line
 $m = -8/5$

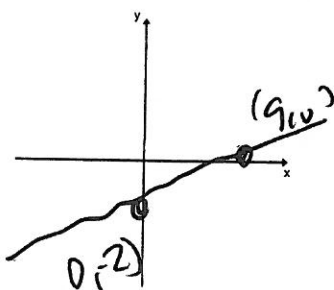
X intercept as a point	Y intercept as a point
$(-5, 0)$	$(0, -8)$

Y = mx+b form of line

$$y = -\frac{8}{5}x - 8$$

Includer Example 2

$$2x - 9y = 18$$



A	B	C	AB
2	-9	18	-18

Slope of the line
 $m = 2/9$

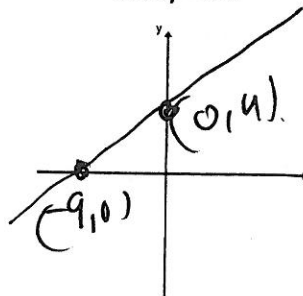
X intercept as a point	Y intercept as a point
$(9, 0)$	$(0, -2)$

Y = mx+b form of line

$$y = \frac{2}{9}x - 2$$

Includer Example 3

$$-4x + 9y = 36$$



A	B	C	AB
-4	9	36	-36

Slope of the line
 $m = 4/9$

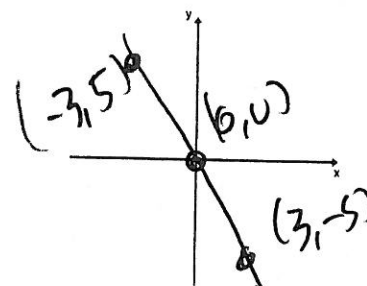
X intercept as a point	Y intercept as a point
$(-9, 0)$	$(0, 4)$

Y = mx+b form of line

$$y = \frac{4}{9}x + 4$$

Includer Example 4

$$-5x - 3y = 0$$



A	B	C	AB
-5	-3	0	15

Slope of the line
 $m = -5/3$

X intercept as a point	Y intercept as a point
$(0, 0)$	$(0, 0)$

Y = mx+b form of line

$$y = -\frac{5}{3}x$$

Complete these statements

- When AB is positive the slope is negative
- When AB is negative the slope is positive