

(6,0) to  $\sqrt{2x-4}$

Given Function:  $y = \sqrt{2 \cdot x - 4}$     Given Point (6,0)

Objective Function: (not expanded)  $D(x) = \sqrt{(x-6)^2 + (\sqrt{2 \cdot x - 4} - 0)^2}$

There are no roots of Objective Function

Objective Function: (expanded)  $D(x) = \sqrt{x^2 - 10 \cdot x + 32}$

Derivative of Objective Function  $D'(x) = \frac{x-5}{\sqrt{x^2 - 10 \cdot x + 32}}$

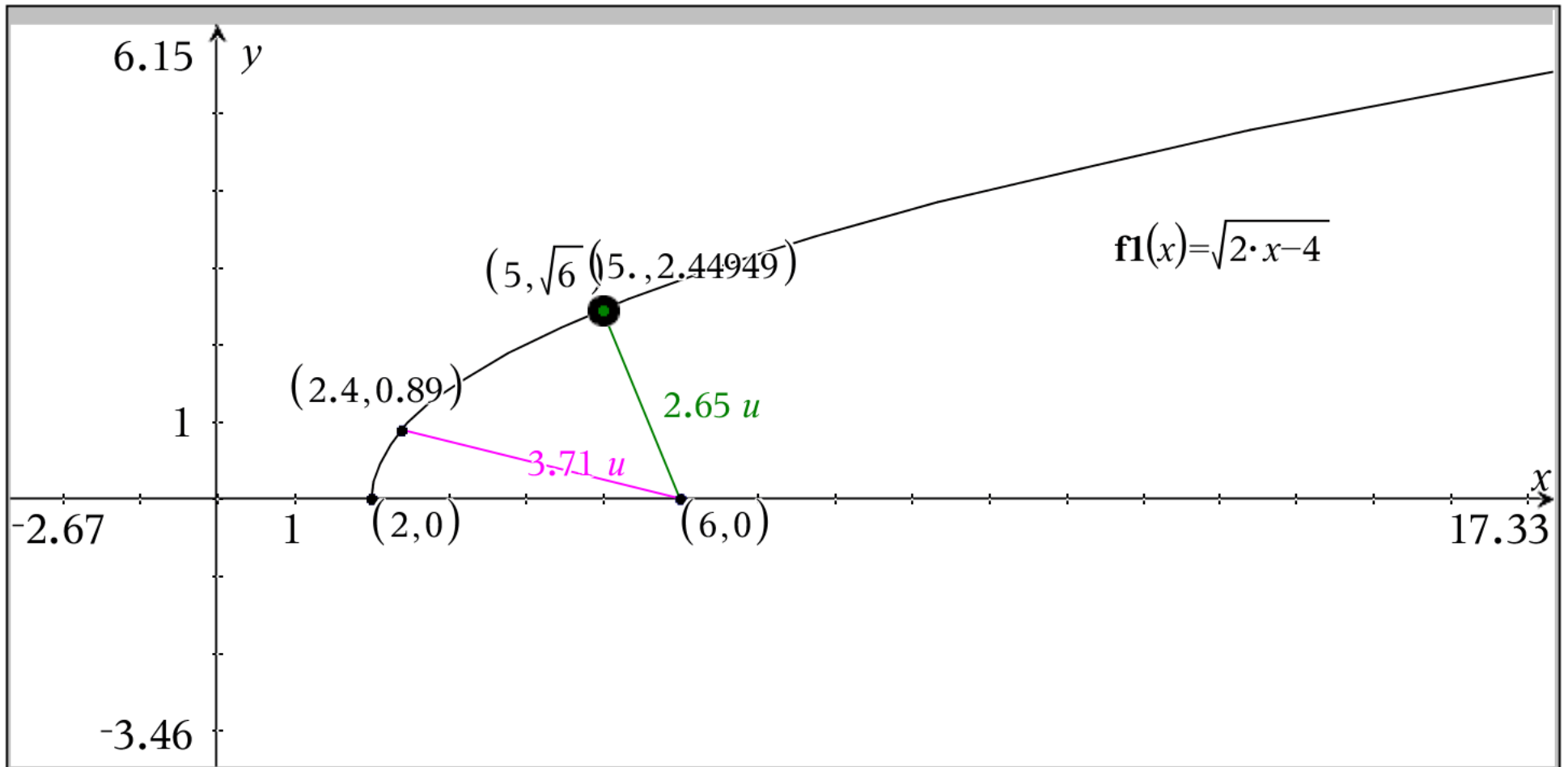
Roots of Derivative Function  $x = 5$

Closest Point on the Given function to the fixed point at (6,0)

is at  $x = 5$  and  $y = \sqrt{2 \cdot 5 - 4} = \sqrt{6} \approx 2.45$  or  $(5, \sqrt{6})$

The minimum distance from the fixed point (6,0) to the given function is

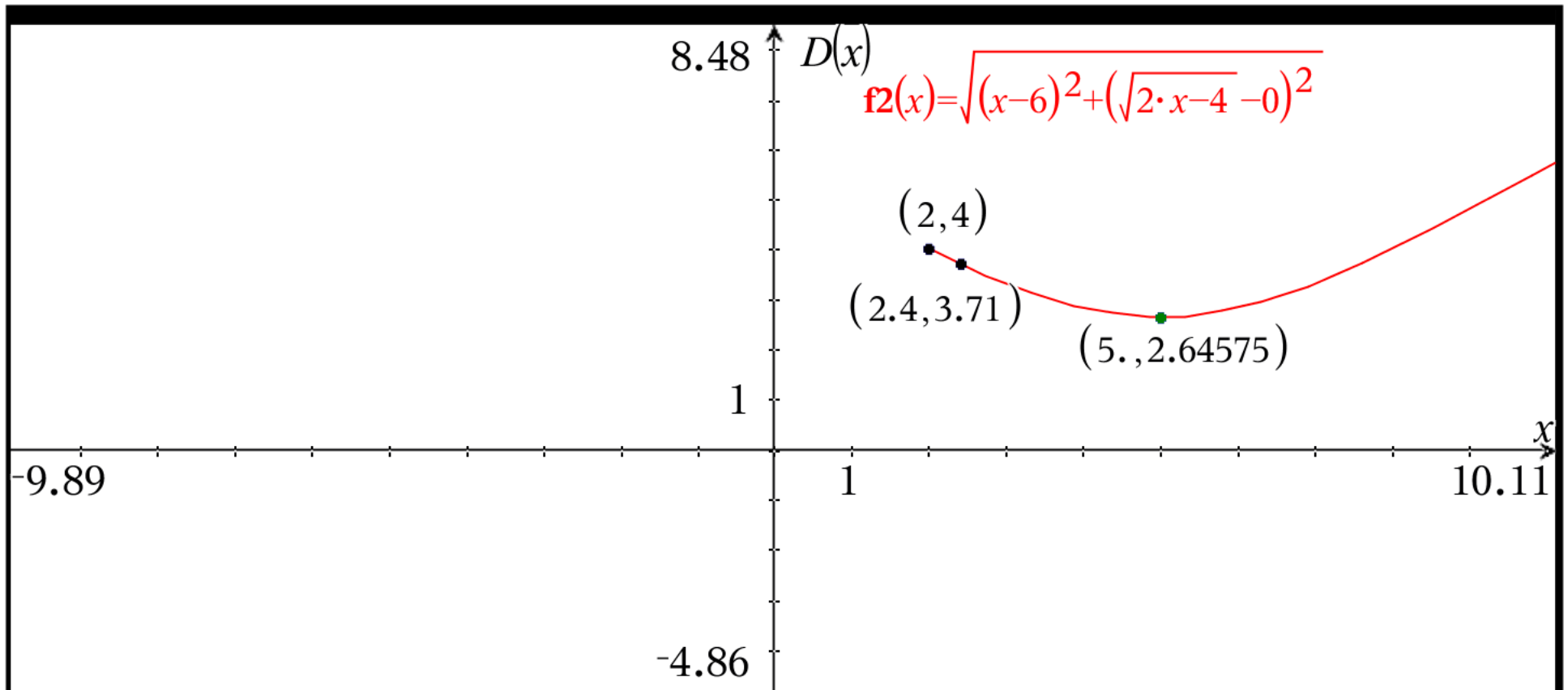
$D(5) = \sqrt{7} \approx 2.65$



any\_x = 2.4

The graph on the graph above is the given function

$$y = \sqrt{2 \cdot (x-2)}$$



$f_4(x) =$

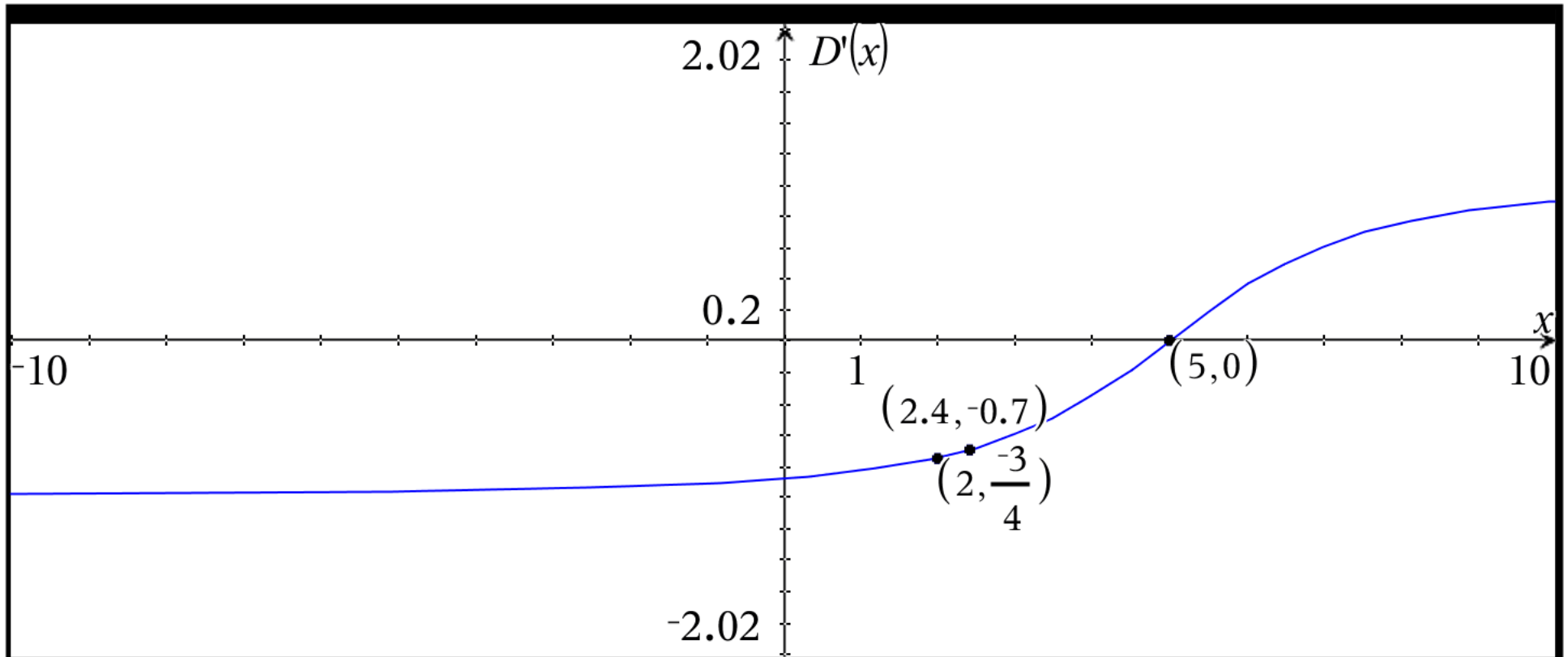


any\_x = 2.4

The graph above is the distance function the measures distance from fixed point  $(6,0)$  to the given function  $y = \sqrt{2 \cdot (x-2)}$

The graph of the above is the distance function

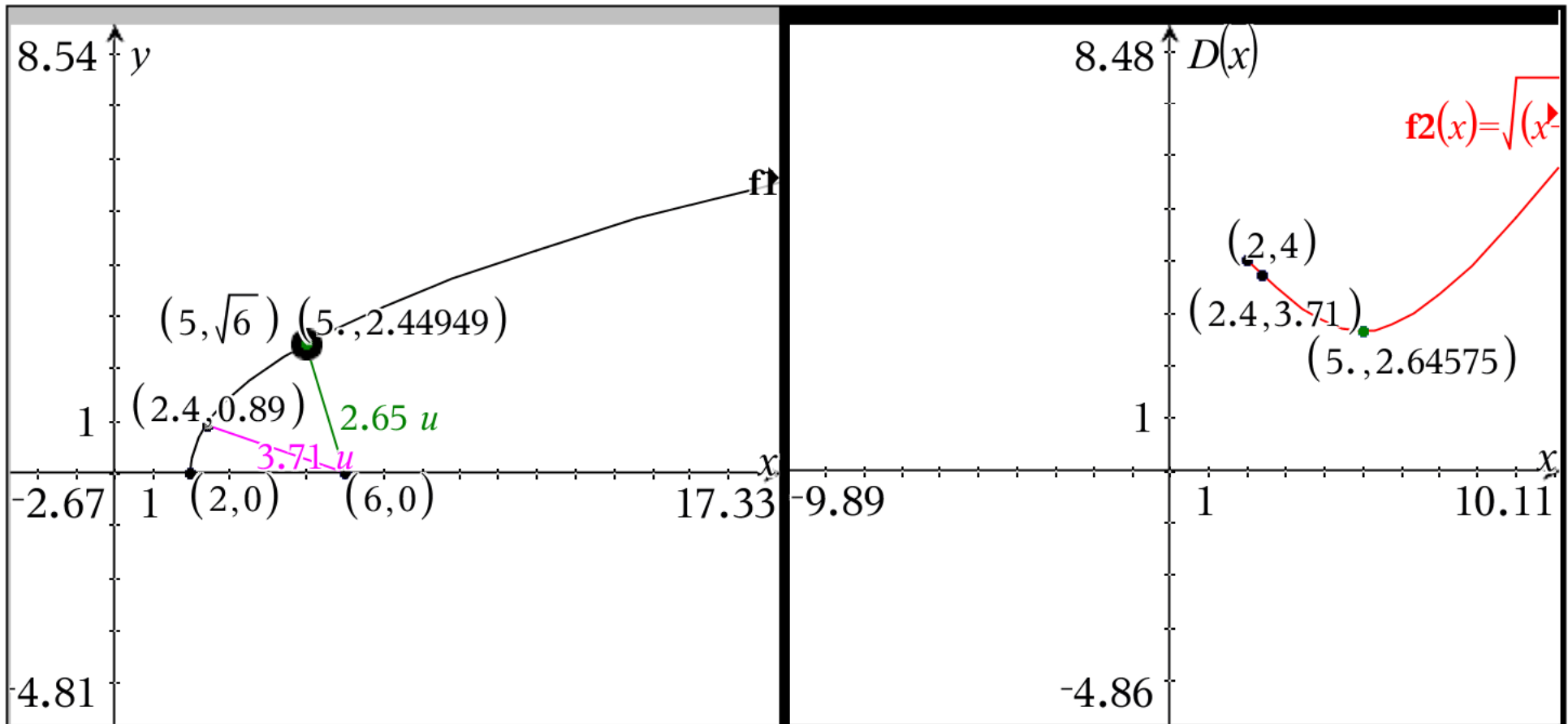
$$D(x) = \sqrt{x^2 - 10 \cdot x + 32}$$



< > any\_x = 2.4

The graph of the above is the derivative of the distance function

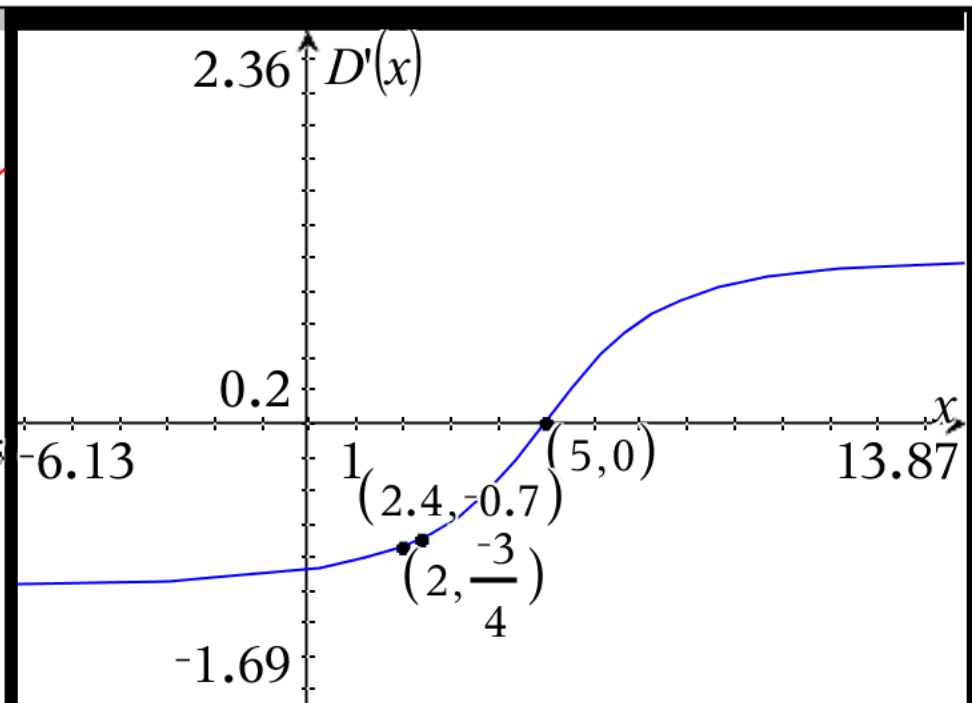
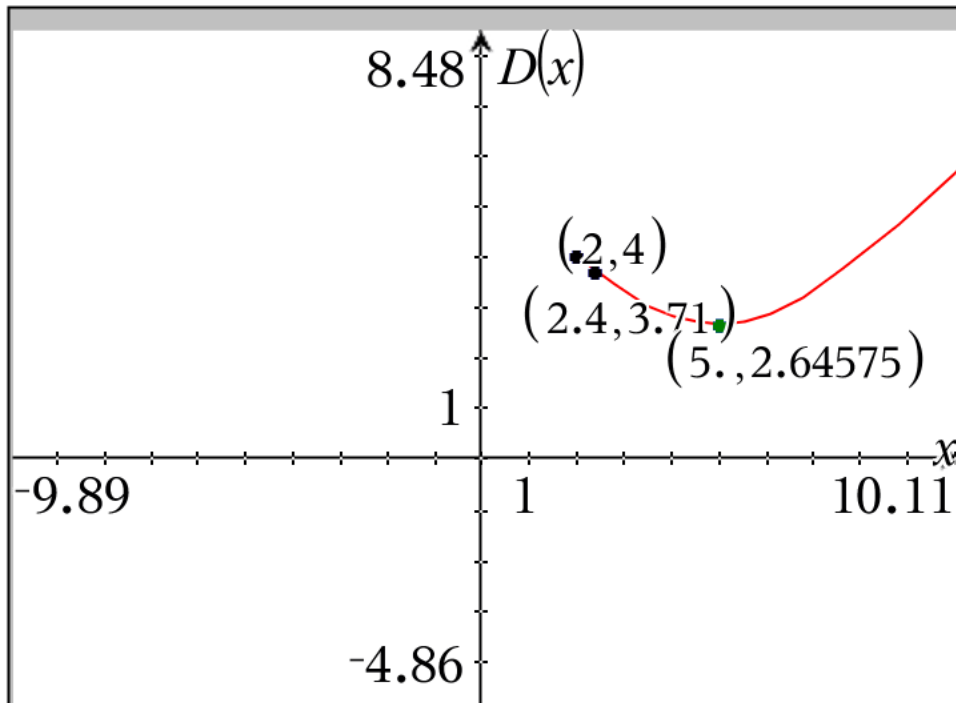
$$D'(x) = \frac{x-5}{\sqrt{x^2-10 \cdot x+32}}$$



< > any\_x = 2.4

The graph on the left is the given function  $y = f_1(x)$

The graph of the right is the distance function  $D(x) = f_2(x)$



any\_x = 2.4

The graph on the left is the distance function  $y = \sqrt{x^2 - 10 \cdot x + 32}$

The graph of the right is the derivative of the distance function

$$D'(x) = \frac{x-5}{\sqrt{x^2 - 10 \cdot x + 32}}$$