

(11,0) to  $\sqrt{8x-32}$

Given Function:  $y = \sqrt{8 \cdot x - 32}$     Given Point (11,0)

Objective Function: (not expanded)  $D(x) = \sqrt{(x-11)^2 + (\sqrt{8 \cdot x - 32} - 0)^2}$

There are no roots of Objective Function

Objective Function: (expanded)  $D(x) = \sqrt{x^2 - 14 \cdot x + 89}$

Derivative of Objective Function  $D'(x) = \frac{x-7}{\sqrt{x^2 - 14 \cdot x + 89}}$

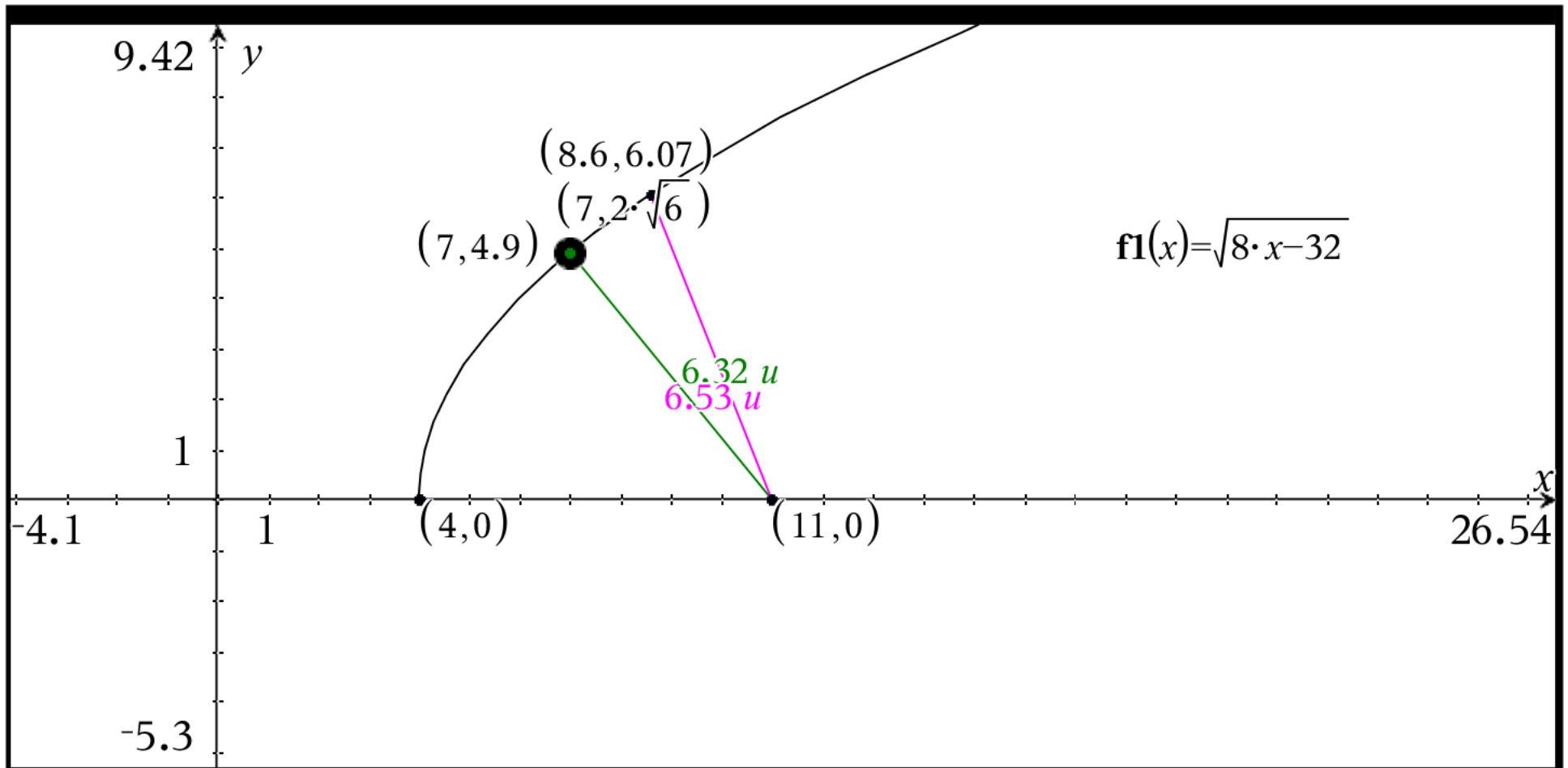
Roots of Derivative Function  $x = 7$

Closest Point on the Given function to the fixed point at (11,0)

is at  $x = 7$  and  $y = \sqrt{8 \cdot 7 - 32} = 2 \cdot \sqrt{6} \approx 4.9$  or  $(7, \sqrt{24})$

The minimum distance from the fixed point (11,0) to the given function is

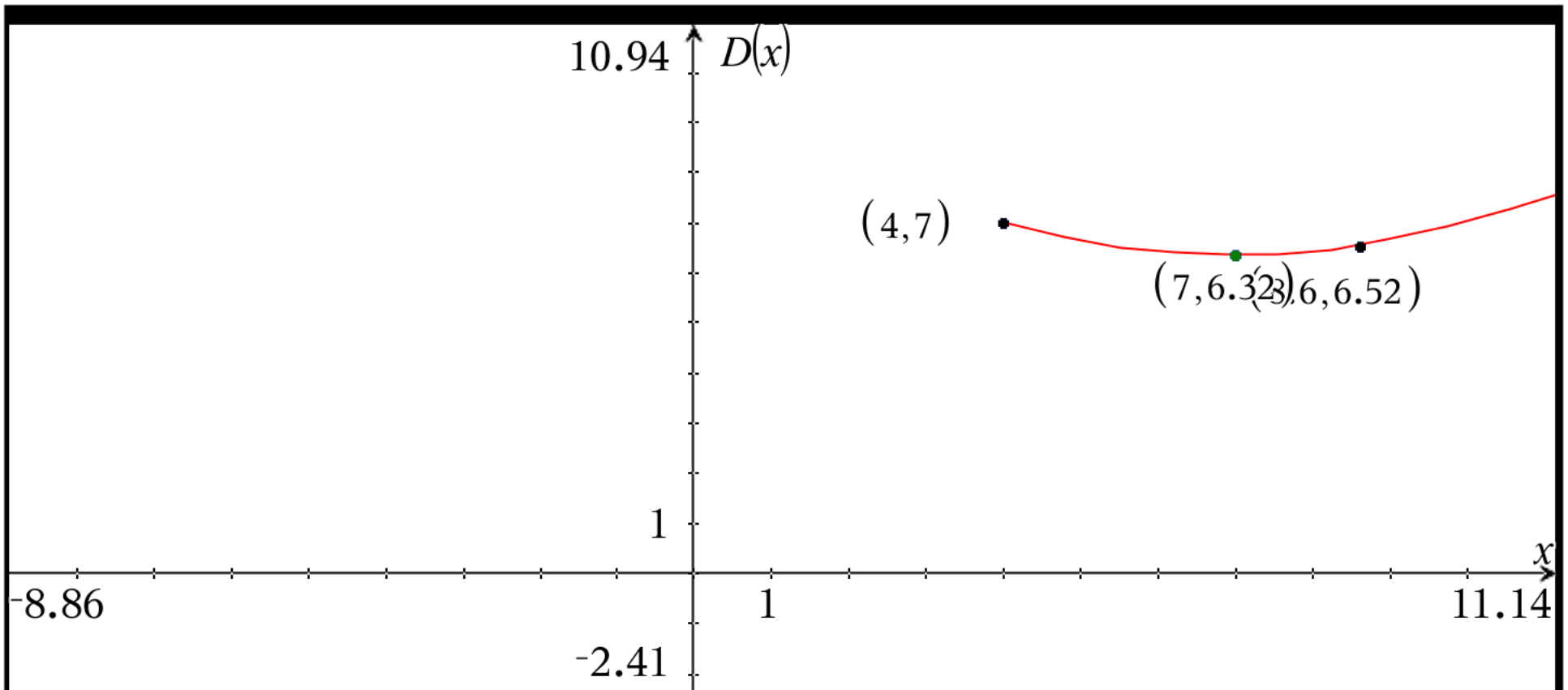
$D(7) = 2 \cdot \sqrt{10} \approx 6.32$



< > any\_x = 8.6

The graph on the graph above is the given function

$$y = 2 \cdot \sqrt{2 \cdot (x - 4)}$$

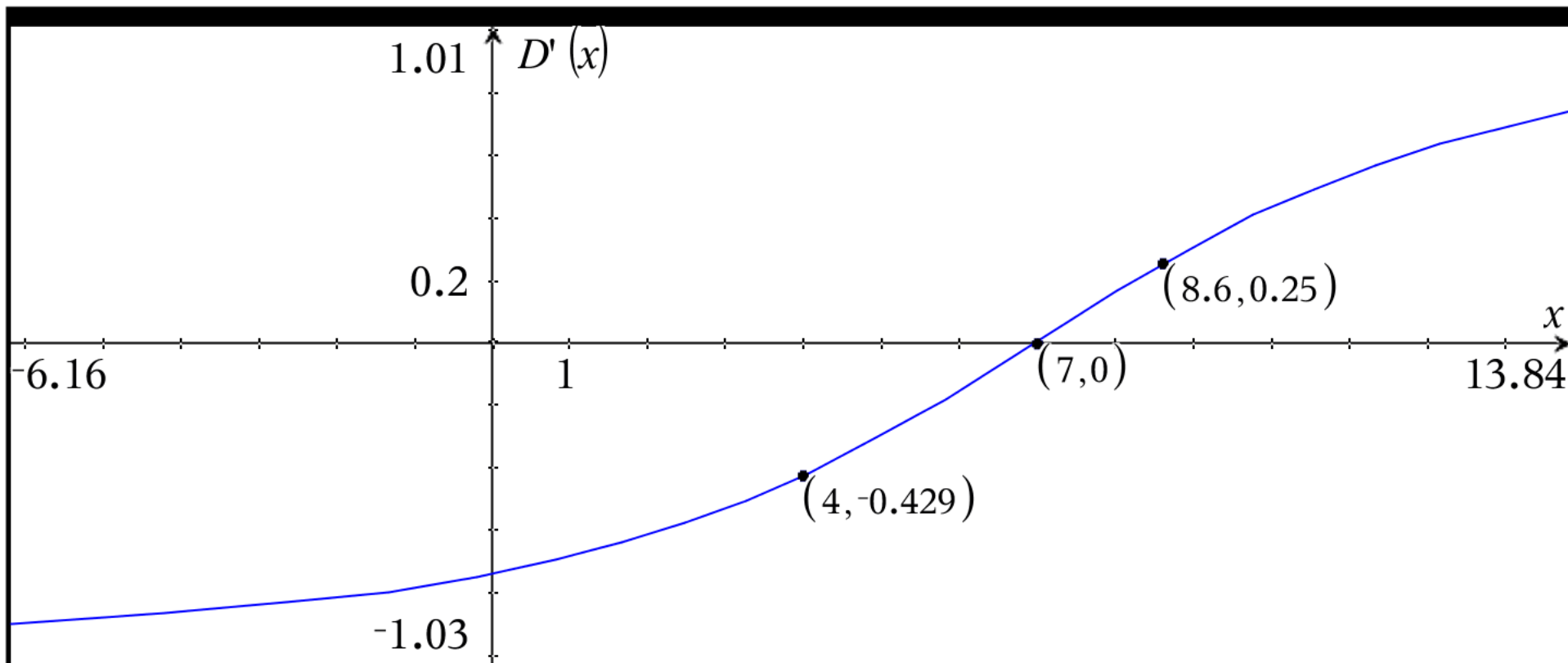


< > any\_x = 8.6

The graph above is the distance function that measures distance from fixed point  $(6, 0)$  to the given function  $y = 2 \cdot \sqrt{2 \cdot (x-4)}$

The graph of the above is the distance function

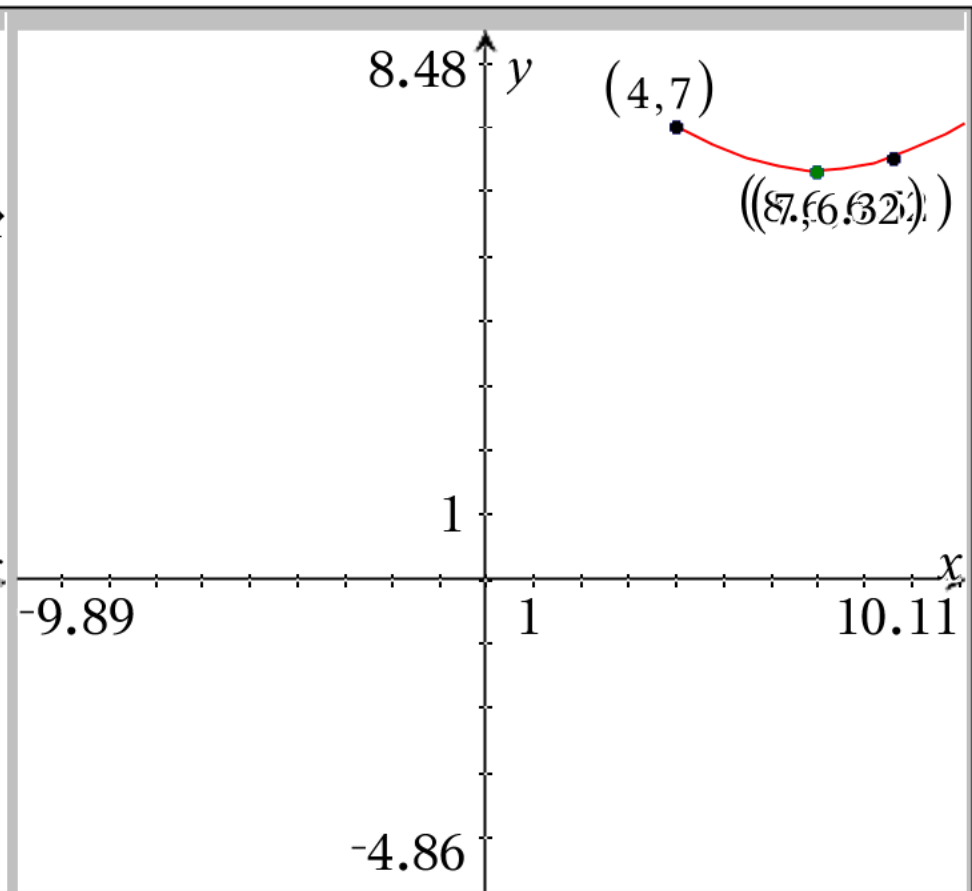
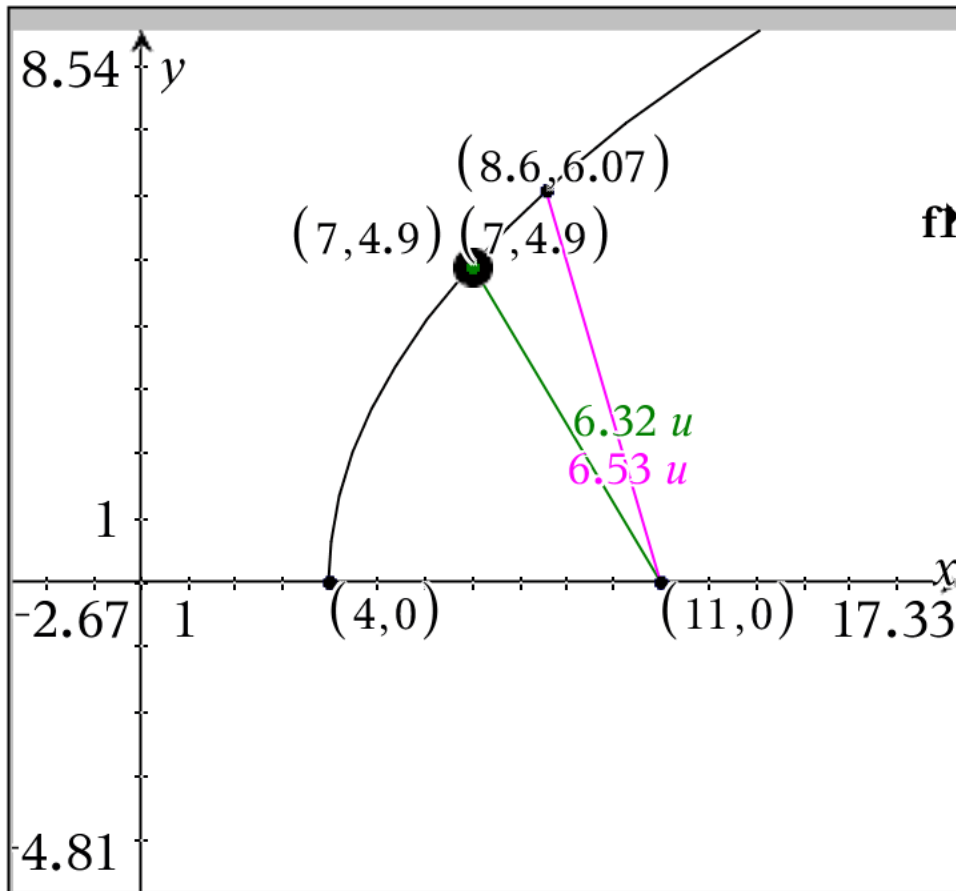
$$D(x) = \sqrt{x^2 - 14 \cdot x + 89}$$



any\_x = 8.6

The graph of the above is the derivative of the distance function

$$D'(x) = \frac{x-7}{\sqrt{x^2-14 \cdot x+89}}$$



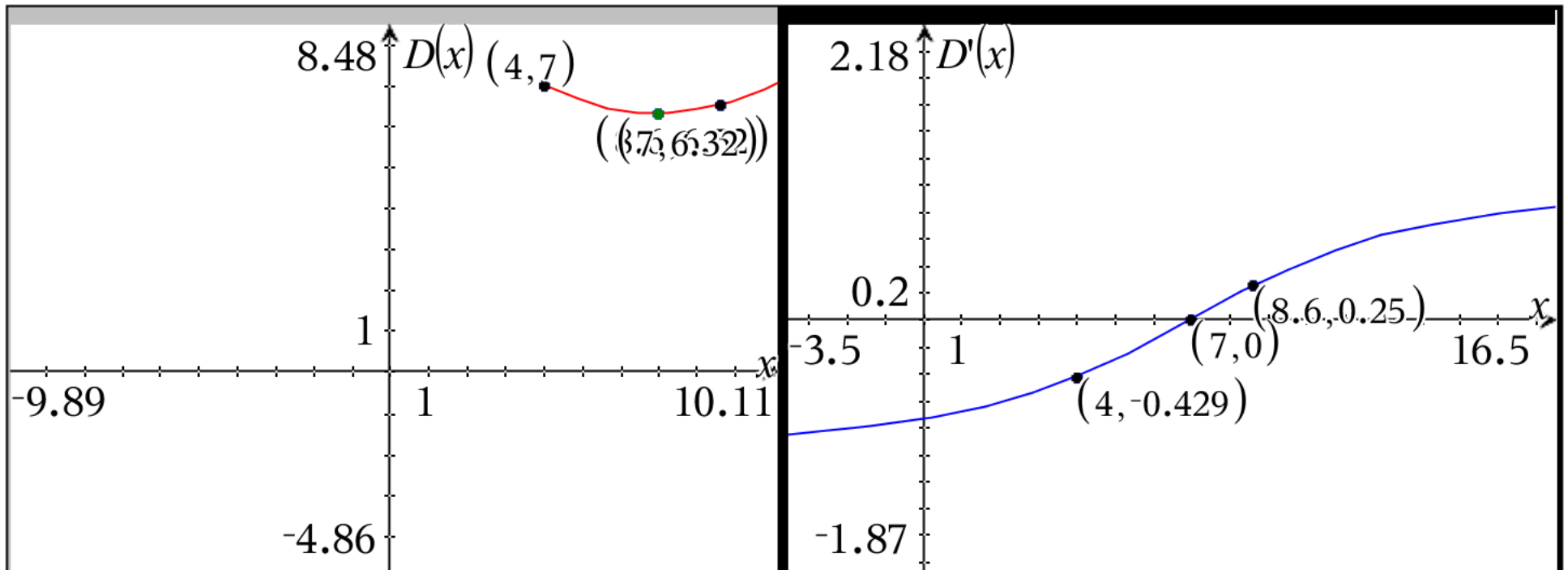
< > any\_x = 8.6

The graph on the left is the given function

$$y = 2 \cdot \sqrt{2 \cdot (x - 4)}$$

The graph of the right is the distance

$$\text{function } D(x) = \sqrt{x^2 - 14 \cdot x + 89}$$



< > any\_x = 8.6

The graph on the left is the distance

function  $y = \sqrt{x^2 - 14 \cdot x + 89}$

The graph of the right is the derivative of the distance function

$$D'(x) = \frac{x-7}{\sqrt{x^2 - 14 \cdot x + 89}}$$