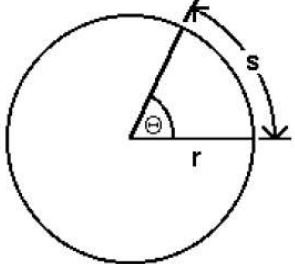


**Angular Speed** --- angle covered for a given time, described in units like revolutions per minute, degrees per second, radians per hour, etc.

**Linear Speed** --- the distance travelled for a given time, described as speed units: meters per second, miles per hour, etc.

## Student Handout

### ANGULAR & LINEAR SPEED: TRIGONOMETRY

<p><b><u>Definitions of Symbols</u></b>            C = circumference            r = radius            d = diameter (<math>d = 2r</math>)            s = arc length  <math>\Theta</math> = central angle <i>in radians</i>  <math>\pi</math> = approximately 3.14</p> <p><b><u>Formulas</u></b>  <math>C = 2\pi r = \pi d</math> and <math>\Theta = \frac{s}{r}</math></p>	 <p>The diagram shows a circle with a center point. A radius is drawn from the center to the circumference, labeled 'r'. A central angle is drawn at the center, labeled 'Θ'. The arc length of this angle is labeled 's'.</p>	<p><b><u>Relationships</u></b>            1 revolution = 1 turn around circle            (<b>definition</b>)</p> <p>1 revolution = <math>2\pi</math> radians            (<i>angular</i> measurement)</p> <p>1 revolution = <math>2\pi r</math>            (<i>linear</i> measurement, i.e. <b>distance</b>)</p>
<p>NOTES:</p>	<p>when <math>s = r</math>, <math>\Theta = 1</math> radian</p>	<p>when <math>s = C</math>, <math>\Theta = 2\pi</math> radians</p>

Ex. Complete the following conversions.

1. 1200 ft per min = \_\_\_\_\_ ft per sec.

2. 55 in per min = \_\_\_\_\_ ft per min

3. 60 mph = \_\_\_\_\_ ft per hr

4. 60 mph = \_\_\_\_\_ ft per sec

5. 24,000 ft per min = \_\_\_\_\_ mph

6. 49 in per sec = \_\_\_\_\_ ft per min

Ex. Find the linear speed for each circular object.

7. radius = 4.5 in and 3 revolutions per min

\_\_\_\_\_ in per min

8. diameter = 10 ft and 6 revolutions per sec

\_\_\_\_\_ ft per sec

9. A roller with diameter 16 in makes 5 revolutions per sec. Find the speed in ft per sec.

10. A wheel with radius 15 inches turns at 35 mph. Find the number of revolutions per minute for the wheel.

Ex. Find the angular speed for each.

9. 12 revolutions per sec = \_\_\_\_\_ radians per sec

10. 4 revolutions per minute = \_\_\_\_\_ radians per min

11. 62 revolutions per min = \_\_\_\_\_ radians per hr

12. 1750 revolutions per hr = \_\_\_\_\_ radians per min

Ex. Solve.

1. A phonograph record has a radius of 3 in and revolves at 45 RPM. Find the linear speed of the outside edge of the record.

2. A car is traveling 60 mph. The diameter of the wheels is 3 ft.

a) Find the number of revolutions per minute the wheels are rotating.

b) What is the angular speed of the wheels in radians per minute?