

$$f(x) = \frac{2x+10}{x-6} = \frac{2 \cdot (x+5)}{x-6}$$

x intercept $(-5, 0)$

HOW? Set numerator = 0 and solve for x

$$y \text{ intercept } (0, \frac{-10}{6}) = (0, \frac{-5}{3})$$

HOW? Set $x = 0$ and evaluate $f(0)$

vertical asymptote at $x = 6$

HOW? Set denominator = 0 and solve for x

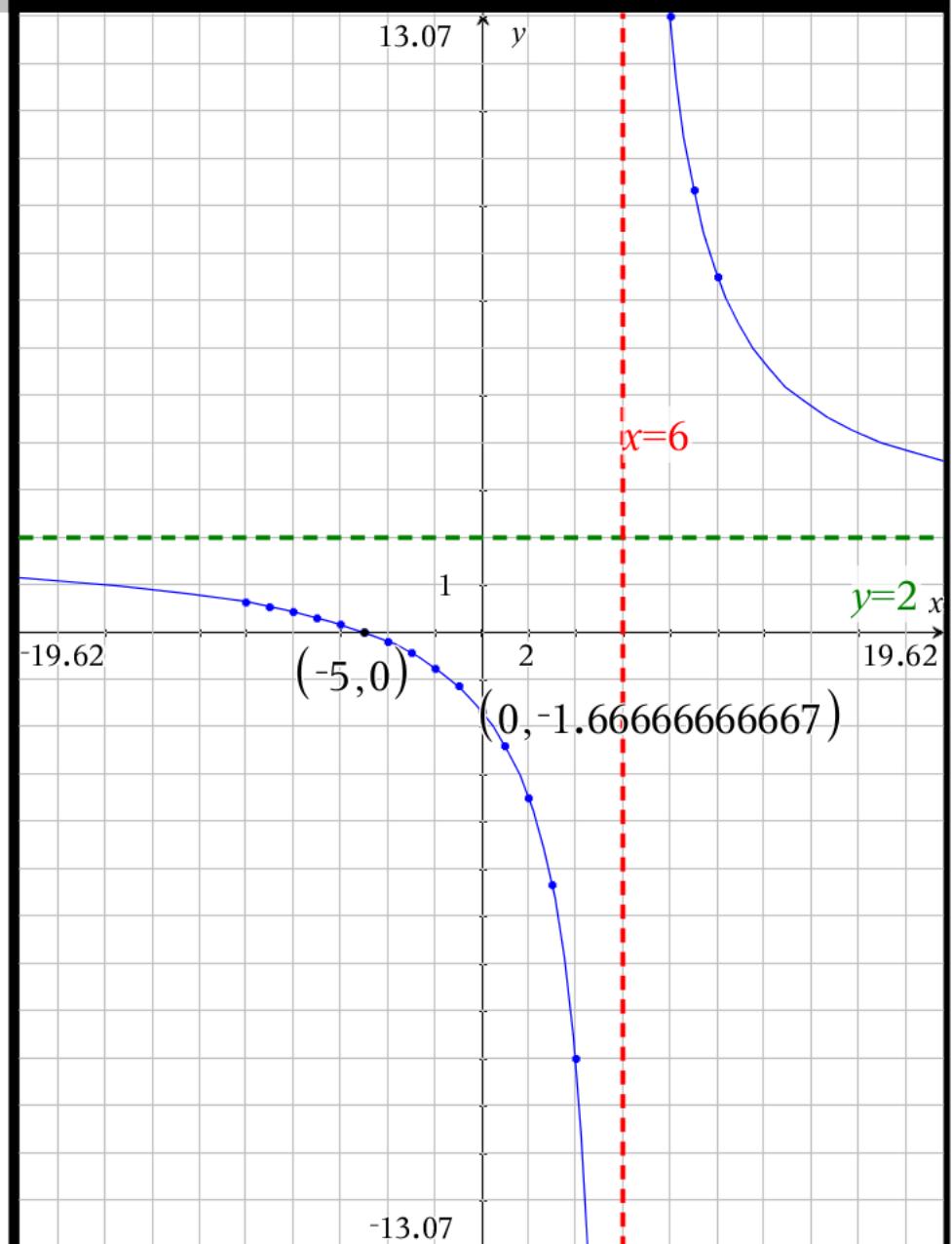
horizontal asymptote at $y = 2$

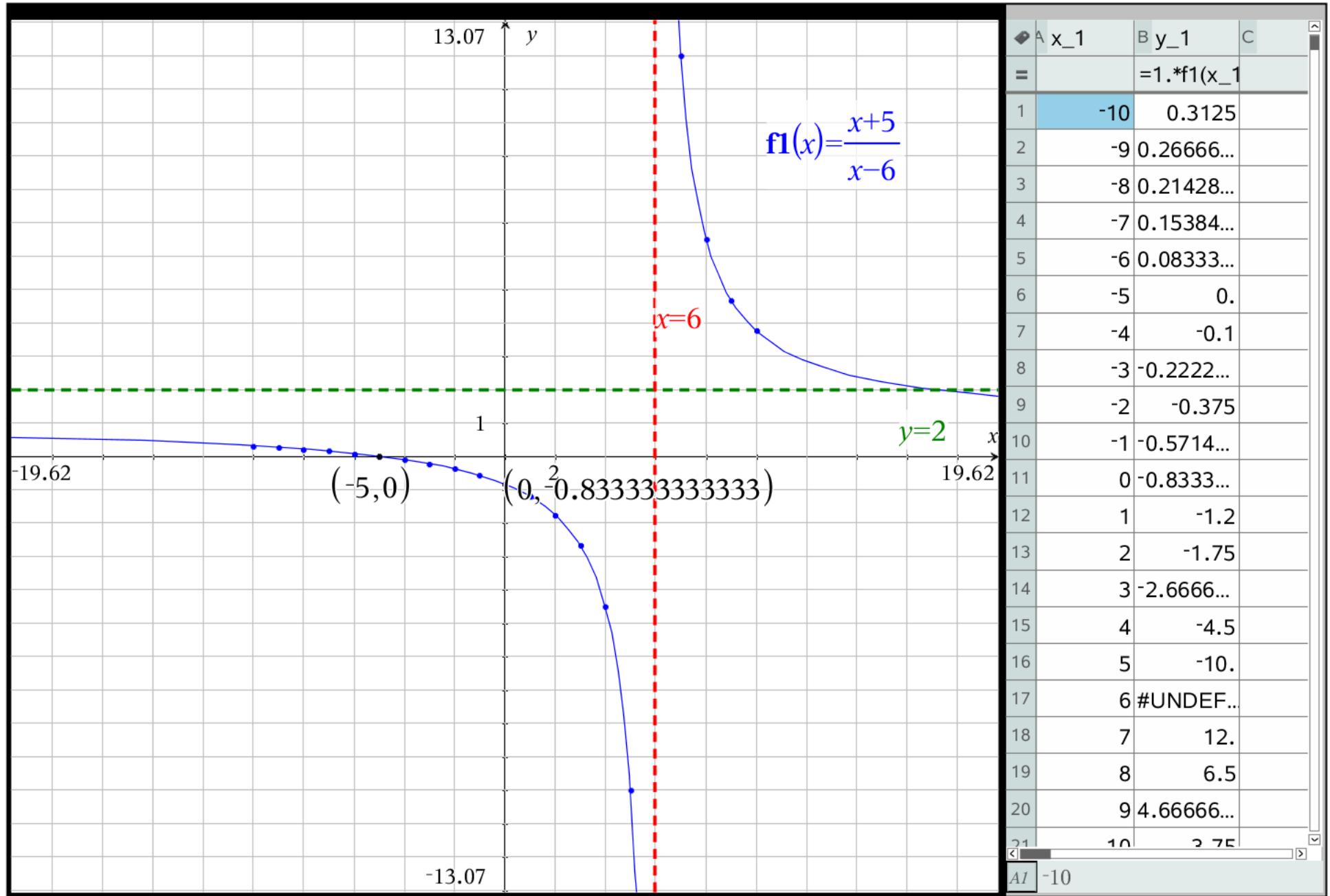
HOW?

Method 1) Lead coefficient over lead coefficient

Method 2) Division quotient

Method 3) Synthetic division quotient





$$g(x) = \frac{x+5}{x-6}$$

x intercept $(-5, 0)$

HOW? Set numerator = 0 and solve for x

y intercept $(0, \frac{-5}{6})$

HOW? Set $x = 0$ and evaluate $g(0)$

vertical asymptote at $x = 6$

HOW? Set denominator = 0 and solve for x

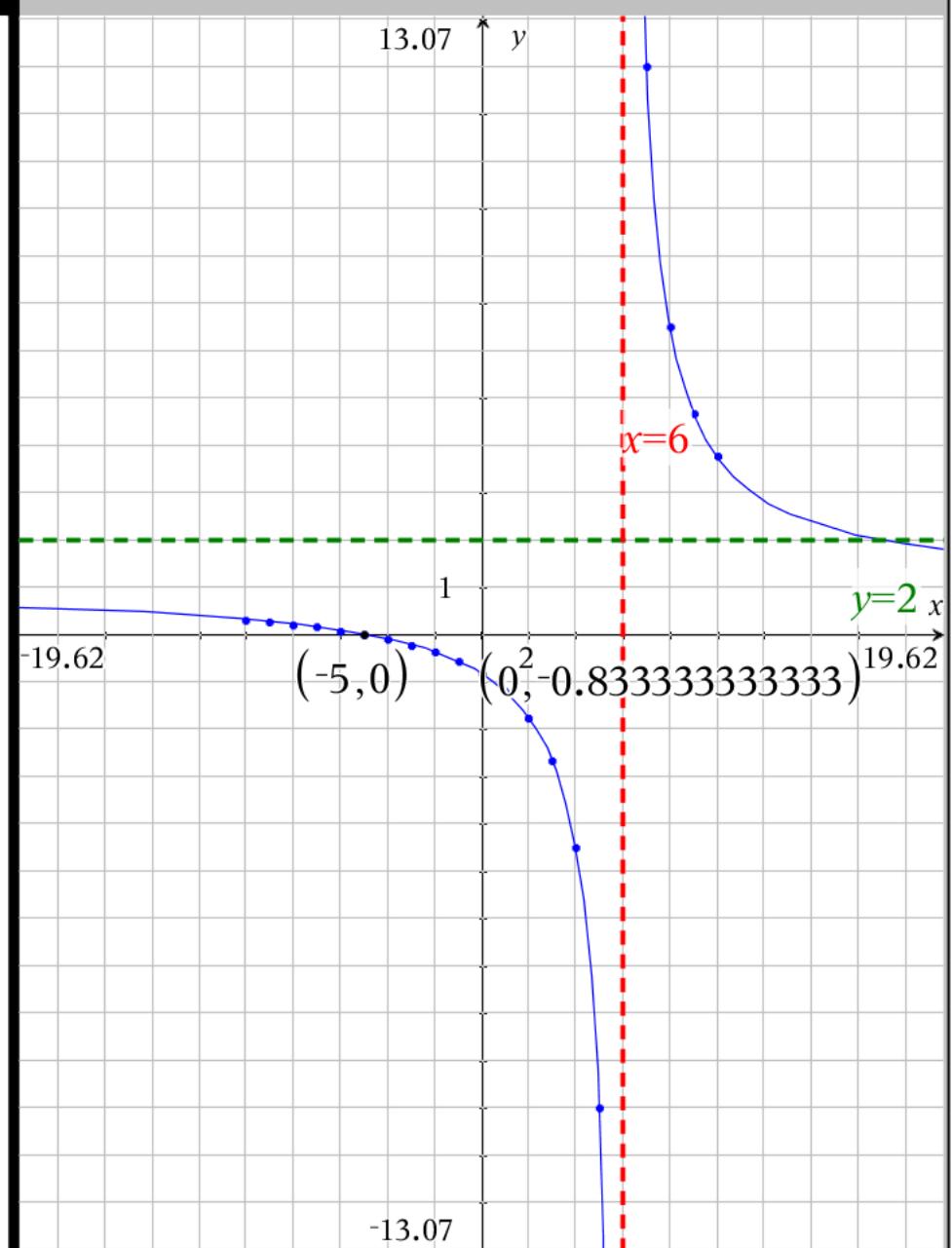
horizontal asymptote at $y = 1$

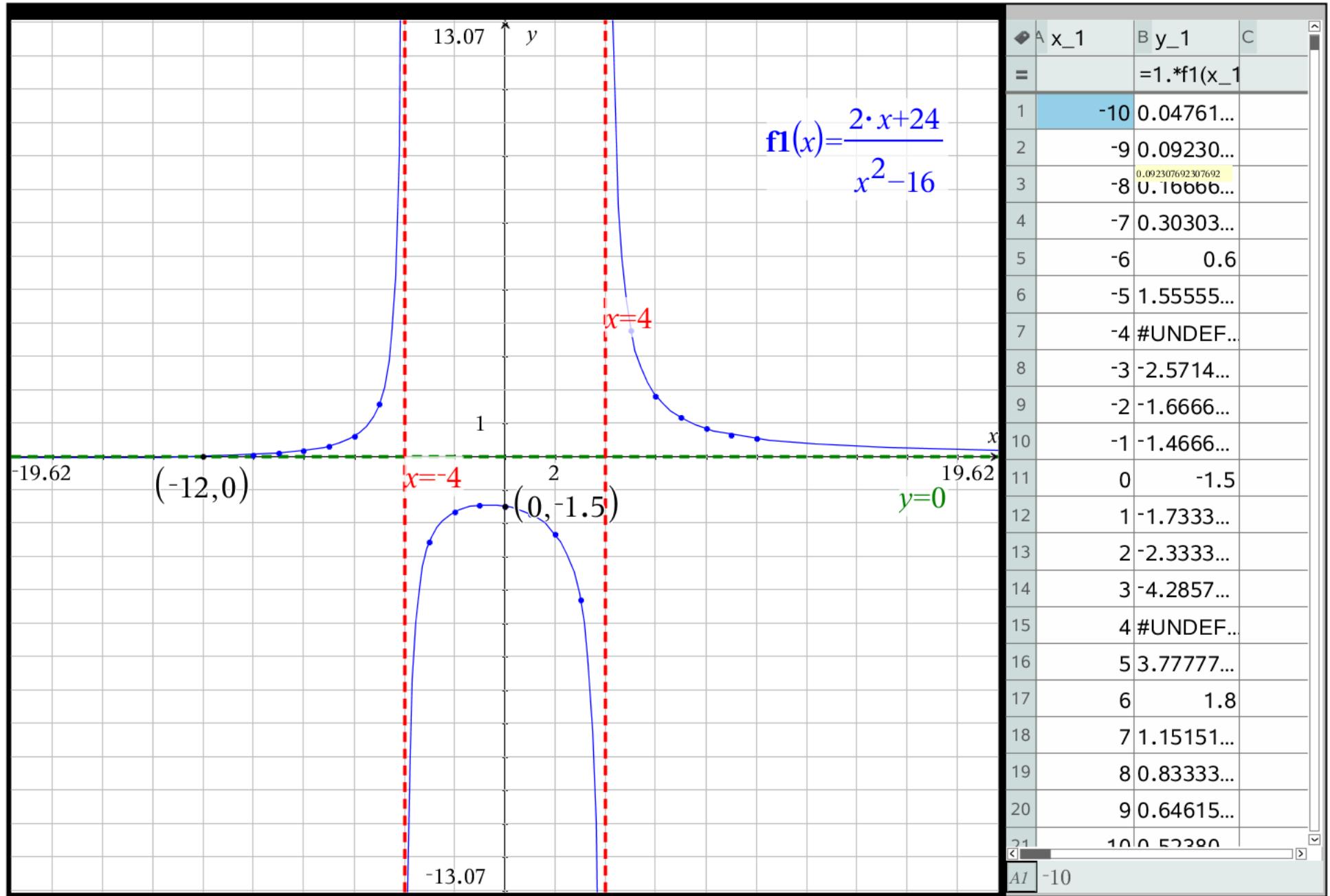
HOW?

Method 1) Lead coefficient over lead coefficient

Method 2) Division quotient

Method 3) Synthetic division quotient





$$h(x) = \frac{2x+24}{x^2 - 16} = \frac{2(x+12)}{(x+4)(x-4)}$$

x intercept $(-12, 0)$

HOW? Set numerator = 0 and solve for x

$$\text{y intercept } (0, \frac{-24}{16}) = (0, -1.5)$$

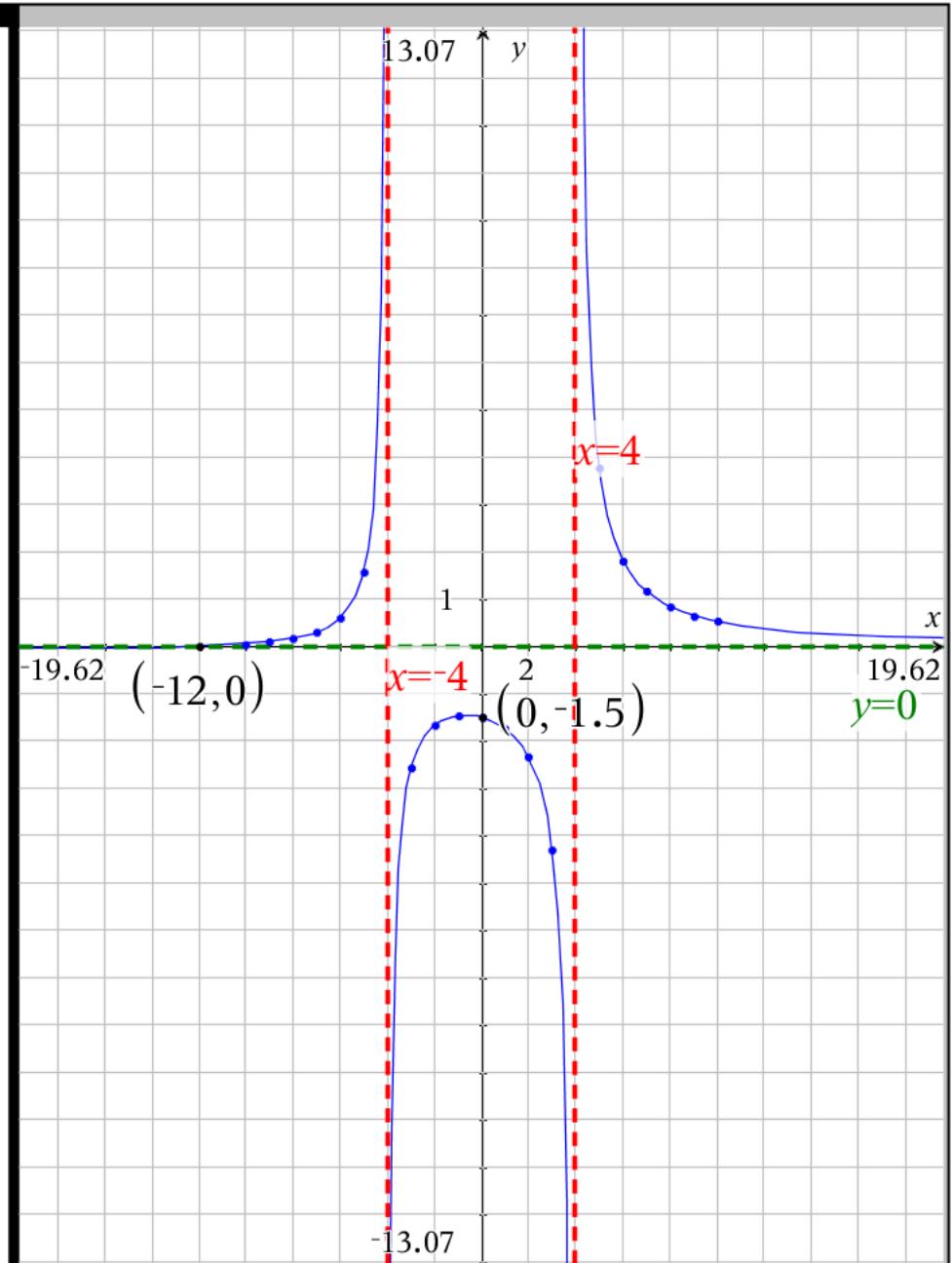
HOW? Set $x = 0$ and evaluate $h(0)$

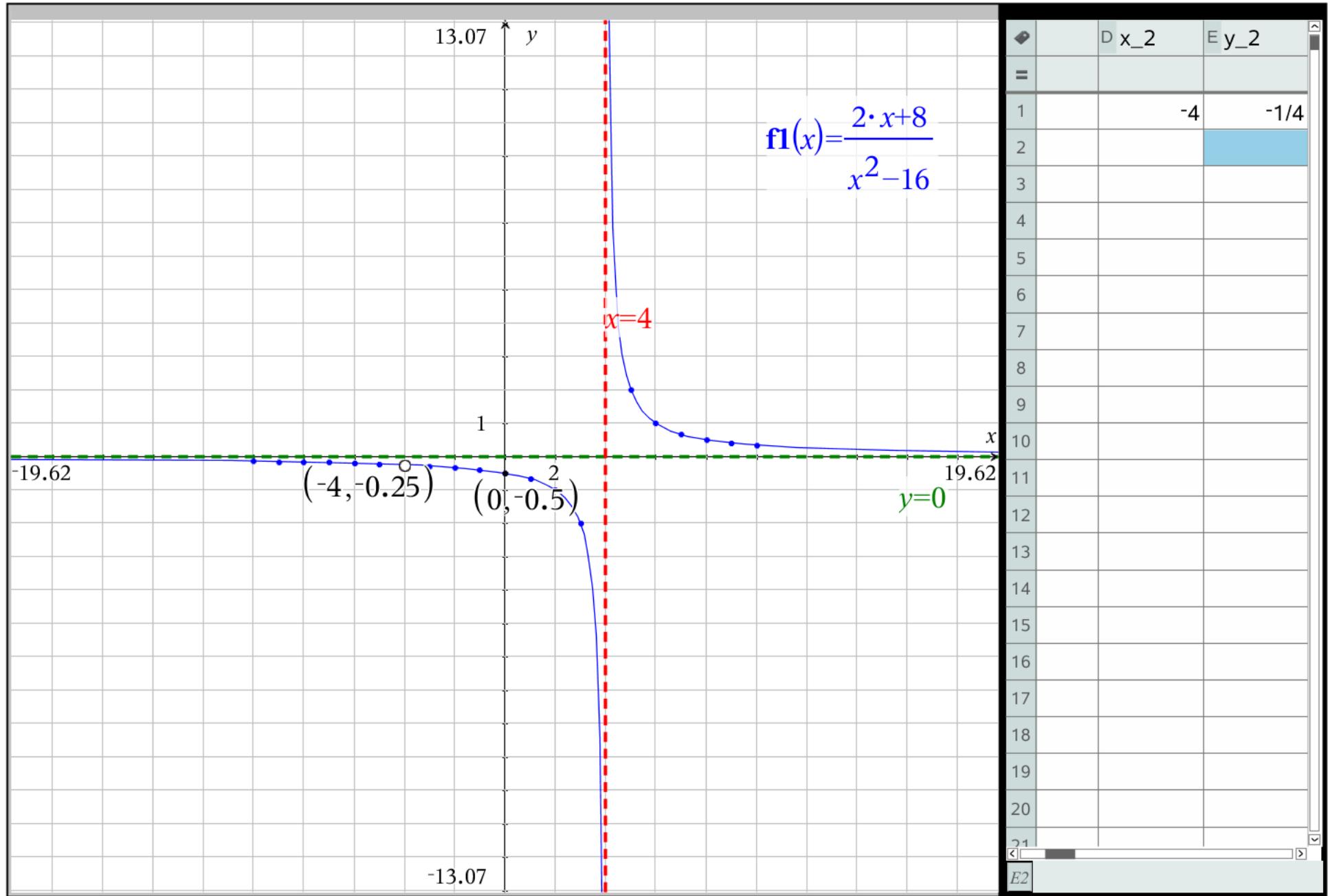
vertical asymptote at $x = -4$ and $x = 4$

HOW? Set denominator = 0 and solve for x

horizontal asymptote at $y = 0$

HOW? when degree of numerator is less than the degree of the denominator, the x axis is the horizontal asymptote





$$j(x) = \frac{2x+8}{x^2-16} = \frac{2(x+4)}{(x+4)(x-4)} = \frac{2}{x-4} \text{ with } x \neq -2$$

HOLE OCCURS!

x intercept NONE

WHY?

reduced version has no x in numerator

$$\text{y intercept } (0, \frac{-8}{16}) = (0, \frac{-1}{2})$$

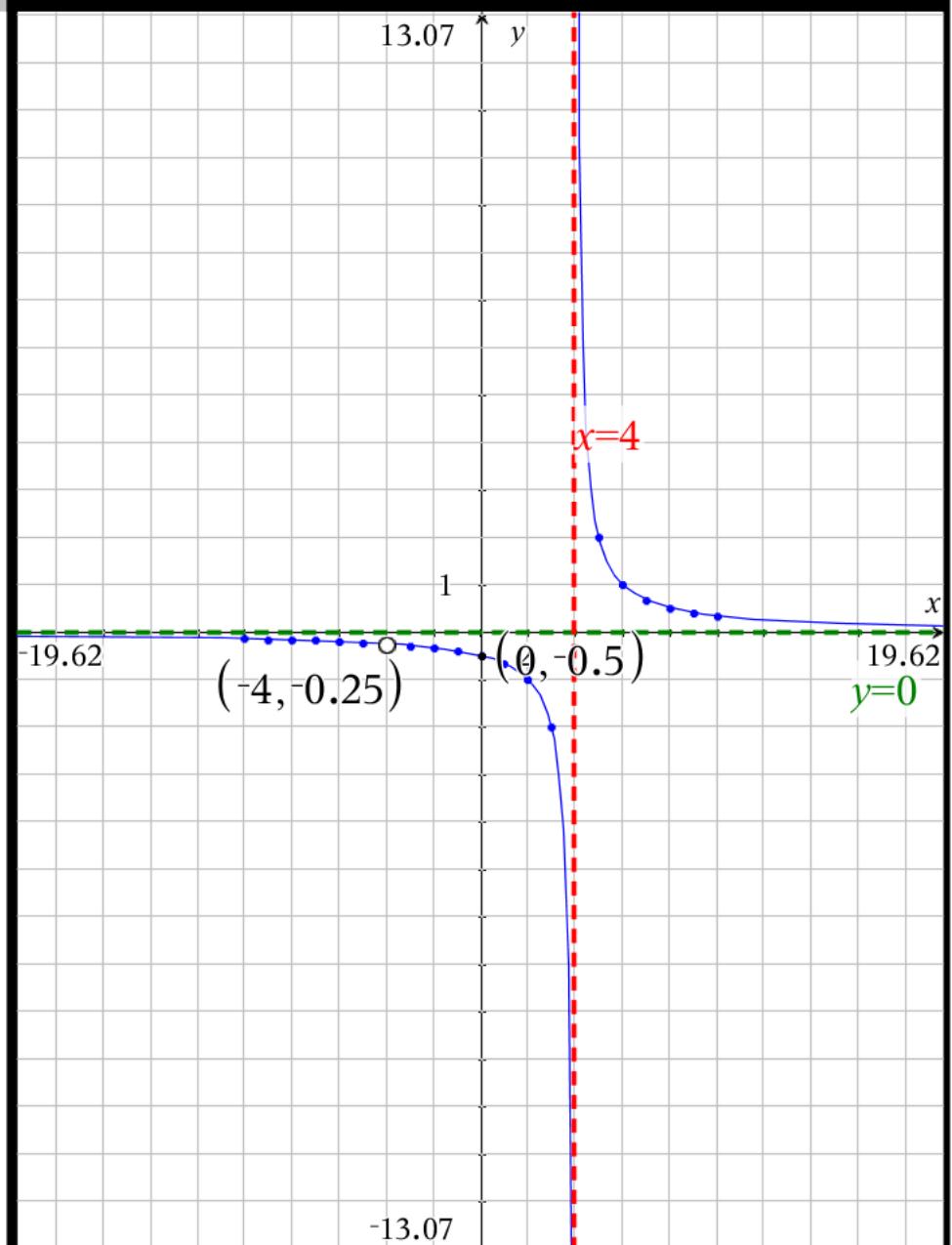
HOW? Set $x = 0$ and evaluate $j(0)$

vertical asymptote at $x = 4$ and x NOT at -4

HOW? Set denominator = 0 and solve for x

horizontal asymptote at $y = 0$

HOW? when degree of numerator is less than the degree of the denominator, the x axis is the horizontal asymptote



$$j(x) = \frac{2x+8}{x^2-16} = \frac{2(x+4)}{(x+4)(x-4)} = \frac{2}{x-4} \text{ with } x \neq -4$$

HOLE OCCURS!

1) since we cancelled $x+4$

2) we set $x + 4 = 0$

3) solve for x and we get $x = -4$

THIS IS X of HOLE

4) replace $x = -4$ into SIMPLIFIED rational function to find y coordinate of hole

$$\frac{2}{-4-4} = \frac{-1}{4}$$

5) HOLE $(-4, \frac{-1}{4})$

