matrix A = 
$$\begin{bmatrix} \mathbf{a} & \mathbf{11} & \mathbf{a} & \mathbf{12} & \mathbf{a} & \mathbf{13} \\ \mathbf{a} & \mathbf{21} & \mathbf{a} & \mathbf{22} & \mathbf{a} & \mathbf{23} \\ \mathbf{a} & \mathbf{31} & \mathbf{a} & \mathbf{32} & \mathbf{a} & \mathbf{33} \end{bmatrix} = \begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
 matrix E =  $\begin{bmatrix} \mathbf{e} & \mathbf{11} & \mathbf{e} & \mathbf{12} & \mathbf{e} & \mathbf{13} \end{bmatrix} = \begin{bmatrix} 6 & -7 & -2 \end{bmatrix}$ 

matrix B = 
$$\begin{bmatrix} \mathbf{b} - 11 & \mathbf{b} - 12 & \mathbf{b} - 13 \\ \mathbf{b} - 21 & \mathbf{b} - 22 & \mathbf{b} - 23 \end{bmatrix} = \begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$$

matrix B = 
$$\begin{bmatrix} \mathbf{b} \ 11 & \mathbf{b} \ 21 & \mathbf{b} \ 22 & \mathbf{b} \ 23 \end{bmatrix} = \begin{bmatrix} 7 & 3 & -2 \ -4 & 5 & 0 \end{bmatrix}$$
 matrix F =  $\begin{bmatrix} \mathbf{f} \ 11 & \mathbf{f} \ 12 & \mathbf{f} \ 13 \ \mathbf{f} \ 21 & \mathbf{f} \ 22 & \mathbf{f} \ 23 \ \mathbf{f} \ 33 \end{bmatrix} = \begin{bmatrix} 0 & 7 & 5 \ 3 & -4 & 0 \ 0 & 1 & -6 \end{bmatrix}$ 

matrix C = 
$$\begin{bmatrix} \mathbf{c}_{-11} \\ \mathbf{c}_{-21} \\ \mathbf{c}_{-31} \end{bmatrix} = \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix}$$

matrix D = 
$$\begin{bmatrix} d_11 & d_12 & d_13 \\ d_21 & d_22 & d_23 \end{bmatrix} = \begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix}$$

-3C

$$-3\begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} -30 \\ 18 \\ 15 \end{bmatrix}$$

-3 is called the scalar

This is called scalar multiplication

$$D-2B = D+-2B$$

$$\begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix} + -2 \begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$$

We TRY to AVOID subtraction to prevent sign errors

$$\begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix} + \begin{bmatrix} -14 & -6 & 4 \\ 8 & -10 & 0 \end{bmatrix}$$
 Perform scalar multiplication FIRST

$$\begin{bmatrix} -8 & -16 & -3 \\ 5 & -6 & -5 \end{bmatrix}$$
 Then add results

-2 is called the scalar

This has scalar multiplication and matrix addition

Matrix Multiplication

THIS IS ONLY POSSIBLE IF INNER DIMENSIONS ARE EQUAL

Matrix B 
$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$$
 has dimension 2 x 3

Matrix A 
$$\begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
 has dimension 3 x 3

#### CHECK INNER DIMENSION

(2x3) (3x3) the inner dimensions are a match!

IF matrix multiplication is possible,

then the resultant matrix has the OUTER DIMENSION as its size

(2x3) (3x3) the inner dimensions are a match!

So matrix product BA has dimension 2 x 3 
$$\begin{bmatrix} \mathbf{ba}_{-}\mathbf{11} & ba_{-}12 & ba_{-}13 \\ ba_{-}21 & ba_{-}22 & ba_{-}23 \end{bmatrix}$$

Matrix Product BA

matrix A = 
$$\begin{bmatrix} \mathbf{a} \mathbf{11} & \mathbf{a} \mathbf{12} & \mathbf{a} \mathbf{13} \\ \mathbf{a} \mathbf{21} & \mathbf{a} \mathbf{22} & \mathbf{a} \mathbf{23} \\ \mathbf{a} \mathbf{31} & \mathbf{a} \mathbf{32} & \mathbf{a} \mathbf{33} \end{bmatrix} = \begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
 matrix B =  $\begin{bmatrix} \mathbf{b} \mathbf{11} & \mathbf{b} \mathbf{12} & \mathbf{b} \mathbf{13} \\ \mathbf{b} \mathbf{21} & \mathbf{b} \mathbf{22} & \mathbf{b} \mathbf{23} \end{bmatrix} = \begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$ 

(remember the address tells us the way to the entries)

ba\_11 needs row 1 of matrix B to be multiplied by column 1 of matrix A ba\_12 needs row 1 of matrix B to be multiplied by column 2 of matrix A ba\_13 needs row 1 of matrix B to be multiplied by column 3 of matrix A

ba\_21 needs row 2 of matrix B to be multiplied by column 1 of matrix A ba\_22 needs row 2 of matrix B to be multiplied by column 2 of matrix A ba\_23 needs row 2 of matrix B to be multiplied by column 3 of matrix A

Matrix Product BA

**ROW 1 WORK** 

(remember the address tells us the way to the entries)

ba\_11 needs row 1 of matrix B to be multiplied by column 1 of matrix A

$$\begin{bmatrix} 7 & 3 & -2 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix} = (7)(1)+(3)(2)+(-2)(-3)=7+6+6=[19]$$
 This is the entry at ba\_11

ba\_12 needs row 1 of matrix B to be multiplied by column 2 of matrix A

$$\begin{bmatrix} 7 & 3 & -2 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \\ 5 \end{bmatrix} = (7)(4) + (3)(0) + (-2)(5) = 28 + 0 + -10 = [18]$$
 This is the entry at ba\_12

ba\_13 needs row 1 of matrix B to be multiplied by column 3 of matrix A

$$\begin{bmatrix} 7 & 3 & -2 \end{bmatrix} \begin{bmatrix} -7 \\ 3 \\ -1 \end{bmatrix} = (7)(-7)+(3)(3)+(-2)(-1)=-49+9+2= \begin{bmatrix} -38 \end{bmatrix}$$
 This is the entry at ba\_13

Matrix Product BA

**ROW 2 WORK** 

(remember the address tells us the way to the entries)

ba\_21 needs row 2 of matrix B to be multiplied by column 1 of matrix A

$$\begin{bmatrix} -4 & 5 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix} = (-4)(1)+(5)(2)+(0)(-3)=-4+10+0=[6]$$
 This is the entry at ba\_21

ba\_22 needs row 2 of matrix B to be multiplied by column 2 of matrix A

$$\begin{bmatrix} -4 & 5 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \\ 5 \end{bmatrix} = (-4)(4)+(5)(0)+(0)(5)=-16+0+0=[-16]$$
 This is the entry at ba\_22

ba\_23 needs row 2 of matrix B to be multiplied by column 3 of matrix A

$$\begin{bmatrix} -4 & 5 & 0 \end{bmatrix} \begin{bmatrix} -7 \\ 3 \\ -1 \end{bmatrix} = (-4)(-7)+(5)(3)+(0)(-1)=28+15+0=[43]$$
 This is the entry at ba\_23

NOW TECHNOLOGY certainly can be used to accomplish the multiplication of two matrices, but we do expect that you will be able to do both methods (by hand and with the assistance of a graphing calculator)

matrix A = 
$$\begin{bmatrix} \mathbf{a} & \mathbf{11} & \mathbf{a} & \mathbf{12} & \mathbf{a} & \mathbf{13} \\ \mathbf{a} & \mathbf{21} & \mathbf{a} & \mathbf{22} & \mathbf{a} & \mathbf{23} \\ \mathbf{a} & \mathbf{31} & \mathbf{a} & \mathbf{32} & \mathbf{a} & \mathbf{33} \end{bmatrix} = \begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
matrix B = 
$$\begin{bmatrix} \mathbf{b} & \mathbf{11} & \mathbf{b} & \mathbf{12} & \mathbf{b} & \mathbf{13} \\ \mathbf{b} & \mathbf{21} & \mathbf{b} & \mathbf{22} & \mathbf{b} & \mathbf{23} \end{bmatrix} = \begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$$
BA = 
$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} \begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix} = \begin{bmatrix} 19 & 18 & -38 \\ 6 & -16 & 43 \end{bmatrix}$$

MATRIX MULTIPLICATION IS NOT COMMUTATIVE!

(unless dealing with VERY special matrices!)

Matrix Multiplication

THIS IS ONLY POSSIBLE IF INNER DIMENSIONS ARE EQUAL

Matrix B 
$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$$
 has dimension 2 x 3

Matrix A 
$$\begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
 has dimension 3 x 3

#### CHECK INNER DIMENSION

(3x3) (2x3) the inner dimensions are NOT a match!

SO matrix multiplication is IMPOSSIBLE, WHY?

lets try to multiply row 1 of matrix A by column 1 of matrix B

$$\begin{bmatrix} 1 & 4 & -7 \end{bmatrix} \begin{bmatrix} 7 \\ -4 \end{bmatrix} = \begin{bmatrix} \mathbf{a} \mathbf{11} & \mathbf{a} \mathbf{12} & \mathbf{a} \mathbf{13} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{b} \mathbf{11} \\ \mathbf{b} \mathbf{21} \end{bmatrix} = \text{Error: Dimension error}$$

each number (entry) in the row of matrix A must correspond to a number (entry) in the column of matrix B. THIS CANNOT happen UNLESS inner dimension is EQUAL!

matrix B = 
$$\begin{bmatrix} \mathbf{b} \\ \mathbf{11} \\ \mathbf{b} \\ \mathbf{21} \end{bmatrix}$$
  $\begin{bmatrix} \mathbf{b} \\ \mathbf{22} \\ \mathbf{b} \\ \mathbf{23} \end{bmatrix}$  =  $\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix}$   
matrix D =  $\begin{bmatrix} \mathbf{d} \\ \mathbf{11} \\ \mathbf{d} \\ \mathbf{21} \end{bmatrix}$   $\begin{bmatrix} \mathbf{d} \\ \mathbf{12} \end{bmatrix}$   $\begin{bmatrix} \mathbf{d} \\ \mathbf{13} \\ \mathbf{d} \\ \mathbf{23} \end{bmatrix}$  =  $\begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix}$   
matrix C =  $\begin{bmatrix} \mathbf{c} \\ \mathbf{11} \\ \mathbf{c} \\ \mathbf{21} \end{bmatrix}$  =  $\begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix}$ 

Note this is Matrix Subtraction (Addition of opposite) followed by Matrix Multiplication

$$(B-D)C = (B +-D)C$$

Step 1) Change signs of matrix D

Step 2) Add B to -D

Step 3) Check inner dimension of matrix B-D (2x3) and matrix C (3x1)

 $(2x_3)$   $(3x_1)$  We can multiply the matrices and the resultant matrix has dimension 2x1 (matrix addition and subtraction does NOT change dimensions)

Step 4 Multiply matrix B -D and matrix C

Problem 5 cont

Problem 5 cont
$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} - 1 \begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} + -1 \begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} + \begin{bmatrix} -6 & 10 & 7 \\ 3 & -4 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 13 & 5 \\ -1 & 1 & 5 \end{bmatrix}$$
Notice the SIZE of the matrix did not change!

B -D = 
$$\begin{bmatrix} 1 & 13 & 5 \\ -1 & 1 & 5 \end{bmatrix}$$
 Notice the SIZE of the matrix did not change

$$(B-D)C = \begin{bmatrix} 1 & 13 & 5 \\ -1 & 1 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} 1 & 13 & 5 \\ -6 & 1 & 5 \end{bmatrix}$$

this is what the resultant matrix looks like

#### **ROW 1 WORK**

(remember the address tells us the way to the entries)

(b-d)c\_11 needs row 1 of matrix B-D to be multiplied by column 1 of matrix C

$$\begin{bmatrix} 1 & 13 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = (1)(10) + (13)(-6) + (5)(-5) = 10 + -78 + -25 = \begin{bmatrix} -93 \end{bmatrix}$$
 This is the entry at (b-d)c\_11

#### **ROW 2 WORK**

(remember the address tells us the way to the entries)

(b-d)c\_21 needs row 2 of matrix B-D to be multiplied by column 1 of matrix C

(b-d)c\_21 needs row 2 of matrix B-D to be multiplied by column 1 of matrix C
$$\begin{bmatrix} -1 & 1 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = (-1)(10) + (1)(-6) + (5)(-5) = -10 + -6 + -25 = \begin{bmatrix} -41 \end{bmatrix}$$
 This is the entry at (b-d)c\_21

$$\begin{bmatrix}
 -5 \end{bmatrix}$$

$$OR\begin{bmatrix} 1 & 13 & 5 \\ -1 & 1 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} -93 \\ -41 \end{bmatrix}$$

NOTE: IF given TECHNOLOGY, you can go directly to inputting the matrices all at same time

$$\begin{bmatrix} 7 & 3 & -2 \\ -4 & 5 & 0 \end{bmatrix} - \begin{bmatrix} 6 & -10 & -7 \\ -3 & 4 & -5 \end{bmatrix} ) \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} -93 \\ -41 \end{bmatrix}$$

JUST REMEMBER THE ()'s and it should do it all at once!

matrix A = 
$$\begin{bmatrix} \mathbf{a} & \mathbf{11} & \mathbf{a} & \mathbf{12} & \mathbf{a} & \mathbf{13} \\ \mathbf{a} & \mathbf{21} & \mathbf{a} & \mathbf{22} & \mathbf{a} & \mathbf{23} \\ \mathbf{a} & \mathbf{31} & \mathbf{a} & \mathbf{32} & \mathbf{a} & \mathbf{33} \end{bmatrix} = \begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix}$$
 matrix F = 
$$\begin{bmatrix} \mathbf{f} & \mathbf{11} & \mathbf{f} & \mathbf{12} & \mathbf{f} & \mathbf{13} \\ \mathbf{f} & \mathbf{21} & \mathbf{f} & \mathbf{22} & \mathbf{f} & \mathbf{23} \\ \mathbf{f} & \mathbf{31} & \mathbf{f} & \mathbf{32} & \mathbf{f} & \mathbf{33} \end{bmatrix} = \begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix}$$

2A +3F

Step1) perform BOTH scalar products

Step 2) add 2A to 3F

$$2\begin{bmatrix} 1 & 4 & -7 \\ 2 & 0 & 3 \\ -3 & 5 & -1 \end{bmatrix} + 3\begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix} = \begin{bmatrix} 2 & 8 & -14 \\ 4 & 0 & 6 \\ -6 & 10 & -2 \end{bmatrix} + \begin{bmatrix} 0 & 21 & 15 \\ 9 & -12 & 0 \\ 0 & 3 & -18 \end{bmatrix}$$
$$= \begin{bmatrix} 2 & 29 & 1 \\ 13 & -12 & 6 \\ -6 & 13 & -20 \end{bmatrix}$$

Problem 7 This problem is a fun one

matrix C = 
$$\begin{bmatrix} \mathbf{c}_{-11} \\ \mathbf{c}_{-21} \\ \mathbf{c}_{-31} \end{bmatrix} = \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix}$$
 matrix E =  $\begin{bmatrix} \mathbf{e}_{-11} & \mathbf{e}_{-12} & \mathbf{e}_{-13} \end{bmatrix} = \begin{bmatrix} 6 & -7 & -2 \end{bmatrix}$  matrix F =  $\begin{bmatrix} \mathbf{f}_{-11} & \mathbf{f}_{-12} & \mathbf{f}_{-13} \\ \mathbf{f}_{-21} & \mathbf{f}_{-22} & \mathbf{f}_{-23} \\ \mathbf{f}_{-31} & \mathbf{f}_{-32} & \mathbf{f}_{-33} \end{bmatrix} = \begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix}$ 

**FCE** 

Step 1 check the inner dimensions

F(3x3) C(3x1) E(1x 3)

FC  $(3x_3)$   $(3x_1)$  the matrix FC will have dimension  $3x_1$ 

(FC) (3x1) E (1x3)

FCE  $(3x_1)$   $(1x_1)$  the matrix FCE will have dimension  $3x_2$ 

Step 2 Find FC

Step 3 Find (FC)(E)

Problem 7 FC

$$FC = \begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix}$$
 This is what FC will look like! and FCE will look like  $\begin{bmatrix} 10 & 10 \\ 10 & 10 \\ 10 & 10 \end{bmatrix}$ 

IF YOU HAVE TECHNOLOGY, you can do this in ONE STEP

$$\mathsf{FC} = \begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} -67 \\ 54 \\ 24 \end{bmatrix}$$

Then (FC)(E)

$$(FC)E = \begin{bmatrix} -67 \\ 54 \\ 24 \end{bmatrix} \begin{bmatrix} 6 & -7 & -2 \end{bmatrix} = \begin{bmatrix} -402 & 469 & 134 \\ 324 & -378 & -108 \\ 144 & -168 & -48 \end{bmatrix} \quad FCE = \begin{bmatrix} -402 & 469 & 134 \\ 324 & -378 & -108 \\ 144 & -168 & -48 \end{bmatrix}$$

OR YOU can do it directly in one step!

FCE = 
$$\begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} \begin{bmatrix} 6 & -7 & -2 \end{bmatrix} = \begin{bmatrix} -402 & 469 & 134 \\ 324 & -378 & -108 \\ 144 & -168 & -48 \end{bmatrix}$$

Problem 7 Matrix Product FC WITHOUT TECHNOLOGY

matrix 
$$F = \begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix}$$
 matrix  $C = \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix}$  FC will look like  $\begin{bmatrix} \Box \\ \Box \\ \Box \end{bmatrix}$ 

COLUMN 1 WORK (remember the address tells us the way to the entries)

fc\_11 needs row 1 of matrix F to be multiplied by column 1 of matrix C

$$\begin{bmatrix} 0 & 7 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = (0)(10) + (7)(-6) + (5)(-5) = 0 + -42 + -25 = \begin{bmatrix} -67 \end{bmatrix}$$
 This is the entry at fc\_11

fc\_21 needs row 2 of matrix F to be multiplied by column 1 of matrix C

$$\begin{bmatrix} 3 & -4 & 0 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = (3)(10) + (-4)(-6) + (0)(-5) = 30 + 24 + 0 = \begin{bmatrix} 54 \end{bmatrix}$$
 This is the entry at fc\_21

fc\_31 needs row 3 of matrix F to be multiplied by column 1 of matrix C

$$\begin{bmatrix} 0 & 1 & -6 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = (0)(10) + (1)(-6) + (-6)(-5) = 0 + -6 + 30 = \begin{bmatrix} 24 \end{bmatrix}$$
 This is the entry at fc\_31

So we NOW know FC = 
$$\begin{bmatrix} 0 & 7 & 5 \\ 3 & -4 & 0 \\ 0 & 1 & -6 \end{bmatrix} \begin{bmatrix} 10 \\ -6 \\ -5 \end{bmatrix} = \begin{bmatrix} -67 \\ 54 \\ 24 \end{bmatrix}$$

Now we need to multiply FC by E

$$(FC)E = \begin{bmatrix} -67 \\ 54 \\ 24 \end{bmatrix} \begin{bmatrix} 6 & -7 & -2 \end{bmatrix}$$

FCE = 
$$\begin{bmatrix} -67 \\ 54 \\ 24 \end{bmatrix}$$
  $\begin{bmatrix} 6 & -7 & -2 \end{bmatrix}$  =  $\begin{bmatrix} -402 & 469 & 134 \\ 324 & -378 & -108 \\ 144 & -168 & -48 \end{bmatrix}$ 

4	Α	В	С	D	E	F	G	Н	I	J	К	L M
=												
1		matrix_a				matrix_c		matrix_e				
2		1	4	-7		10		6	-7	-2		
3		2	0	3		-6				matrix_f		
4		-3	5	-1		-5				0	7	5
5		matrix_b				matrix_d				3	-4	0
6		7	3	-2		6	-10	-7		0	1	-6
7		-4	5	0		-3	4	-5				
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