

## Scenario 2: Arc Length

Known:  $r = 10$ 

$$\theta = \frac{\pi}{6}$$

$$s = \theta \cdot r$$

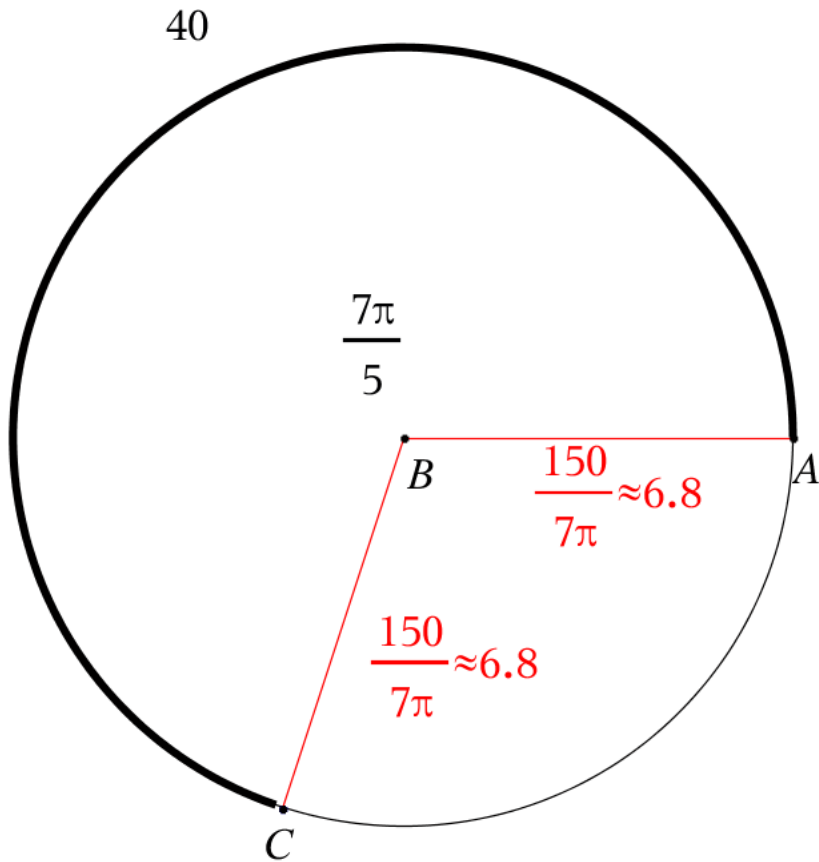
Want  $\theta$ 

1) Write equation

$$s = 10 \cdot \frac{\pi}{6} = \frac{10 \cdot \pi}{6} = \frac{5 \cdot \pi}{3}$$

$$s = \frac{5\pi}{3}$$

$$\text{NOTE } \theta = \frac{\pi}{6} \cdot \frac{180}{\pi} \approx 30^\circ$$



### Scenario 3: Arc Length

Known:  $\theta = \frac{7 \cdot \pi}{5}$

$s = 30$

$s = \theta \cdot r$

Want r

1) Write equation

$$30 = \frac{7 \cdot \pi}{5} \cdot r$$

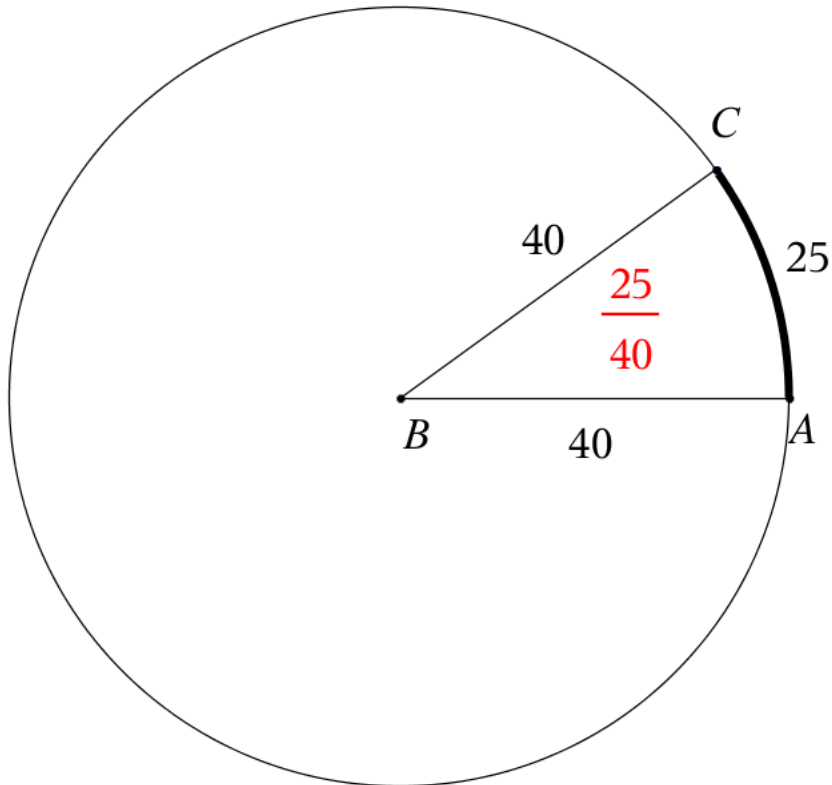
2) Solve equation

$$\frac{30}{1} \cdot \frac{5}{7 \cdot \pi} = \frac{7 \cdot \pi \cdot r}{5} \cdot \frac{5}{7 \cdot \pi}$$

$$r = \frac{150}{7 \cdot \pi} \approx 6.821$$

NOTE  $\theta = \frac{18 \cdot \pi}{40} \cdot \frac{180}{\pi} \circ$

scenario 4



Scenario 4: Arc Length

Known:  $r = 40$

$$s = 25$$

$$s = \theta \cdot r$$

Want  $\theta$

1) Write equation

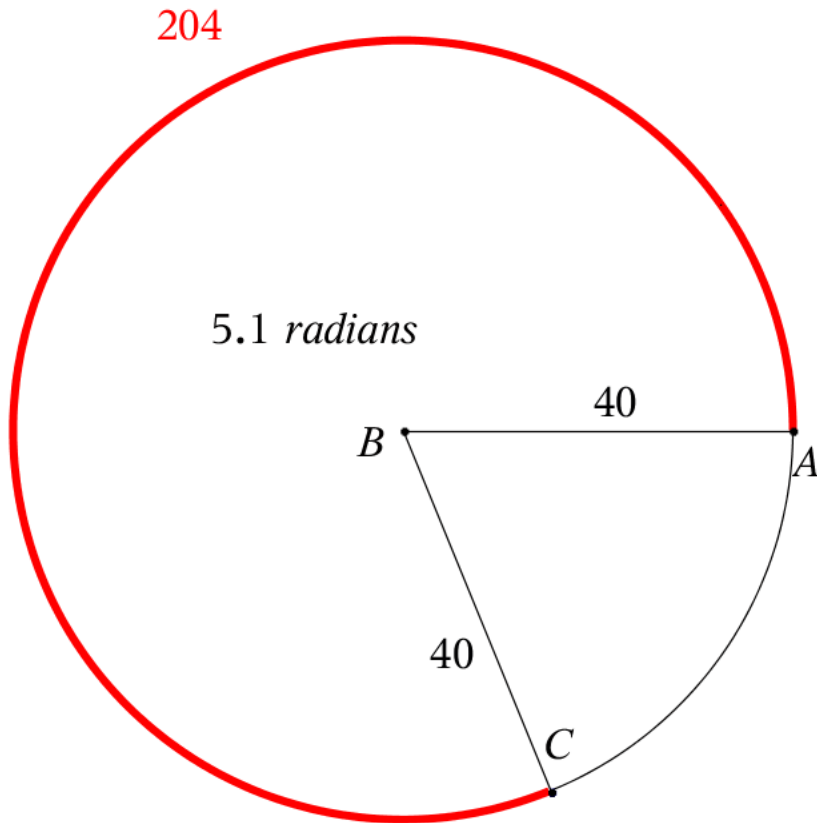
$$25 = 40 \cdot \theta$$

2) Solve equation

$$\frac{25}{40} = \frac{40 \cdot \theta}{\theta}$$

$$\theta = \frac{25}{40} = 0.625 \text{ radians}$$

$$\text{NOTE } \theta = \frac{25}{40} \cdot \frac{180.}{\pi} \approx 35.81^\circ$$



### Scenario 5: Arc Length

Known:  $r = 40$

$$\theta = 5.1 \text{ radians}$$

$$s = \theta \cdot r$$

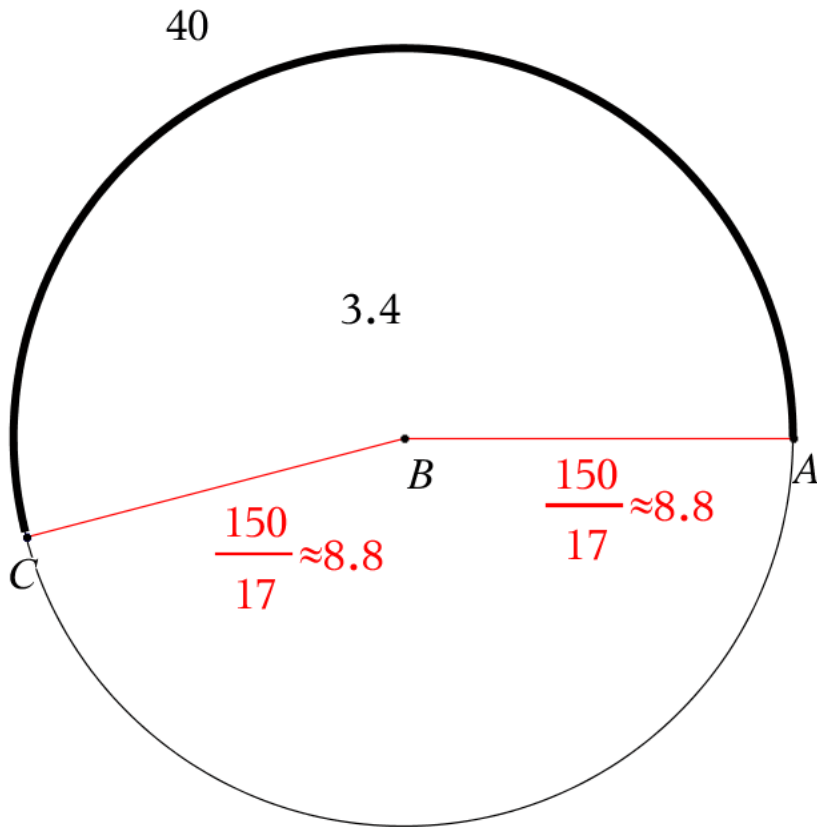
Want  $\theta$

1) Write equation

$$s = 40 \cdot 5.1 = 204$$

$$s = 204$$

NOTE  $\theta = 5.1 \cdot \frac{180}{\pi} \approx 292.2^\circ$



### Scenario 3: Arc Length

Known:  $\theta = 3.4$

$$s = 30$$

$$s = \theta \cdot r$$

Want  $r$

1) Write equation

$$30 = 3.4 \cdot r$$

2) Solve equation

$$\frac{30}{3.4} = \frac{3.4 \cdot r}{3.4}$$

$$r = \frac{30}{3.4} = \frac{150}{17} = 8.824$$

NOTE  $\theta = 3.4 \cdot \frac{180}{\pi} \approx 194.8^\circ$

$122 + \frac{56}{60} + \frac{14}{3600}$	$\frac{221287}{1800}$
$\frac{221287}{1800}$	122.9
1800.	
□	

**DMS to DECIMAL DEGREES**

**KNOW**

1 degree = 60 minutes  
 1 degree = 3600 seconds

1) convert parts to degrees  
 2) add the parts

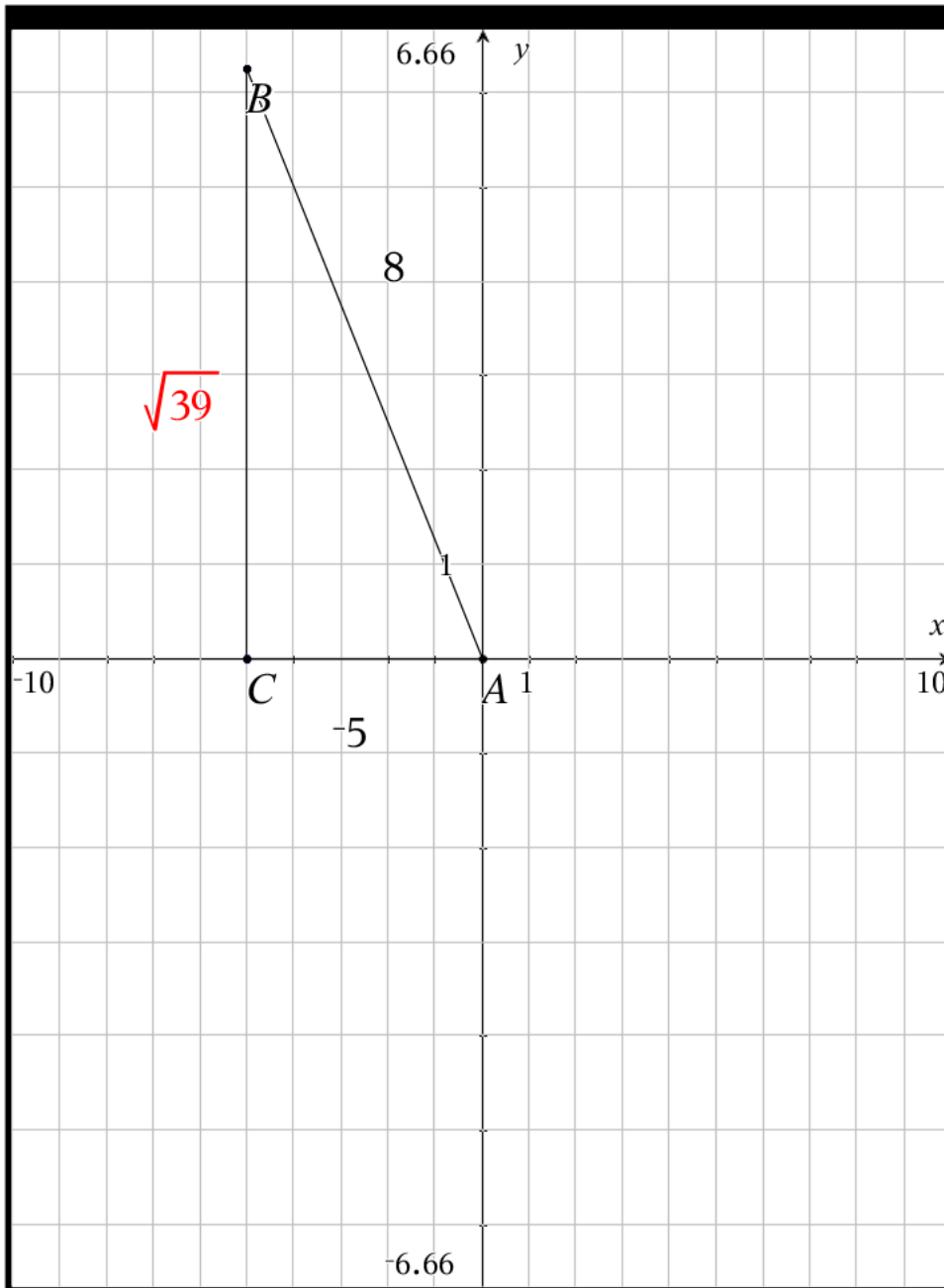
$$122^{\circ}56'14'' = 122 + \frac{56}{60} + \frac{14}{3600}$$

$$122^{\circ}56'14'' = \frac{221287}{1800}$$

$$122^{\circ}56'14'' \approx 122.9^{\circ}$$

<p>(78.549)►DMS <span style="float: right;">78°32'56.4"</span></p> <p>□</p>	<p><b>78.549° to DMS</b></p> <p>Step 1 find the decimal minutes</p> <p>Step 2 convert decimal minutes to seconds</p> <p>Step 3 write DMS</p> <p>Step 1)</p> $0.549^\circ = 0.549 \cdot 60 \blacktriangleright 32.94$ $78.549^\circ \rightarrow 78^\circ 32.94'$ <p>Step 2)</p> $0.94 \cdot 60 \blacktriangleright 56.4$ $78^\circ 32.94' \rightarrow 78^\circ 32' 56.4''$ <p>OR Step 1 FIND the button</p> $(78.549) \blacktriangleright \text{DMS} \blacktriangleright 78^\circ 32' 56.4''$
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$$\sec x = -8/5$$



$$\text{Given } \sec x = \frac{-8}{5} = \frac{8}{-5} \quad \text{and} \quad \frac{\pi}{2} < x < \pi$$

This is a Q2 angle ASTC applies

First we know

HYPOTENUSE IS ALWAYS POSITIVE

$$\sec x = \frac{\text{hyp}}{\text{adj}} = \frac{8}{-5}$$

$$\text{we find } \text{opp} = \pm\sqrt{8^2 - 5^2} = \pm\sqrt{39}$$

( $+\sqrt{39}$  because  $y > 0$  in Q2)

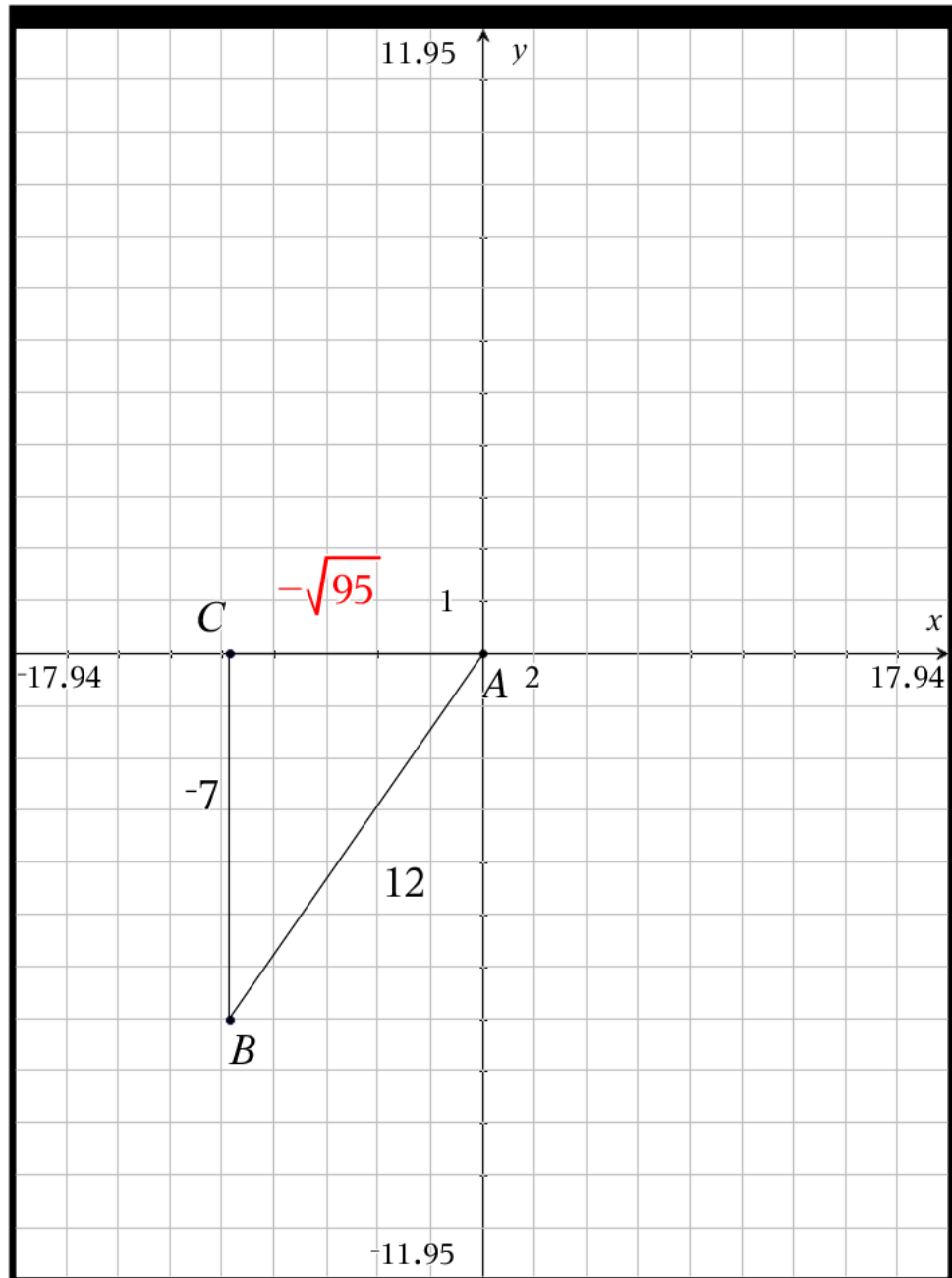
$$\sin x = \frac{\sqrt{39}}{8} \quad \cos x = \frac{-5}{8} \quad \tan x = \frac{\sqrt{39}}{-5}$$

$$\cot x = \frac{-5}{\sqrt{39}} = \frac{-5 \cdot \sqrt{39}}{39}$$

$$\csc x = \frac{8}{\sqrt{39}} = \frac{8 \cdot \sqrt{39}}{39}$$



$$\csc x = -12/7$$



$$\text{Given } \csc x = \frac{-12}{7} = \frac{12}{-7} \quad \text{and} \quad \pi < x < \frac{3\pi}{2}$$

This is a Q3 angle ASTC applies

First we know

HYPOTENUSE IS ALWAYS POSITIVE

$$\csc x = \frac{\text{hyp}}{\text{opp}} = \frac{12}{-7}$$

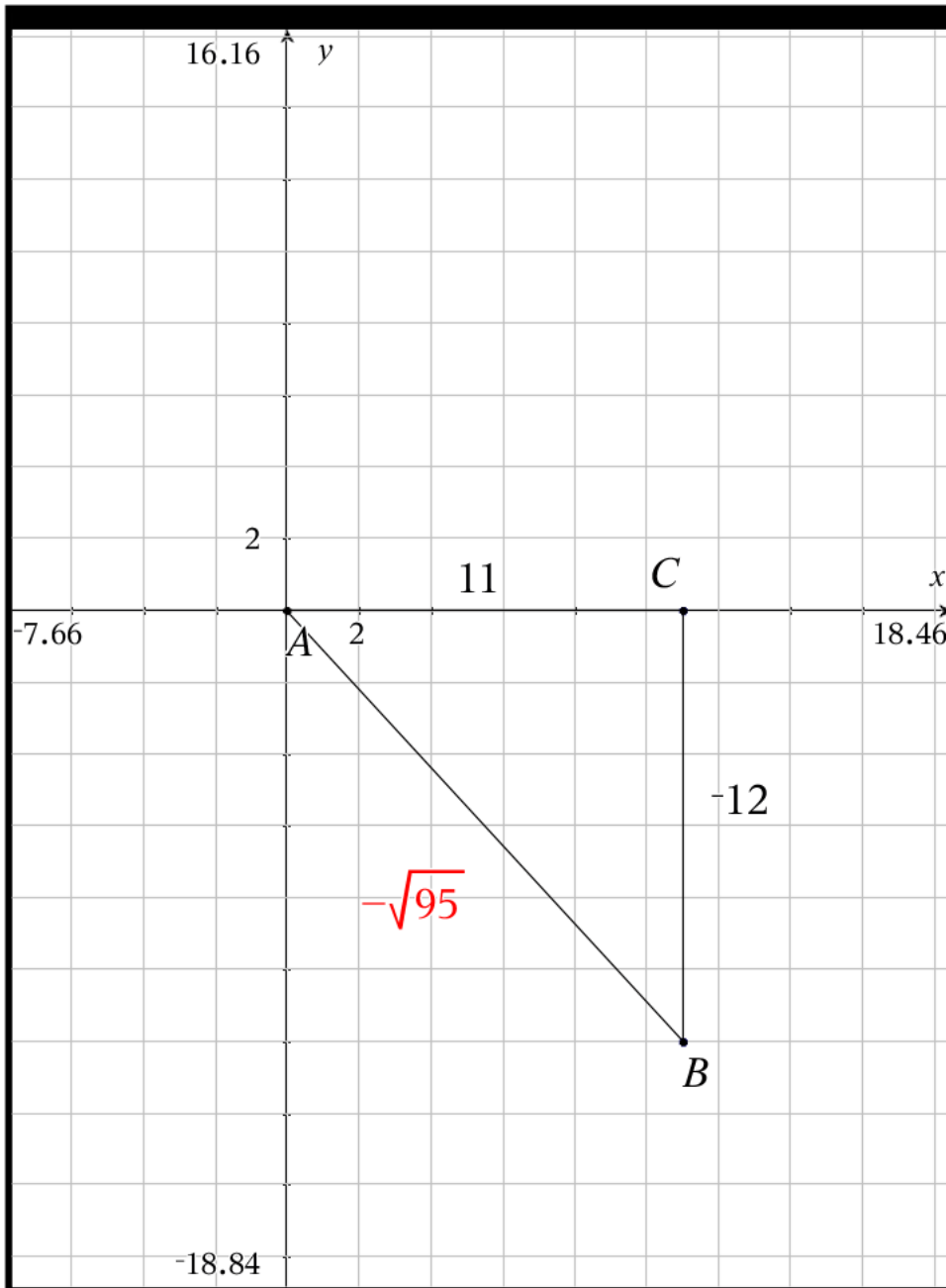
$$\text{we find } \text{adj} = \pm \sqrt{12^2 - 7^2} = -\sqrt{95}$$

( $-\sqrt{95}$  because  $y < 0$  in Q3)

$$\sin x = \frac{-7}{12} \quad \cos x = \frac{-\sqrt{95}}{12} \quad \tan x = \frac{-7}{-\sqrt{95}} = \frac{7 \cdot \sqrt{95}}{95}$$

$$\cot x = \frac{-\sqrt{95}}{-7} = \frac{\sqrt{95}}{7} \quad \sec x = \frac{12}{-\sqrt{95}} = \frac{-12 \cdot \sqrt{95}}{95}$$

$$\cot x = -11/12$$



Given  $\cot x = \frac{-11}{12} = \frac{11}{-12}$  and  $\frac{3\pi}{2} < x < 2\pi$

This is a Q4 angle ASTC applies

First we know

HYPOTENUSE IS ALWAYS POSITIVE

$$\csc x = \frac{\text{hyp}}{\text{opp}} = \frac{12}{-7}$$

we find  $\text{hyp} = \sqrt{12^2 + 11^2} = \sqrt{265}$

( $\sqrt{265}$  because  $\text{hyp} > 0$ )

$$\sin x = \frac{-12}{\sqrt{265}} = \frac{-12 \cdot \sqrt{265}}{265}$$

$$\cos x = \frac{11}{\sqrt{265}} \rightarrow \frac{11 \cdot \sqrt{265}}{265} \quad \tan x = \frac{-12}{11}$$

$$\csc x = \frac{-\sqrt{265}}{12} \quad \sec x = \frac{\sqrt{265}}{11}$$