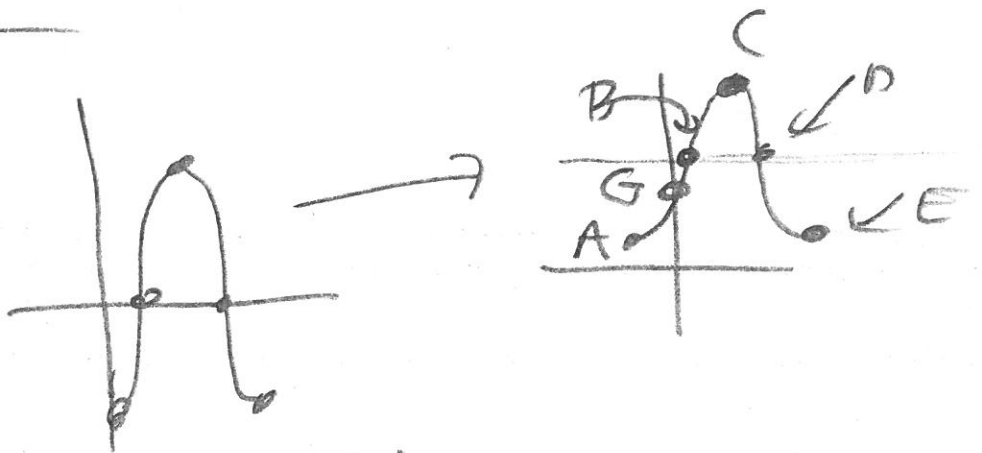


Problem 1 cont

So since



G = give starting height

$(0, f(G))$ = starting height

time from G to C is 3 seconds

time from A to E is 8 seconds

time from A to C is 4 seconds

so time from A to G is 1 second

this means $y = a \sin\left(\frac{2\pi}{\text{period}}(x+1)\right) + b$

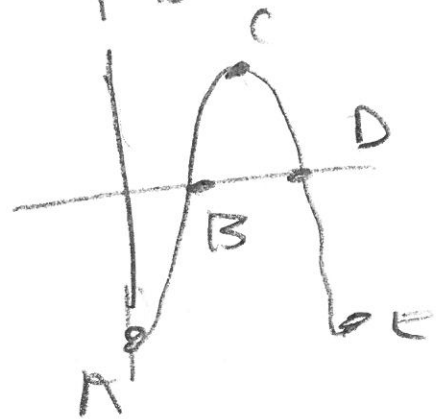
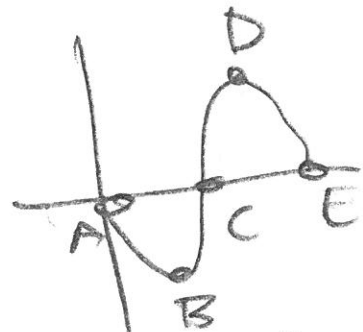
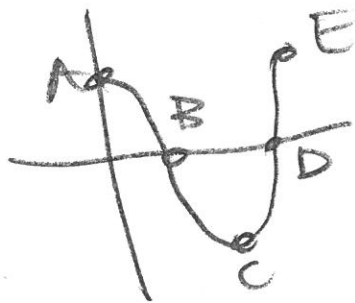
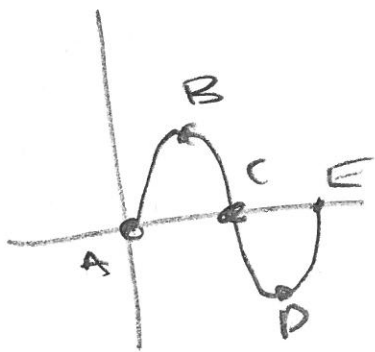
this is THE hardest part of this model

PROBLEM 1

Start with time

Time fact ① = 1 revolution = 8 sec
(this is period)

What does time fact ① tell us



If A = start
= 0

B = $\frac{1}{4}$ ride = 2 sec

C = $\frac{2}{4}$ ride = 4 sec

D = $\frac{3}{4}$ ride = 6 sec

E = $\frac{4}{4}$ ride = 8 sec

Problem 1 cont

Time Fact 2

it took 3 seconds

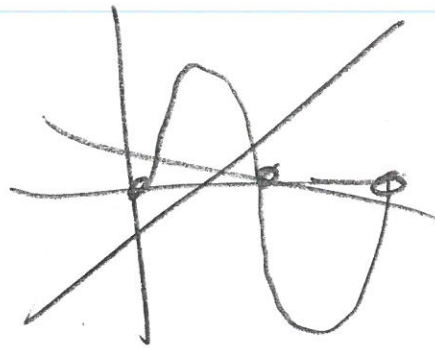
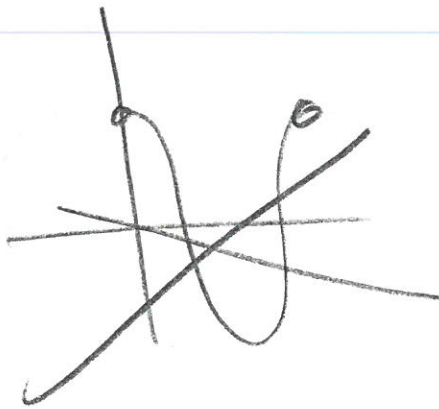
to reach maximum,

Timefact 2

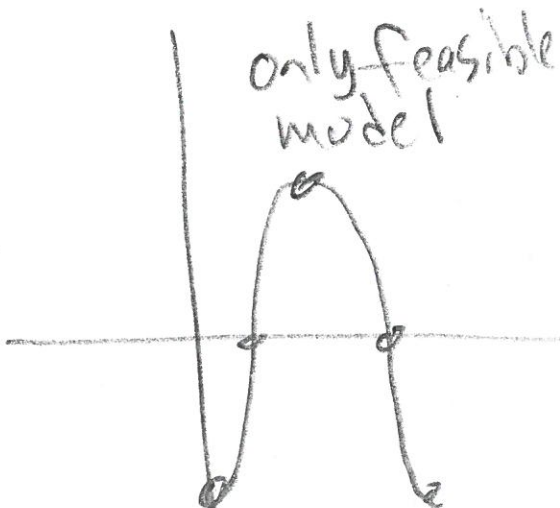
implies we start BELOW
max $\rightarrow a < 0$

also we start somewhere
other than pts A, B, C, D
or E

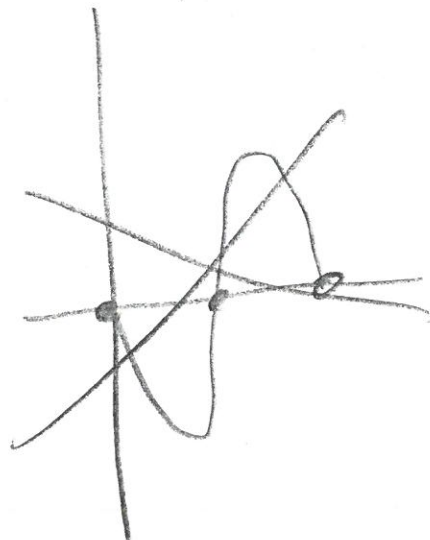
so



eliminate three possible models



or



Problem 1 cont

Wheel fact 1

diameter = 40 ft
implies $r = 20$ ft

Note in Ferris wheel model

$$y = a + \text{trig} \left(\frac{2\pi}{\text{period}} (x \pm \text{phase}) \right) + d$$

↓
 $a = \pm \text{radius}$

So we now know

$$y = -20 \cos \left(\frac{2\pi}{\text{period}} (x + 1) \right) + d$$

but we know period = 8 sec

$$\text{So } y = -20 \cos \left(\frac{2\pi}{8} (x + 1) \right) + d$$

So finally Problem 1

Model General Mode

$$h(x) = a + r \cdot \sin\left(\frac{2\pi}{\text{period}}(x \pm \text{phase})\right) + d$$

a depends on mode of travel

$$a = \pm \text{radius}$$

period = length of ride

phase depends on where rider starts

$$d = \text{radius} + \text{platform height}$$

$$\begin{aligned} \text{platform height} &= \text{Max-diameter} \\ &= \text{midline} - \text{radius} \end{aligned}$$

Problem 1 cont

Our model

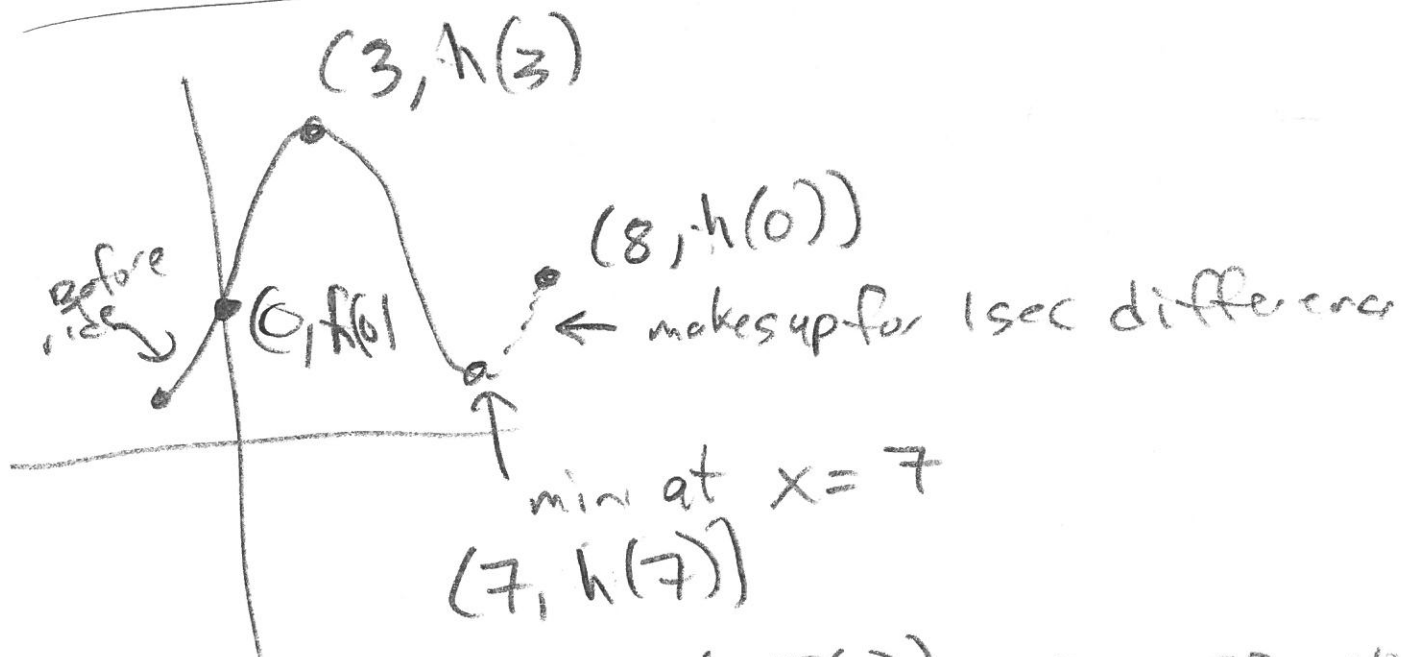
$$h(x) = -20 \cos\left(\frac{2\pi}{8}(x+1)\right) + 23$$

↙
- radius

↙
length
of
ride

↙
tough
but
3 sec to
top
told us

Max - radius
radius + platform
↓



test $h(0) = -20 \cos\left(\frac{2\pi}{8}(1)\right) + 23 = 23 - 10\sqrt{2} \approx 8.$

$$h(3) = -20 \cos\left(\frac{2\pi}{8}(4)\right) + 23 = 43$$

$$h(7) = -20 \cos\left(\frac{2\pi}{8}(8)\right) + 23 = 3$$

Problem 1 Now lets answer

Paul's Questions

1A) done

1B) we did not "officially" do

$$\text{MAX-diameter} = \text{platform height}$$
$$43 - 40 = 3 = \text{platform height}$$

1C) Done $h(x) = -20 \cos\left(\frac{2\pi}{8}(x+1)\right) + 23$
(easiest to see) \rightarrow

$$\begin{aligned} 1D) \quad h(6) &= -20 \cos\left(\frac{2\pi}{8}(6+1)\right) + 23 \\ &= -20 \cos\left(\frac{14\pi}{8}\right) + 23 \\ &= -20 \cos\left(\frac{7\pi}{4}\right) + 23 \\ &= -20\left(\frac{\sqrt{2}}{2}\right) + 23 = 23 - 10\sqrt{2} \\ &\approx 8.58 \text{ ft} \end{aligned}$$

(15)

$$h\left(\frac{13}{3}\right) = -20 \cos\left(\frac{2\pi}{8}\left(\frac{13}{3}+1\right)\right) + 23$$

$$= -20 \cos\left(\frac{2\pi}{8} \cdot \frac{16}{3}\right) + 23$$

$$= -20 \cos\left(\frac{32\pi}{24}\right) + 23$$

$$= -20 \cos\left(\frac{4\pi}{3}\right) + 23$$

$$= -20\left(-\frac{1}{2}\right) + 23$$

$$= 33$$

$$h(0) = -20 \cos\left(\frac{2\pi}{8}(0+1)\right) + 23$$

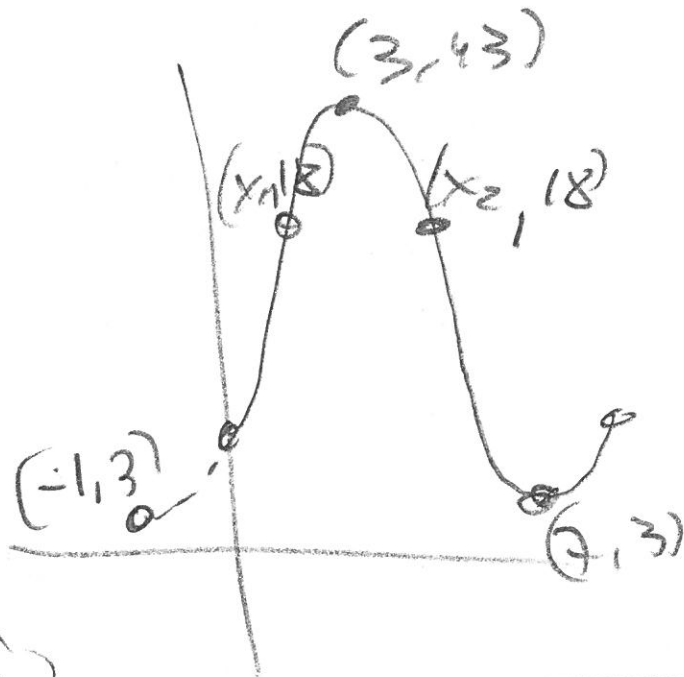
$$= -20 \cos\left(\frac{2\pi}{8}\right) + 23$$

$$= -20\left(\frac{\sqrt{2}}{2}\right) + 23$$

$$= -10\sqrt{2} + 23$$

$$\approx 8.858$$

Problem 1



1c

$$h(x) = 18 \text{ for 2nd time}$$

Easy with calculator (graphing)

$$\text{Set } 18 = h(x)$$

$$18 = -20 \cos\left(\frac{2\pi}{8}(x+1)\right) + 23$$

take $x_2 > 3$ solution

$$x \approx 5.32$$

(1E) without calculator.

$$18 = -20 \cos\left(\frac{2\pi}{8}(x+1)\right) + 23$$

$$18 - 23 = -20 \cos\left(\frac{2\pi}{8}(x+1)\right)$$

$$-5 = -20 \cos\left(\frac{2\pi}{8}(x+1)\right)$$

$$\frac{-5}{-20} = \cos\left(\frac{2\pi}{8}(x+1)\right)$$

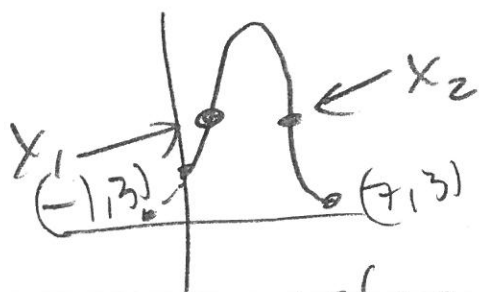
$$\frac{1}{4} = \cos\left(\frac{2\pi}{8}(x+1)\right)$$

$$\cos^{-1}\left(\frac{1}{4}\right) = \frac{2\pi}{8}(x+1)$$

$$\frac{8}{2\pi} \left(\cos^{-1}\left(\frac{1}{4}\right)\right) = x+1$$

$$x_1 = -1 + \frac{8}{2\pi} \cos^{-1}\left(\frac{1}{4}\right)$$

$$\approx 0.678$$

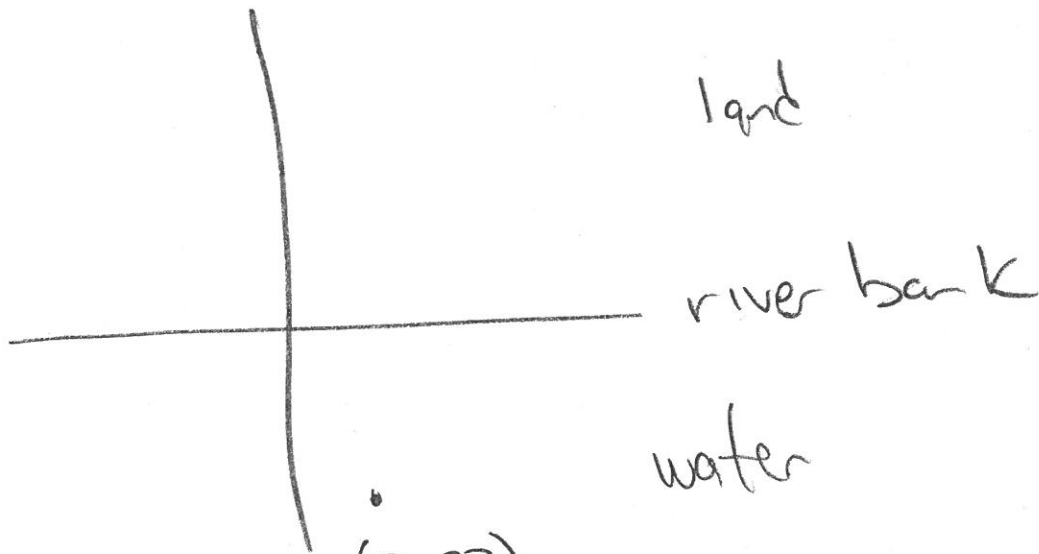


$$x_2 = 7 - \frac{8}{2\pi} \cos^{-1}\left(\frac{1}{4}\right)$$
$$\approx 5.322$$

referencing is awesome!

Problem 8

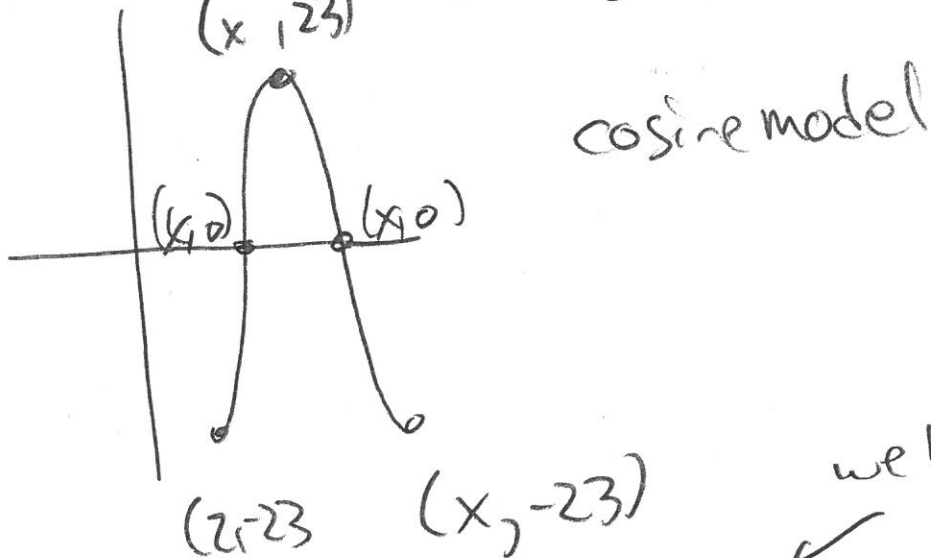
Tarzan Problem



$(z, -23)$
↓
time

↓
distance away from river bank

$(x, 23)$ max away from river bank

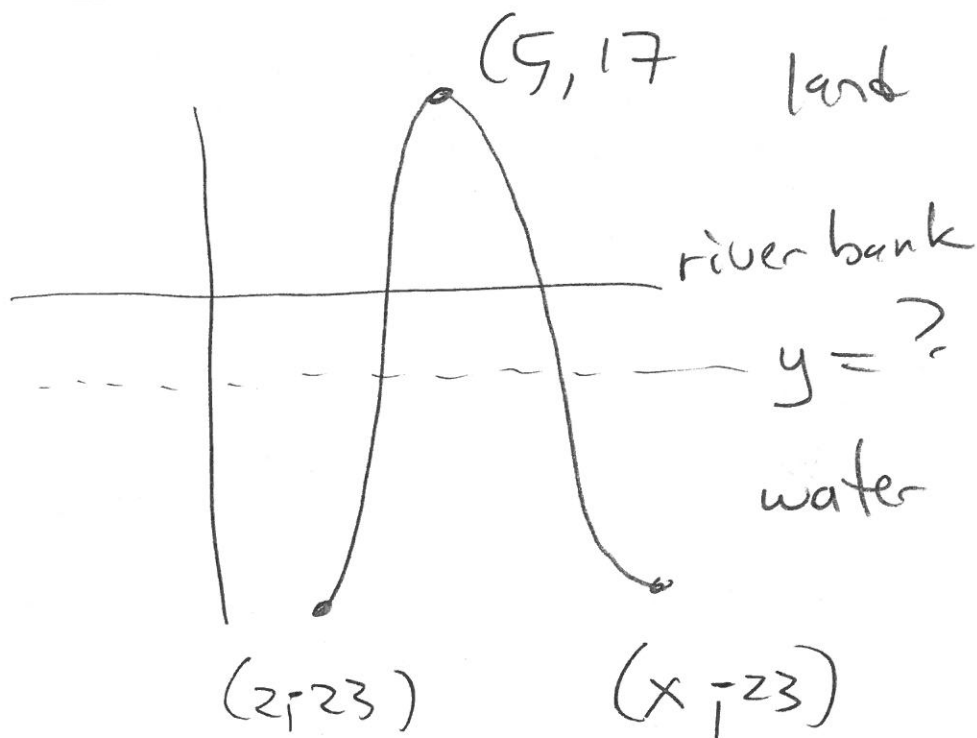


we know

$$y = a \cos\left(\frac{2\pi}{\text{period}}(x - z)\right) + d$$

with $a < 0$

Problem 2 Tarzan Problem



$$|\text{max}_{\text{water}}| \text{ to } |\text{max}_{\text{land}}| = |-23| + |17| = 40$$

$$\text{So range} = 40 \quad \frac{1}{2} \text{ range} = \text{amplitude} = \boxed{20}$$

$$\text{So } y = -20 \cos\left(\frac{2\pi}{\text{period}}(x - 2)\right) + d$$

reflected cosine

can find now

shifts right

can find now

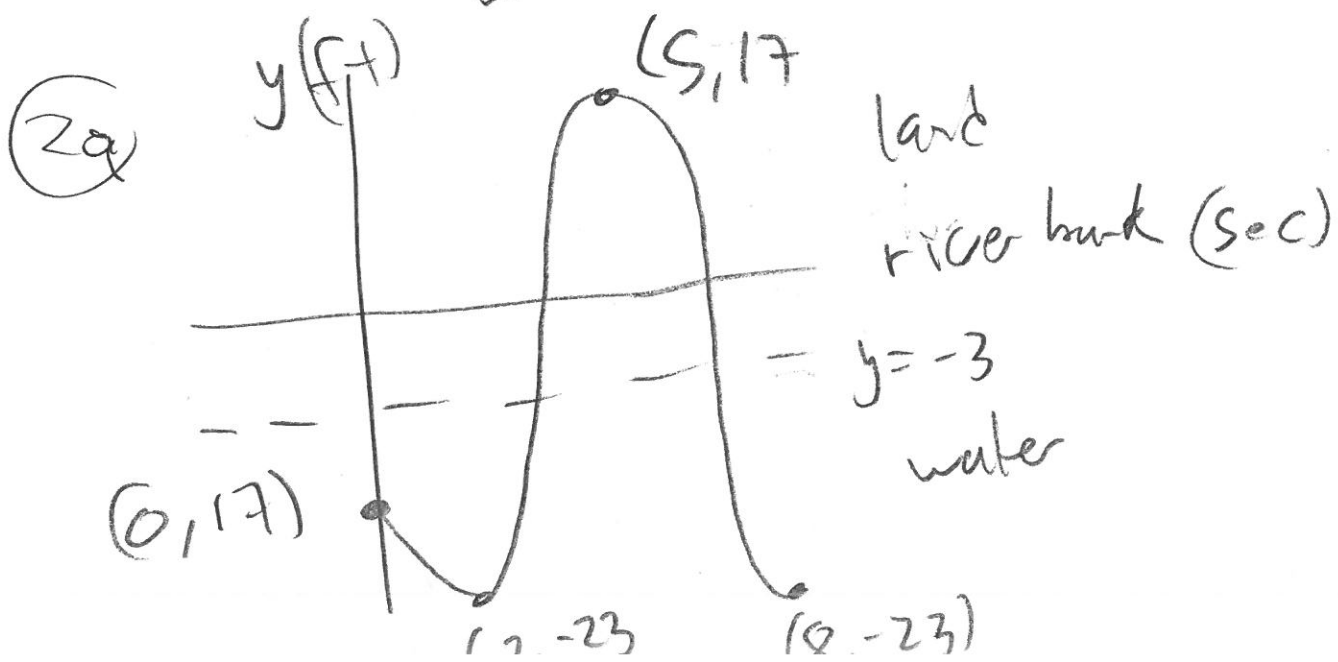
Problem 2

$\frac{1}{2}$ tide is from 2 to 5 or 3 sec
period = whole tide = $2(3) = 6$ Sec.

$$\text{So } y = -20 \cos\left(\frac{2\pi}{6}(x-2)\right) + d$$

$$d = \frac{1}{2}(-23 + 17) = \frac{1}{2}(-6) = -3$$

$$\text{So model } \boxed{y = -20 \cos\left(\frac{2\pi}{6}(x-2)\right) - 3}$$

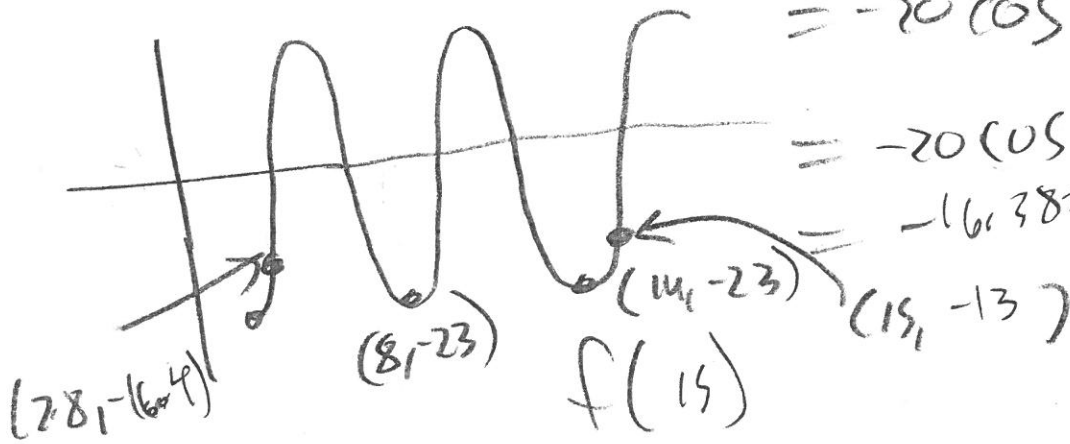


Problem (2b) $f(x) = -20 \cos\left(\frac{2\pi}{6}(x-2)\right) - 3$

Problem (2d) $f(0) = -20 \cos\left(\frac{2\pi}{6}(0-2)\right) - 3$
 $= -20 \cos\left(-\frac{4\pi}{6}\right) - 3$
 $= -20 \cos\left(-\frac{2\pi}{3}\right) - 3$
 $= 17$

Jane is 17 ft over water when she starts stopwatch

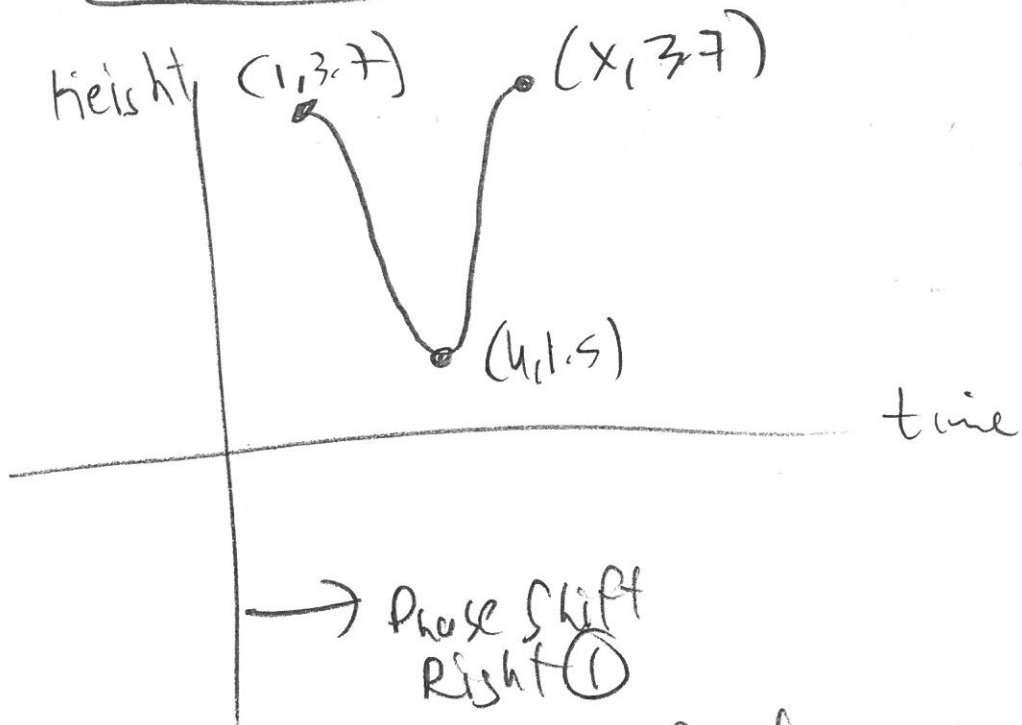
Problem (2c) $f(2.8) = -20 \cos\left(\frac{2\pi}{6}(2.8-2)\right) - 3$
 $= -20 \cos\left(\frac{1.6\pi}{6}\right) - 3$



$= -20 \cos\left(\frac{16}{60}\pi\right) - 3$
 $= -16.383$

$f(15) = -20 \cos\left(\frac{2\pi}{6}(15-2)\right) - 3$
 $= -20 \cos\left(\frac{26\pi}{6}\right) - 3 = -13$

Problem 3 Oil well



This is phase shifted cosine model

$$\text{max} - \text{min} = \text{range} = 3.7 - 1.5 = 2.2$$

$$\frac{1}{2} \text{range} = \text{amplitude} = \frac{1}{2} (2.2) = 1.1$$

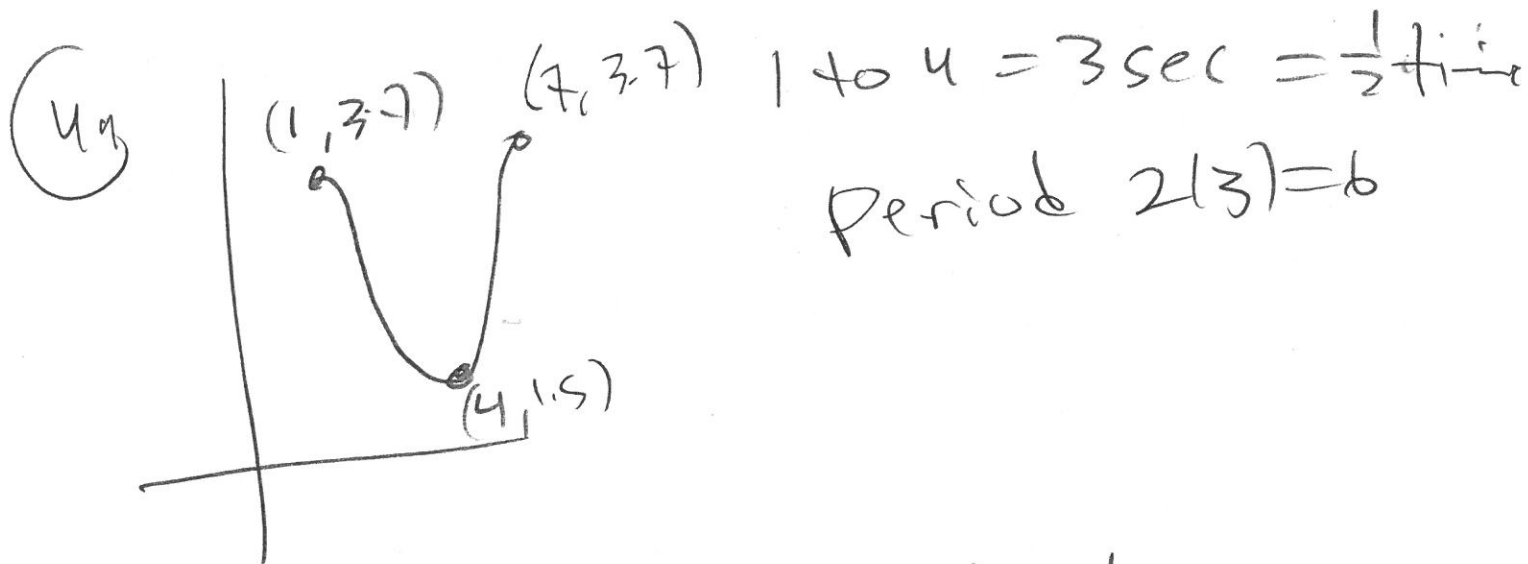
$$y = 1.1 \cos\left(\frac{2\pi}{\text{period}}(x - 1)\right) + d$$

↓ we can find now

↓ Phase Shift R

↓ $\frac{\text{max} + \text{min}}{2}$

Problem 4 cont



$$y = 1.1 \cos\left(\frac{2\pi}{6}(x-1)\right) + d$$

$$d = \frac{\text{max} + \text{min}}{2} = \frac{3.7 + 1.5}{2} = \frac{5.2}{2}$$

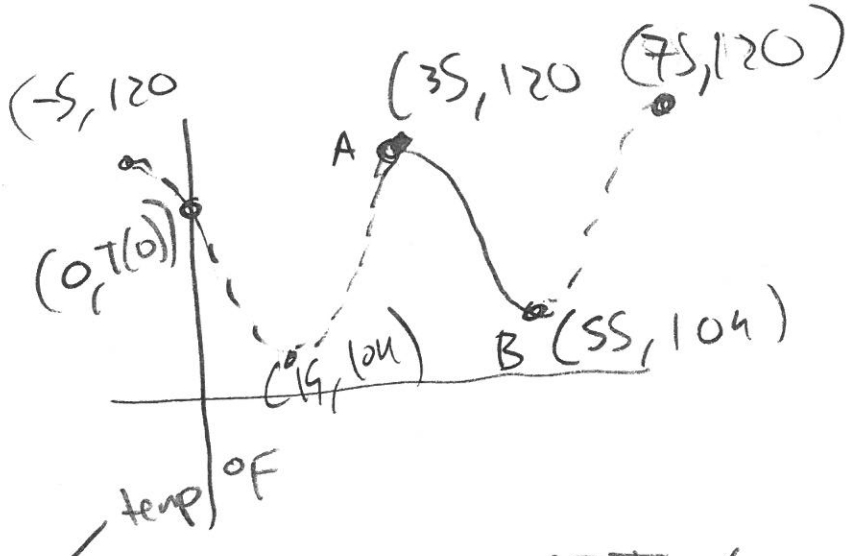
$$= 2.6$$

(4b) Model

$$y = 1.1 \cos\left(\frac{2\pi}{6}(x-1)\right) + 2.6$$

E.T. Being Problem

(4) high temp = 120 ← after 35 min
 low temp = 104 ← after 55 min
 20+35



$$T(x) = a \operatorname{trig} \left(\frac{2\pi}{\text{period}} (x - \text{shift}) \right) + d$$

↳ time min

↙ implied

A = (35, 120)
 (x, T(x))
 |
 (time, temp)

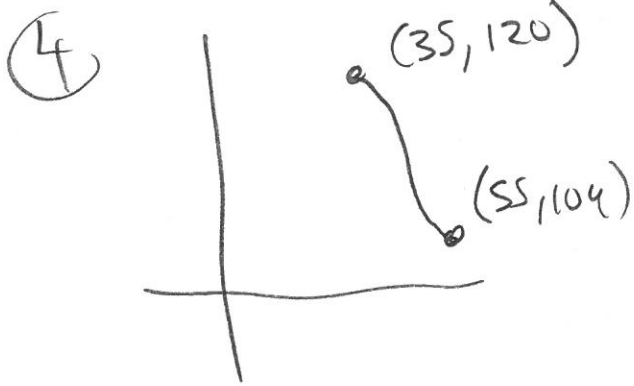
given 35 + 20 = 55

(B) (55, 104)
 ↳ given

120 max temp

104 min temp

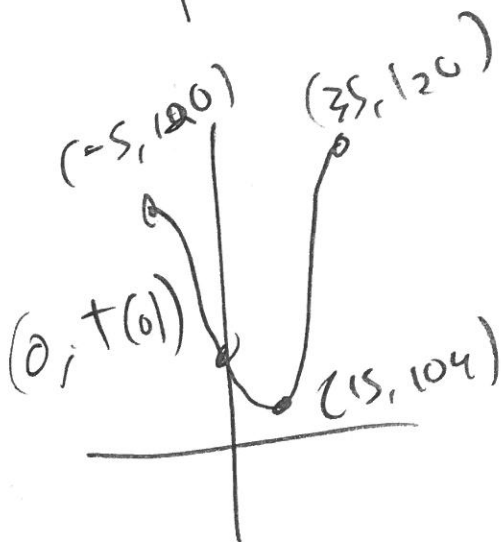
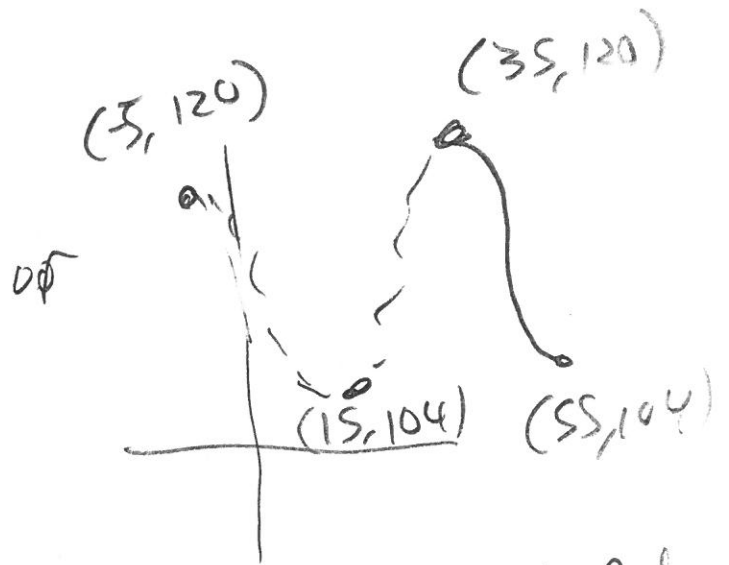
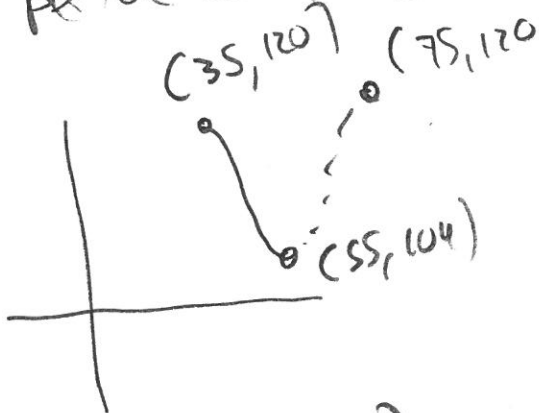
ET Being Cont



this is the given (implied given)

$\frac{1}{2}$ period = 20 min

period = 40 min



← This is more helpful in writing model

PHASE = -5 5 left

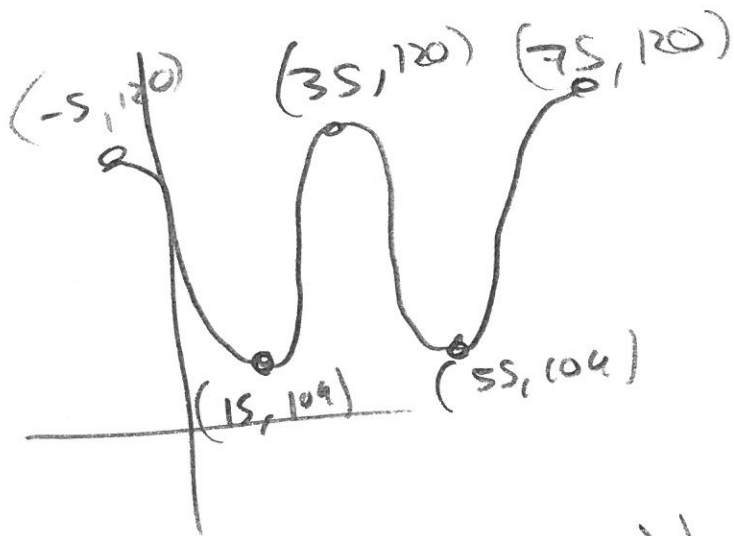
$$y = a + b \sin\left(\frac{2\pi}{\text{period}}(x + 5)\right) + d$$

Period = 40

$$y = a + b \sin\left(\frac{2\pi}{40}(x + 5)\right) + d$$

for any x, y →

④ ET being cool



$$y = a \operatorname{trig} \left(\frac{2\pi}{40}(x+s) \right) + d$$

↓

cosine
model
 $a > 0$

$$y = a \cos \left(\frac{2\pi}{40}(x+s) \right) + d$$

min 104°F
max 120°F

$$\begin{aligned} d &= \text{midline} \\ &= \frac{1}{2}(120 + 104) \\ &= \frac{1}{2}(224) \end{aligned}$$

$$\boxed{d = 112}$$

$$\begin{aligned} \text{Range} &= 120 - 104 \\ &= 16 \end{aligned}$$

$$\frac{1}{2} \text{Range} = 8$$

$$\begin{aligned} \text{so } a &= 8 \leftarrow \text{not reflected} \\ a &= -8 \end{aligned}$$

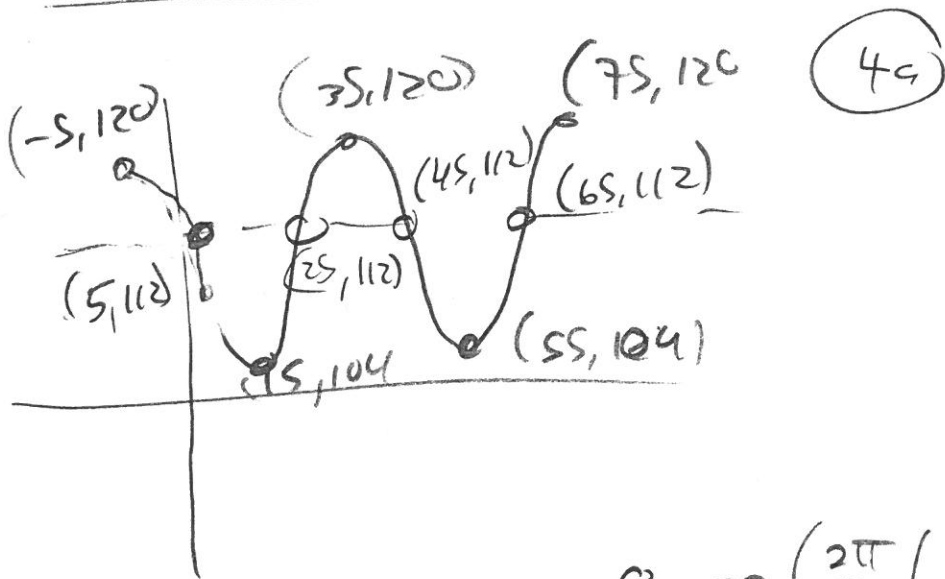
ET Beig cont

$$y = 9 \cos\left(\frac{2\pi}{40}(x+s)\right) + 112$$

temp in $^{\circ}\text{F}$

$$|T(x) = 8 \cos\left(\frac{2\pi}{40}(x+s)\right) + 112 \quad x = \text{time in min}$$

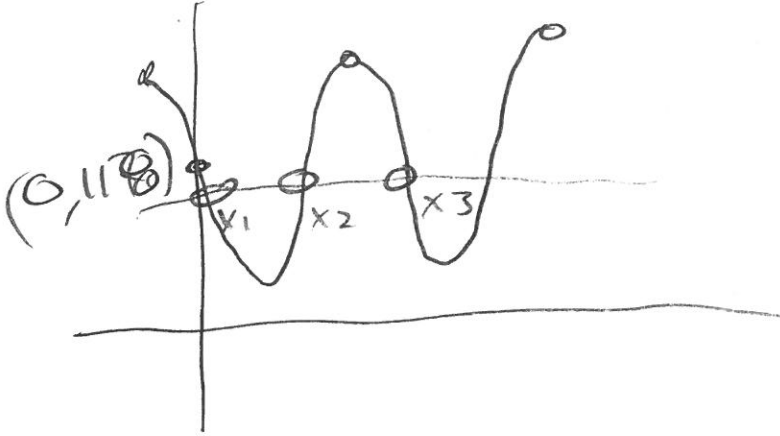
4b



$$\begin{aligned} \textcircled{4c} \text{ what is } T(0) &= 8 \cos\left(\frac{2\pi}{40}(s)\right) + 112 \\ &= 8 \cos\left(\frac{10\pi}{40}\right) + 112 \\ &= 8 \cos\left(\frac{\pi}{4}\right) + 112 \\ &= 8 \frac{\sqrt{2}}{2} + 112 \\ &= 4\sqrt{2} + 112 \\ &\approx 117.657^{\circ}\text{F} \end{aligned}$$

Et Being cont

$$T(x) = 8 \cos\left(\frac{2\pi}{40}(x+5)\right) + 112$$



x_1, x_2, x_3 times such that

$$T(x_1) = T(x_2) = T(x_3) = 114$$

$$114 = 8 \cos\left(\frac{2\pi}{40}(x+5)\right) + 112$$

$$2 = 8 \cos\left(\frac{2\pi}{40}(x+5)\right)$$

$$\frac{2}{8} = \cos\left(\frac{2\pi}{40}(x+5)\right)$$

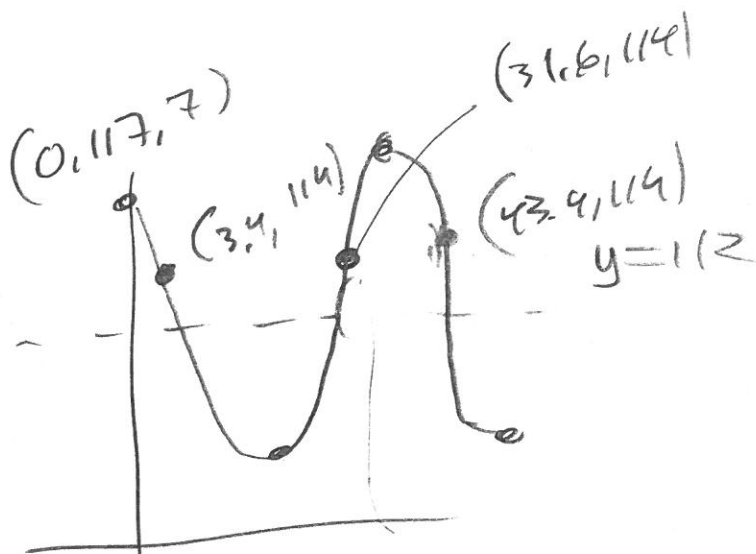
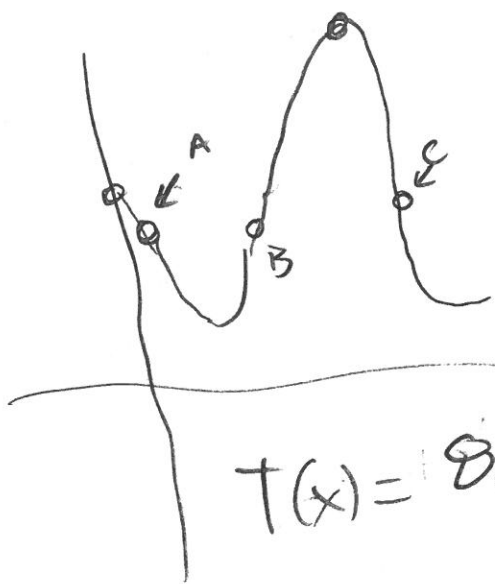
$$\cos^{-1}\left(\frac{2}{8}\right) = \frac{2\pi}{40}(x+5)$$

$$x+5 = \frac{40}{2\pi} \left(\cos^{-1}\left(\frac{1}{4}\right)\right)$$

$$x = -5 + \frac{40}{2\pi} \cos^{-1}\left(\frac{1}{4}\right)$$

$$\approx 3.391 \text{ minutes} = x_1$$

ET berg cont



$$T(x) = 8 \cos\left(\frac{2\pi}{40}(x+5)\right) + 112 \quad (4d) \nearrow$$

$$A_x = -5 + \frac{40}{2\pi} \left(\cos^{-1}\left(\frac{1}{4}\right)\right) \approx 3.391$$

$$A_y = 114$$

$$C_x = A_x + 40 = 35 + \frac{40}{2\pi} \cos^{-1}\left(\frac{1}{4}\right) \approx 43.391$$

$$C_y = 114$$

$$B_x = 35 - \frac{40}{2\pi} \cos^{-1}\left(\frac{1}{4}\right) \approx 31.619^\circ$$

$$B_y = 114 \quad (4d) \quad \boxed{x = 3.391, 43.391, 31.619}$$

All

$$x_1 = -5 + \frac{40}{2\pi} \cos^{-1}\left(\frac{1}{4}\right) + 40n \quad n \in \mathbb{Z}$$

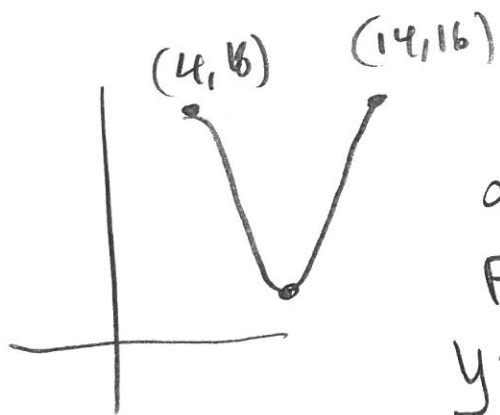
$$x_2 = 35 - \frac{40}{2\pi} \cos^{-1}\left(\frac{1}{4}\right) + 40n \quad n \in \mathbb{Z}$$

STEAM BOAT Problem

(5) $x = 4 \xrightarrow{\text{sec}}$ 16 ft \rightarrow max height

$x = 4 + 10 \rightarrow$ period 10 sec

$= 14 \text{ sec} \rightarrow$ 16 again



$$y = a \cos\left(\frac{2\pi}{\text{period}}(x - \text{shift})\right) + d$$

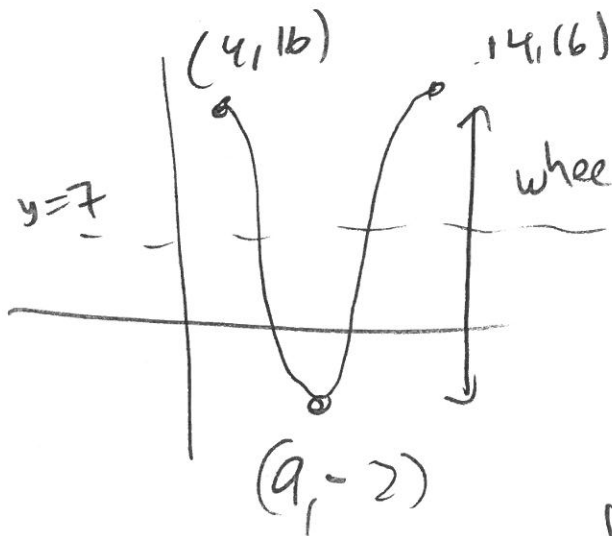
$a > 0$ (starts at max)

period = 10 sec

$$y = a \cos\left(\frac{2\pi}{10}(x - \text{shift})\right) + d$$

at x max at 4 & 14 sec

implies (-6, max) true / not feasible
but true



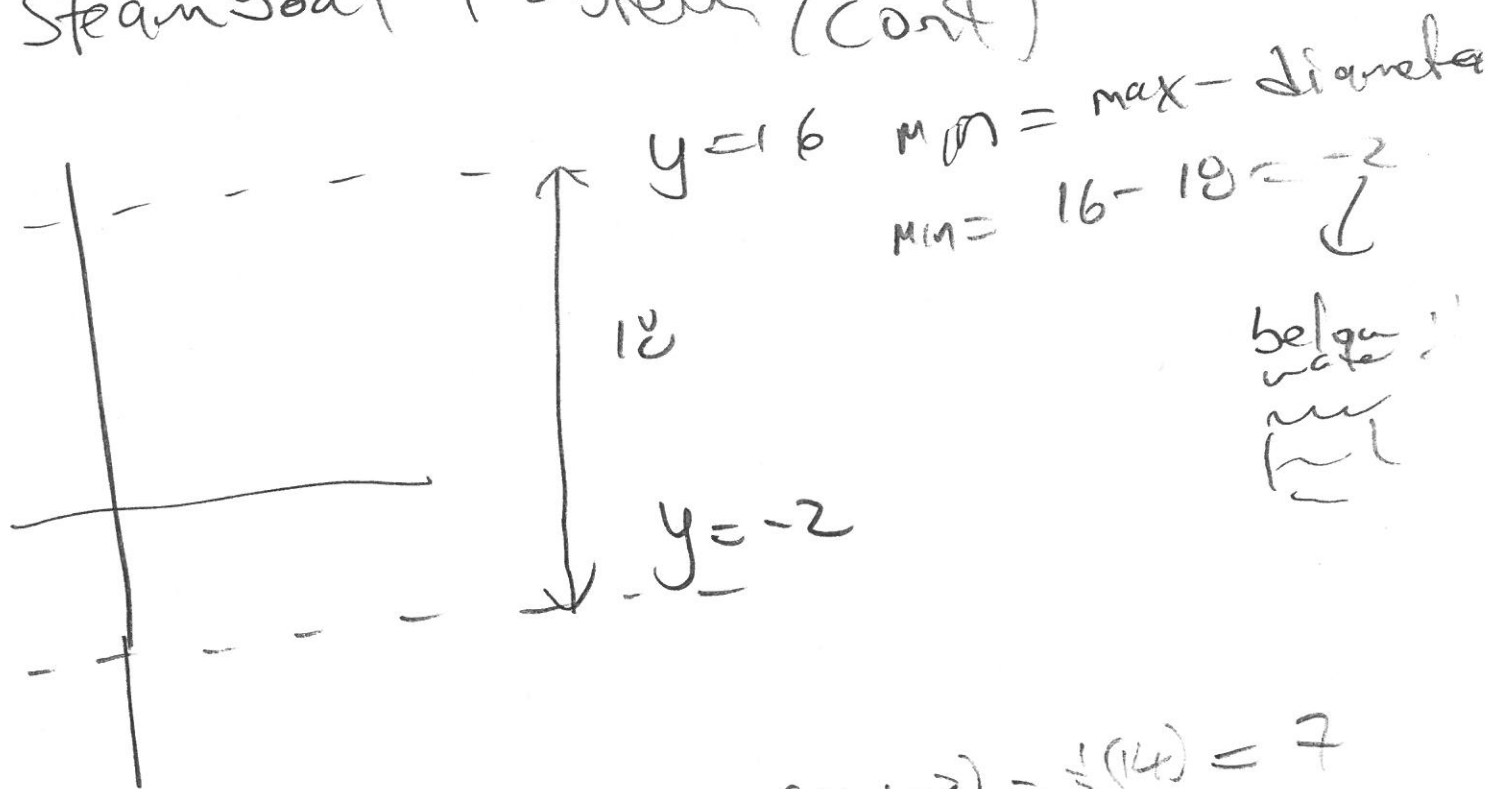
wheel = 18 ft diameter

$r = 9 \text{ ft}$

$a = 9$

$$y = 9 \cos\left(\frac{2\pi}{10}(x - \text{shift})\right) + d$$

Steamboat Problem (cont)

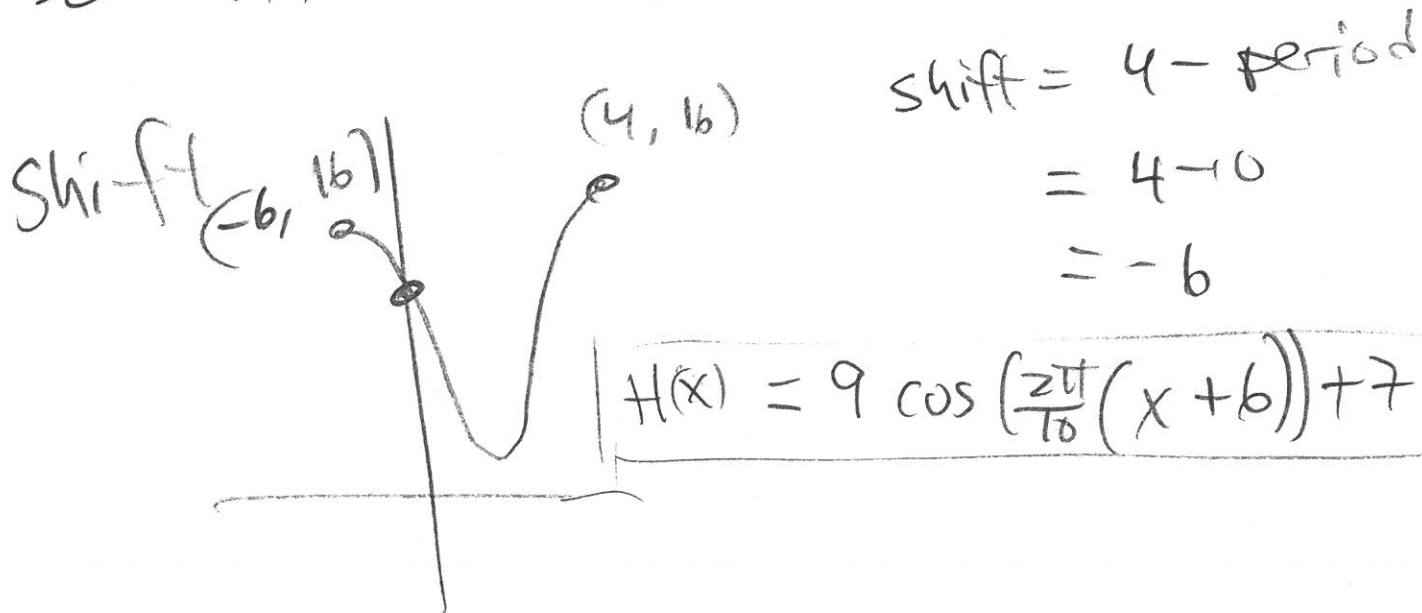


$$d = \frac{1}{2}(\max + \min) = \frac{1}{2}(16 + (-2)) = \frac{1}{2}(14) = 7$$

$$= \max - \text{amp} = 16 - 9 = 7$$

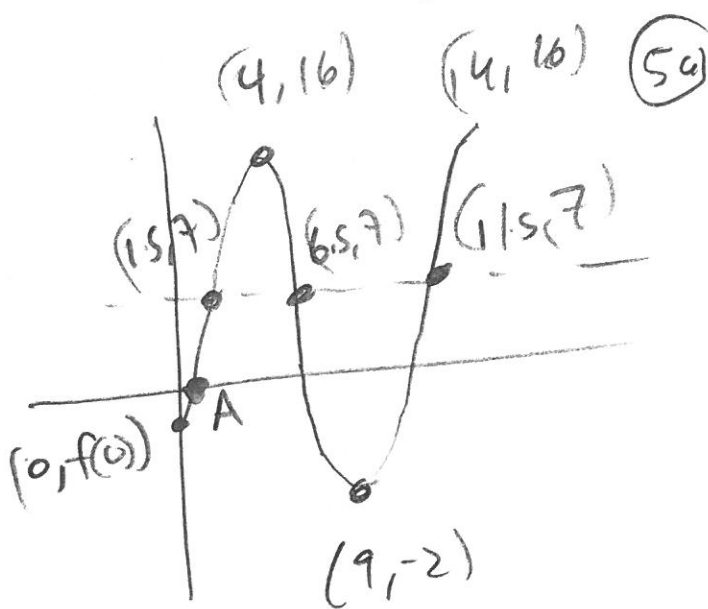
$$= \min + \text{amp} = -2 + 9 = 7$$

So $H(x) = 9 \cos\left(\frac{2\pi}{10}(x - \text{shift})\right) + 7$



$$H(x) = 9 \cos\left(\frac{2\pi}{10}(x + 6)\right) + 7$$

Steam boat Problem



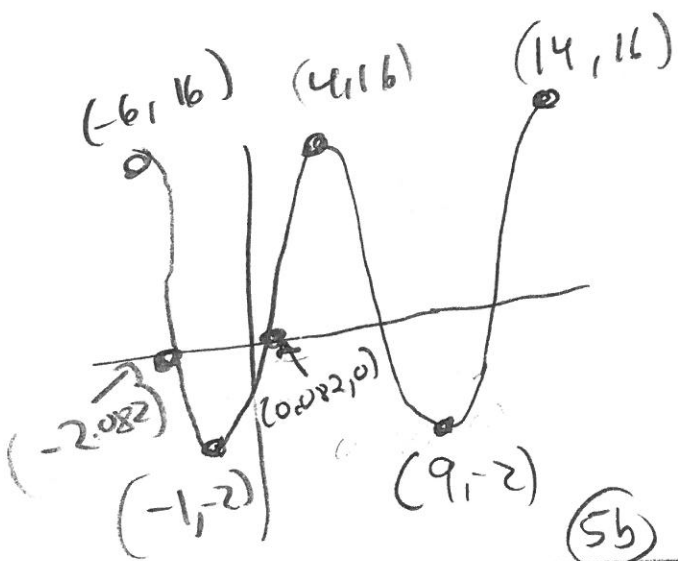
5a

$$h(5) = 9 \cos\left(\frac{2\pi}{10}(11)\right) + 7$$

$$\approx 14.281$$

$$h(17) = 9 \cos\left(\frac{2\pi}{10}(23)\right) + 7$$

$$\approx 4.219$$



5b

$$0 = 9 \cos\left(\frac{2\pi}{10}(x+6)\right) + 7$$

$$-7 = 9 \cos\left(\frac{2\pi}{10}(x+6)\right)$$

$$-\frac{7}{9} = \cos\left(\frac{2\pi}{10}(x+6)\right)$$

$$\cos^{-1}\left(-\frac{7}{9}\right) = \frac{2\pi}{10}(x+6)$$

$$x+6 = \frac{10}{2\pi} \cos^{-1}\left(-\frac{7}{9}\right)$$

$$x = -6 + \frac{10}{2\pi} \cos^{-1}\left(-\frac{7}{9}\right)$$

$$x \approx -2.082$$

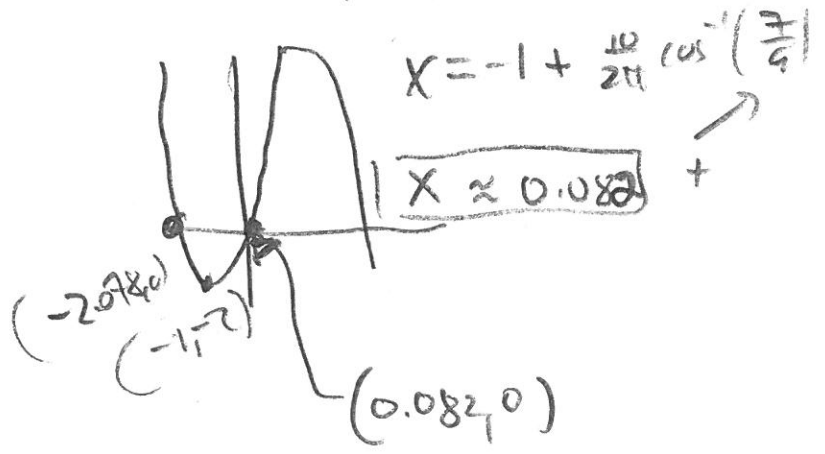
$$h(x) = 9 \cos\left(\frac{2\pi}{10}(x+6)\right) + 7$$

5b

$$x = -1 + \frac{10}{2\pi} \cos^{-1}\left(\frac{7}{9}\right)$$

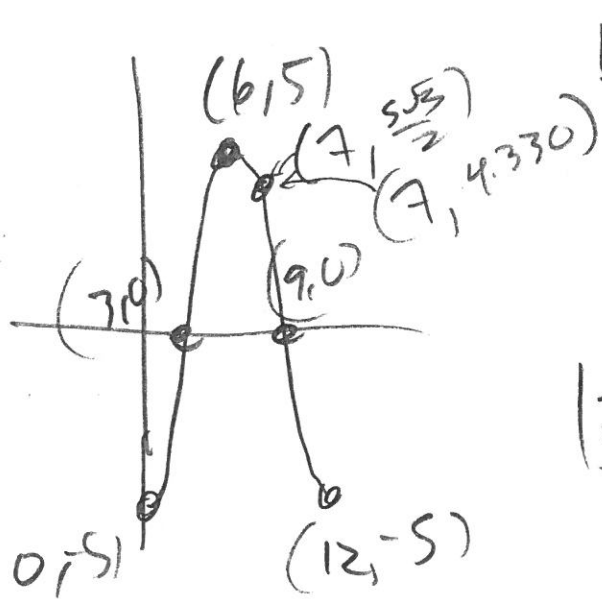
$$x = 0.082$$

On way out of water



Boat Problem (6)

$$y = -5 \cos\left(\frac{\pi}{6}x\right) \rightarrow y = -5 \cos\left(\frac{2\pi}{12}x\right)$$



$$b = \frac{\pi}{6}$$

$$PL = \frac{2\pi}{\frac{\pi}{6}} = \frac{2\pi}{1} \cdot \frac{6}{\pi} = \frac{12\pi}{\pi}$$

$$\boxed{PL = 12}$$

$$\textcircled{6a} \quad y(0) = -5 \cos\left(\frac{\pi}{6}(0)\right) = -5(1) = -5$$

$$y(7) = -5 \cos\left(\frac{\pi}{6}(7)\right)$$

$$= -5 \cos\left(\frac{7\pi}{6}\right)$$

$$= -5\left(-\frac{\sqrt{3}}{2}\right)$$

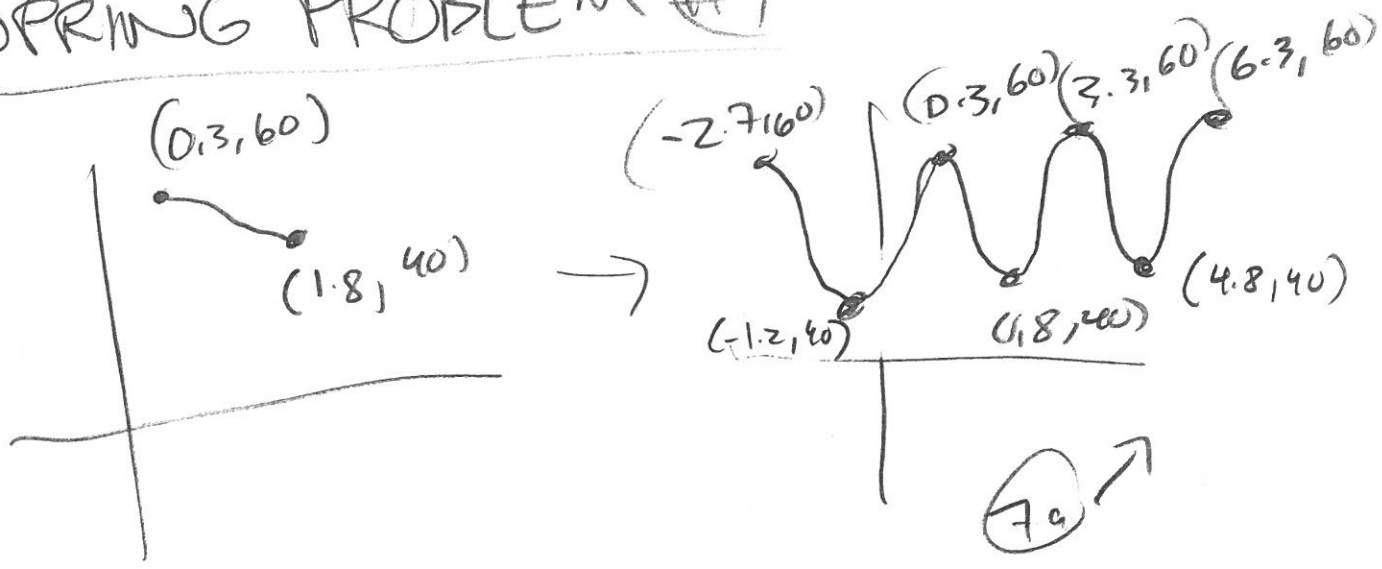
$$= \frac{5\sqrt{3}}{2}$$

$$\approx 4.330$$

$\textcircled{6b}$ max occurs at 5 ft
min occurs at -5 ft

$\textcircled{6c}$ period 12 secs

SPRING PROBLEM #7



$$\frac{1}{2} \text{ Period} = 1.8 - 0.3 = 1.5$$

$$\text{Period} = 2(1.5) = 3$$

$$y = a \text{ trig} \left(\frac{2\pi}{\text{Period}} (x - \text{shift}) \right) + d$$

$$\text{max} = 60$$

$$\text{min} = 40$$

$$\text{range} = 60 - 40 = 20$$

$$\frac{1}{2} \text{ range} = \text{amplitude} = \frac{20}{2} = 10$$

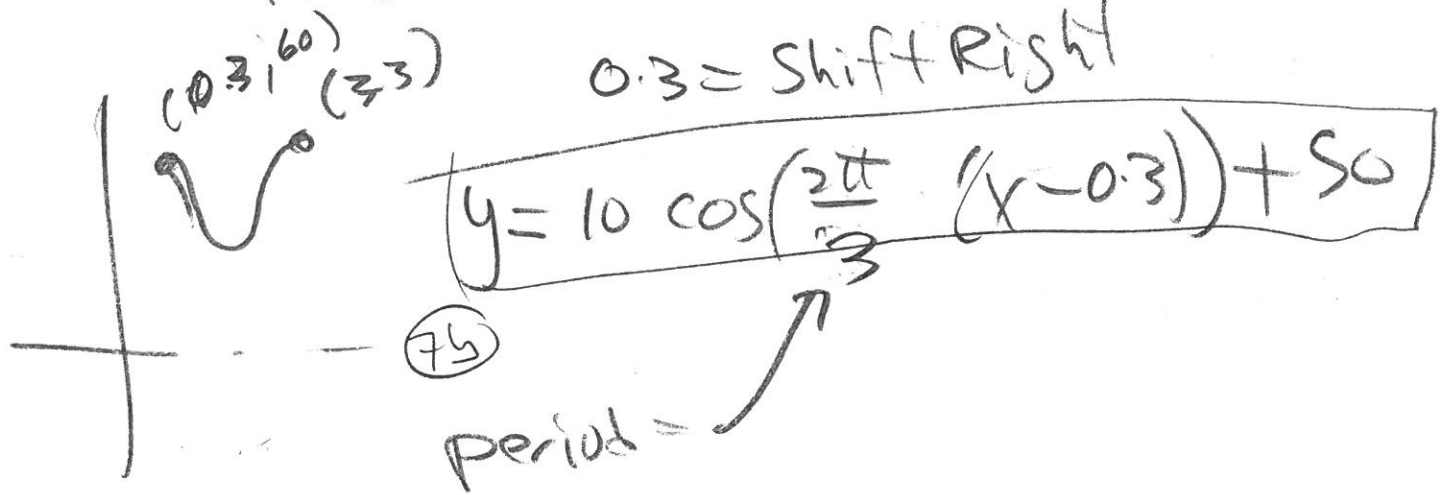
$$y = 10 \text{ trig} \left(\frac{2\pi}{\text{Period}} (x - \text{shift}) \right) + d$$

$$d = \frac{1}{2} (\text{max} + \text{min}) = \frac{1}{2} (60 + 40) = \frac{1}{2} (100) = 50$$

$$y = 10 \cos \left(\frac{2\pi}{\text{Period}} (x - \text{shift}) \right) + 50$$

why \cos shape

SPRING PROBLEM (cont)

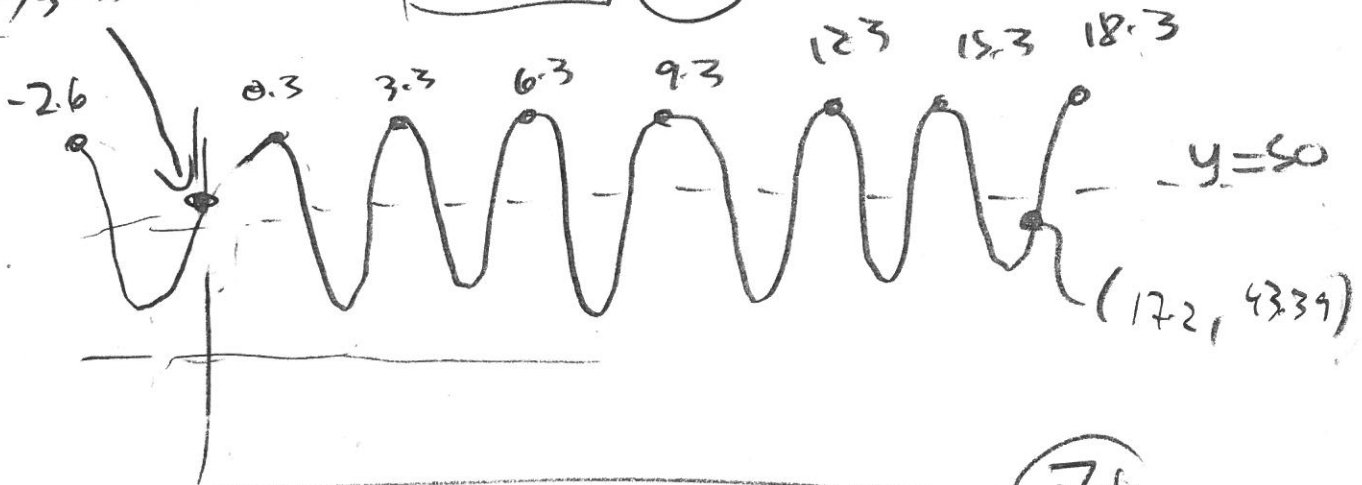


$$y(17.2) = 10 \cos\left(\frac{2\pi}{3}(17.2 - 0.3)\right) + 50$$

$$= 10 \cos\left(\frac{2\pi}{3}(16.9)\right) + 50$$

$$\approx \boxed{43.39} \quad (76)$$

$(0, 58.090)$
 $(0, y(0))$

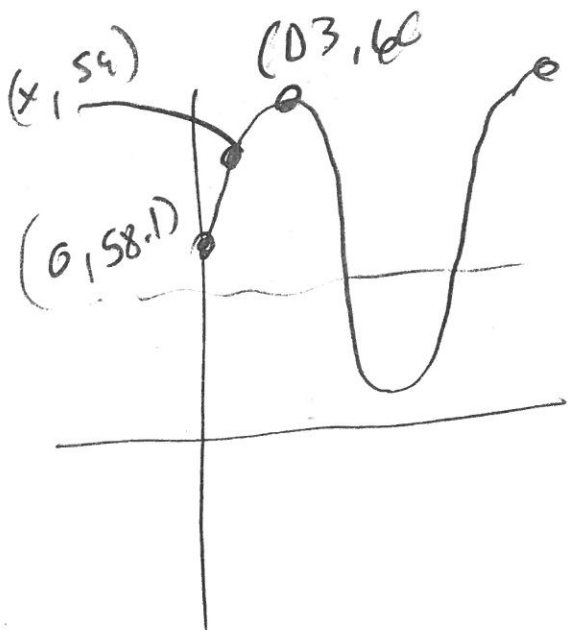


$$y(0) = 10 \left(\cos\left(\frac{2\pi}{3}(-0.3)\right) \right) + 50$$

$$\approx 58.090$$

(7d)

Spring Problem (7 cont)



$$S_9 = 10 \cos\left(\frac{2\pi}{3}(x - 0.3)\right) + 50$$

$$9 = 10 \cos\left(\frac{2\pi}{3}(x - 0.3)\right)$$

$$\frac{9}{10} = \cos\left(\frac{2\pi}{3}(x - 0.3)\right)$$

$$\frac{2\pi}{3}(x - 0.3) = \cos^{-1}\left(\frac{9}{10}\right)$$

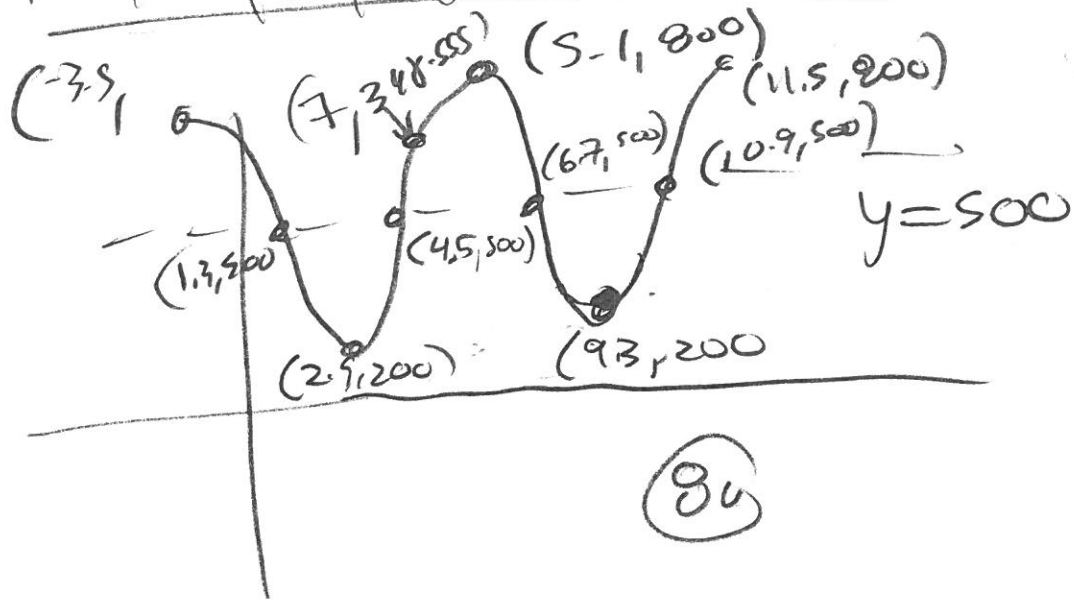
$$x - 0.3 = \frac{3}{2\pi} \cos^{-1}\left(\frac{9}{10}\right)$$

$$x = 0.3 + \frac{3}{2\pi} \cos^{-1}\left(\frac{9}{10}\right)$$

$$x \approx 0.515$$

(7e)

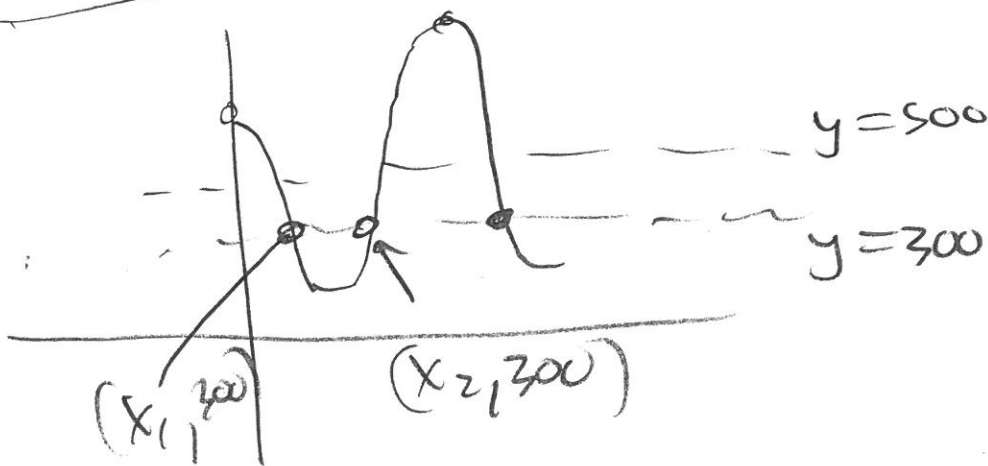
FOX POPULATION (CN) cont



$$P(x) = -300 \cos\left(\frac{2\pi}{6.4} (x - 2.9)\right) + 500$$

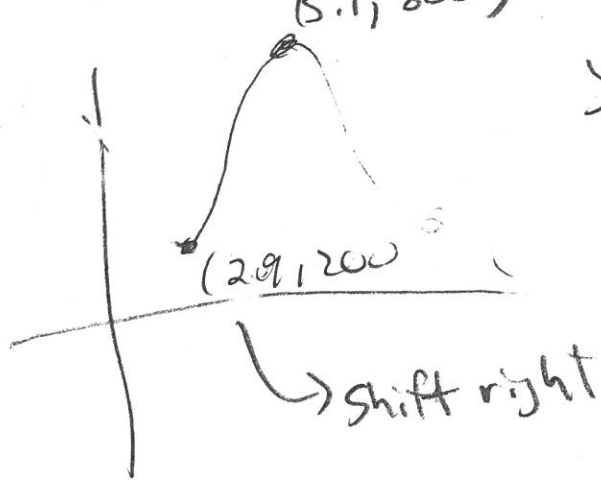
$$\textcircled{80} \quad P(7) = -300 \left(\cos\left(\frac{2\pi}{6.4} (7 - 2.9)\right)\right) + 500$$

$$P(7) \approx 348.555$$



$$x_1 = 2.043 \quad x_2 = 3.757$$

FOX POPULATION #3



$$y = a \cos\left(\frac{2\pi}{\text{period}}(x - \text{shift})\right) + d$$

$$\downarrow$$

$$a < 0$$

$$\frac{1}{2} \text{ period} = 5.1 - 2.9 = 2.2 \text{ second}$$

$$\text{period} = 6.4$$

$$y = -a \text{ amp} \cos\left(\frac{2\pi}{6.4}(x - 2.9)\right) + d$$

$$\frac{1}{2} \text{ range} = \text{amp} = \frac{1}{2}(800 - 200) = \frac{1}{2}(600) = 300$$

$$y = -300 \cos\left(\frac{2\pi}{6.4}(x - 2.9)\right) + d$$

$$d = \frac{1}{2}(\text{max} + \text{min}) = \frac{1}{2}(800 + 200) = \frac{1}{2}(1000)$$

$$d = 500$$

(8b)

$$P(x) = -300 \cos\left(\frac{2\pi}{6.4}(x - 2.9)\right) + 500$$

FOX POPULATION

$$300 = -300 \cos\left(\frac{2\pi}{6.4}(x-2.9)\right) + 500$$

$$-200 = -300 \left(\cos\left(\frac{2\pi}{6.4}(x-2.9)\right)\right)$$

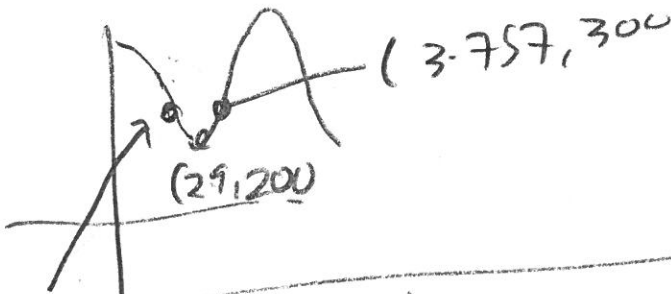
$$\frac{2}{3} = \cos\left(\frac{2\pi}{6.4}(x-2.9)\right)$$

$$\frac{2\pi}{6.4}(x-2.9) = \cos^{-1}\left(\frac{2}{3}\right)$$

$$x-2.9 = \frac{6.4}{2\pi} \cos^{-1}\left(\frac{2}{3}\right)$$

$$x = 2.9 + \frac{6.4}{2\pi} \cos^{-1}\left(\frac{2}{3}\right)$$

$$x \approx 3.757 \quad (8d)$$

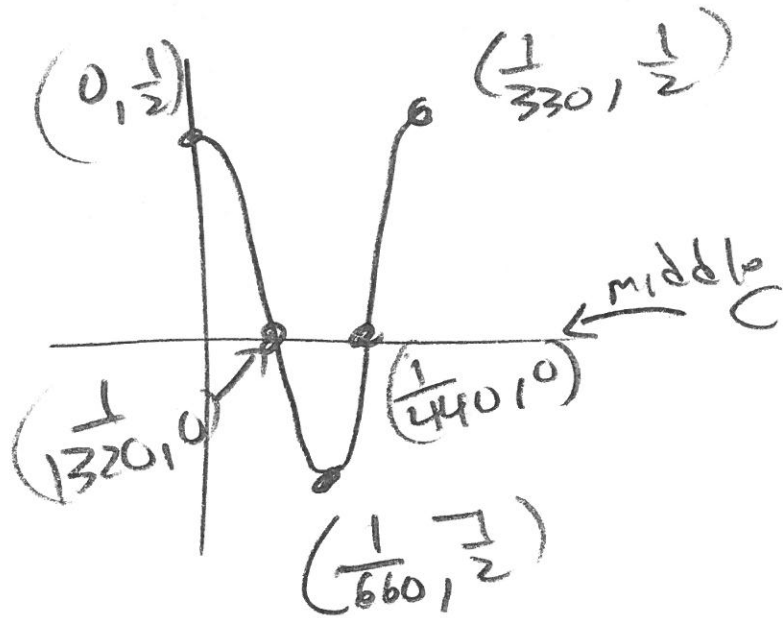


$$x_1 = 2.9 - \frac{6.4}{2\pi} \cos^{-1}\left(\frac{2}{3}\right) \approx 2.043$$

$$2.043 < x < 3.757 \leftarrow 8d$$

$$200 < P(x) < 300 \leftarrow \text{Result of } 8d$$

9) Music Problem



$$PL = \frac{2\pi}{b} \quad b = 660d$$

$$PL = \frac{2\pi}{660} = \frac{1}{330}$$

$$\text{amp} = |a|$$

$$y = 0.5 \cos(660\pi t)$$

\downarrow
 $\text{99} \rightarrow a \rightarrow \text{amp} = 0.5$
 \rightarrow

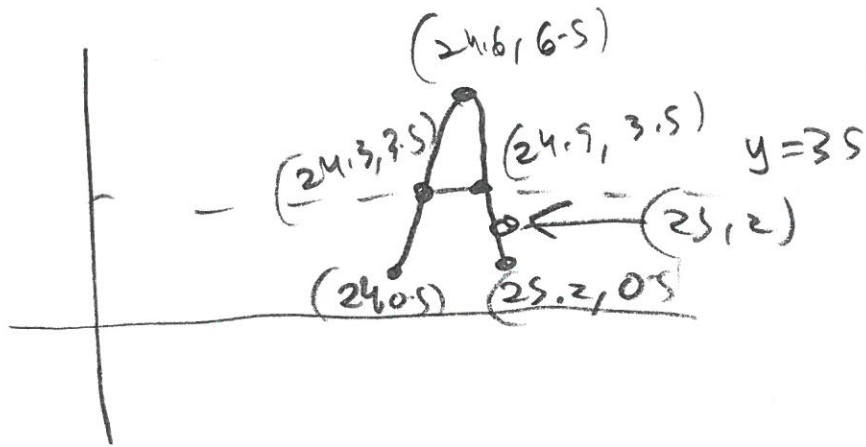
9b)

$$\text{Period} = \frac{1}{330}$$

9c) Range $[-\frac{1}{2}, \frac{1}{2}]$

$$E = C \pm \frac{1}{2}$$

Entertainment Problem (#10 con)



$$f(x) = -3 \cos\left(\frac{\pi}{3}x\right) + 3.5$$

$$f(25) = -3 \cos\left(\frac{\pi}{3}(25)\right) + 3.5$$

$$= -3 \cos\left(\frac{125\pi}{3}\right) + 3.5$$

$$= -3 \cos\left(41\frac{2}{3}\pi\right) + 3.5$$

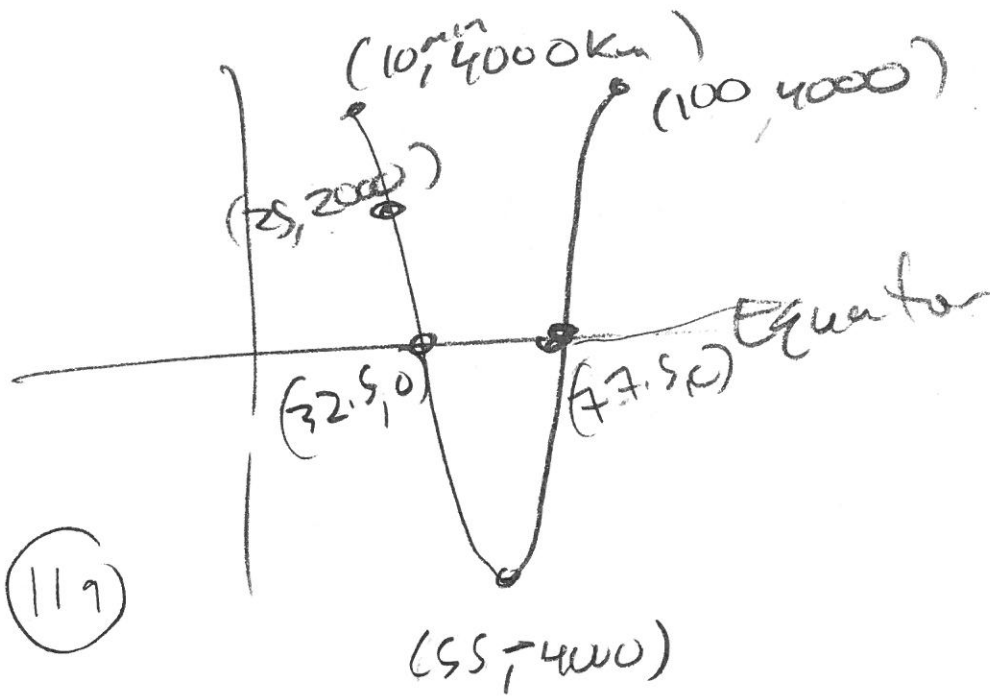
$$= -3\left(\frac{1}{2}\right) + 3.5$$

$$= -1.5 + 3.5$$

$$f(25) = 2$$

$(25, 2)$ on $f(x)$

Space SHIP Problem #11



(11a)

$$\left. \begin{array}{l} \max = 4000 \\ \min = -4000 \end{array} \right\} \begin{array}{l} \text{amp} = 4000 \\ \left. \begin{array}{l} q = +4000 \\ q = -4000 \end{array} \right\} \end{array}$$

$$y = +4000 \cos\left(\frac{2\pi}{90}(x-10)\right) + 0$$

$$y = 4000 \left(\cos\left(\frac{2\pi}{90}(x-10)\right) \right)$$

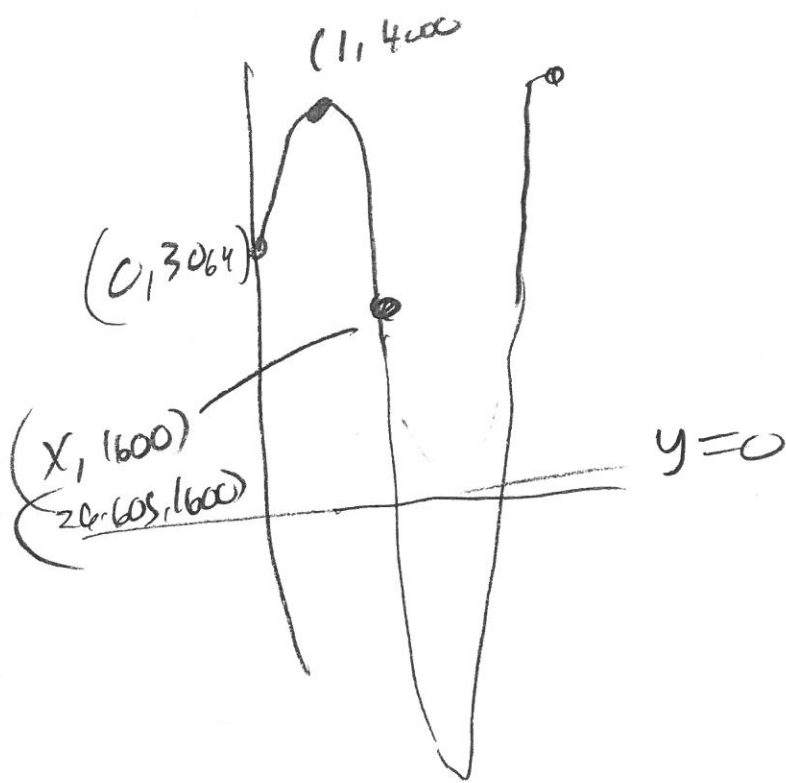
(11b)

$$y(25) = 4000 \cos\left(\frac{2\pi}{90}(25-10)\right)$$

$$= 4000 \cos\left(\frac{30\pi}{90}\right)$$

$$= 4000 \cos\left(\frac{\pi}{3}\right) = \boxed{2000}$$

Space Ship Problem cont



$$1600 = 4000 \cos\left(\frac{2\pi}{90}(x-10)\right)$$

$$\frac{1600}{4000} = \cos\left(\frac{2\pi}{90}(x-10)\right)$$

$$\cos^{-1}\left(\frac{1600}{4000}\right) = \frac{2\pi}{90}(x-10)$$

$$\frac{2\pi}{90}(x-10) = \cos^{-1}\left(\frac{1600}{4000}\right)$$

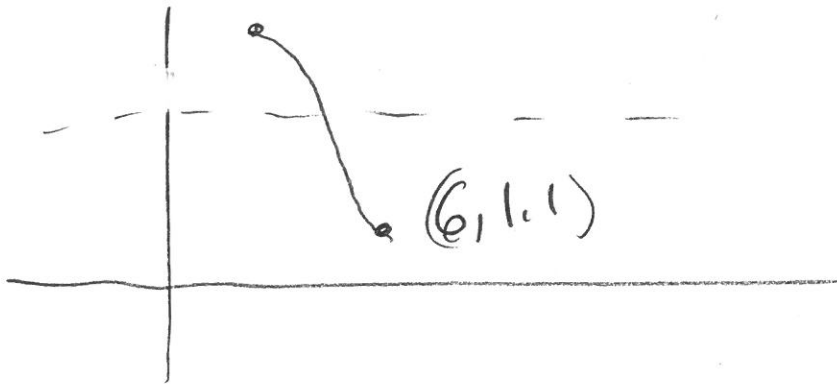
$$x-10 = \frac{90}{2\pi} \left(\cos^{-1}\left(\frac{1600}{4000}\right)\right)$$

11c

$$\boxed{x = 10 + \frac{90}{2\pi} \cos^{-1}\left(\frac{1600}{4000}\right) \approx 26.608}$$

TIDE Problem # 12

(2, 1.5)



max 1.5

min 1.1

$$\frac{1}{2}(\text{max} + \text{min}) = d = \frac{1}{2}(1.5 + 1.1) = \frac{1}{2}(2.6)$$

$$\boxed{d = 1.3}$$

$$\frac{1}{2}(\text{max} - \text{min}) = \text{amp} = \frac{1}{2}(1.5 - 1.1) = \frac{1}{2}(0.4)$$

$$\boxed{\text{amp} = 0.2}$$

$$y = \pm 0.2 \text{ trig}\left(\frac{2\pi}{\text{Period}}(x - \text{shift})\right) + 1.3$$

Shift to cosine model

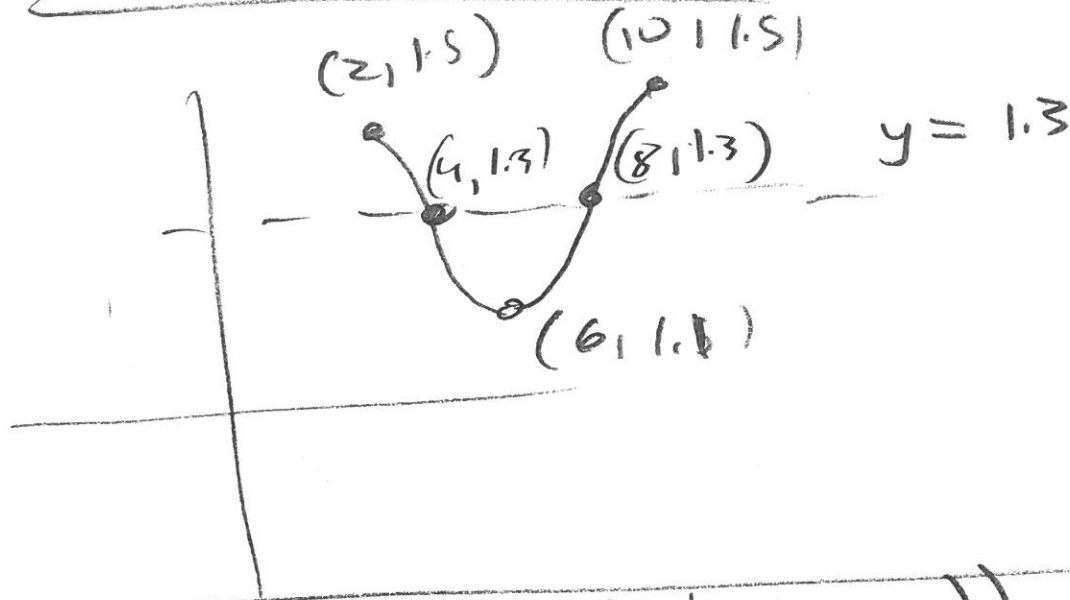
$$y = 0.2 \cos\left(\frac{2\pi}{\text{period}}(x - 2)\right) + 1.3$$

$$\frac{1}{2} \text{Period} = 4$$

$$\text{Period} = 8$$

$$\boxed{h(x) = 0.2 \cos\left(\frac{2\pi}{8}(x - 2)\right) + 1.3}$$

TIDE Problem #12 cont



$$h(x) = 0.2 \cos\left(\frac{2\pi}{8}(x-2)\right) + 1.3$$

$(x, h(x))$
 \downarrow \downarrow
 time height
 hrs at
 since time
 12:00 noon x

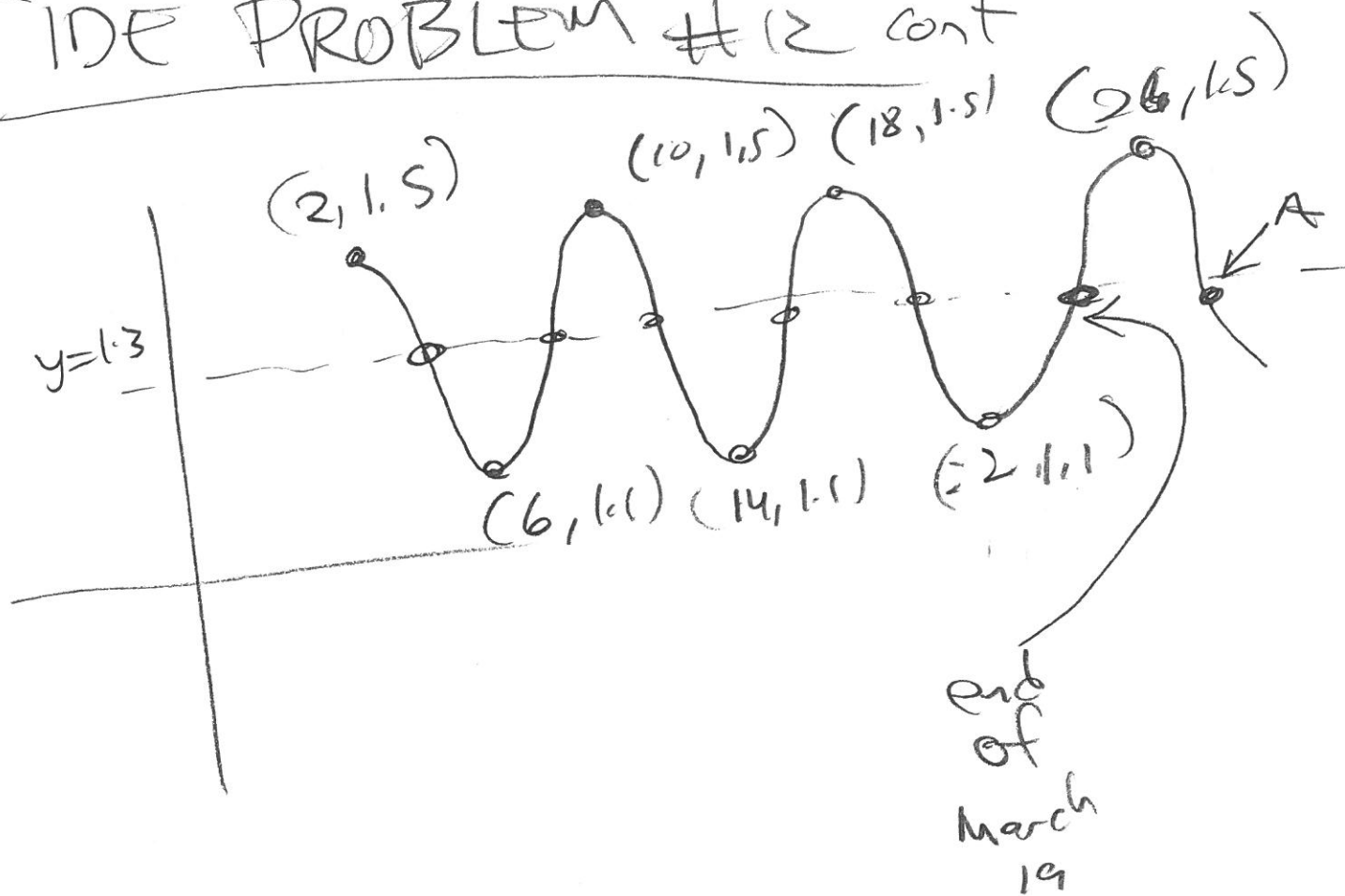
129

$$\begin{aligned}
 h(4) &= 0.2 \cos\left(\frac{2\pi}{8}(4-2)\right) + 1.3 \\
 &= 0.2 \cos\left(\frac{4\pi}{8}\right) + 1.3 \\
 &= 0.2 \cos\left(\frac{\pi}{2}\right) + 1.3
 \end{aligned}$$

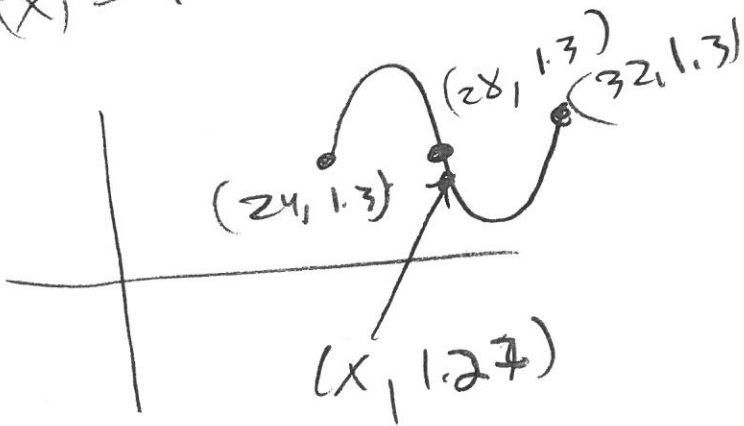
$h(4) = 1.3$ or by graph

126

TIDE PROBLEM #12 cont



$A =$ earliest time on $f(x)$ that
 $f(x) = 1.27m$ with $x > 24$



Tide Problem #12

$$f(x) = 0.2 \cos\left(\frac{2\pi}{8}(x-2)\right) + 1.3$$

$$1.27 = 0.2 \cos\left(\frac{2\pi}{8}(x-2)\right) + 1.3$$

$$-0.03 = 0.2 \cos\left(\frac{2\pi}{8}(x-2)\right)$$

$$-0.15 = \cos\left(\frac{2\pi}{8}(x-2)\right)$$

$$\frac{2\pi}{8}(x-2) = \cos^{-1}(-0.15)$$

$$x-2 = \frac{8}{2\pi} \cos^{-1}(-0.15)$$

$$x = 2 + \frac{8}{2\pi} \cos^{-1}(-0.15)$$

$$\boxed{x = 4.192}$$

$$\boxed{x = 2 - \frac{8}{2\pi} \cos^{-1}(-0.15) = -0.192}$$

$$x = \begin{cases} -0.192 + 8n \\ 4.192 + 8n \end{cases} \quad n \in \mathbb{Z}$$

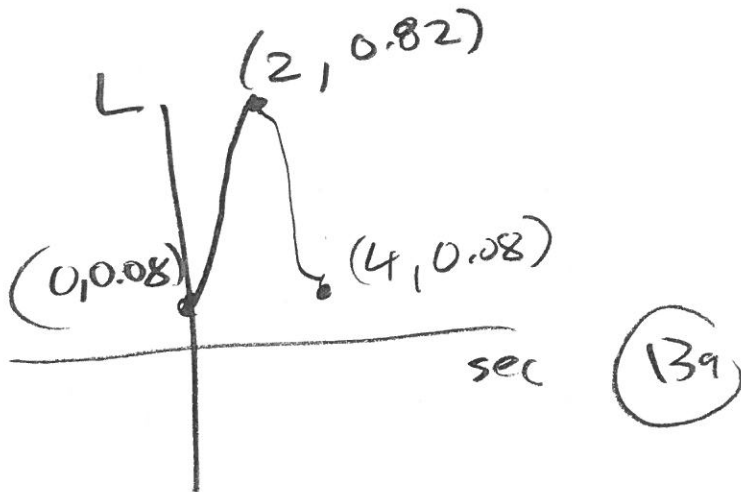
$$\boxed{\text{Let } n = 3 \quad 4.192 + 8(3) = 28.192}$$

Health Problem # B

In & out each 4 seconds

min 0.08 L max 0.82 L

min at $t=0$ max at $t=2$



$$\frac{1}{2}(\text{min} + \text{max}) = d = \frac{1}{2}(0.08 + 0.82)$$
$$= \frac{1}{2}(0.90)$$

$$d = 0.45$$

$$\frac{1}{2}(\text{max} - \text{min}) = \text{amp} = \frac{1}{2}(0.82 - 0.08)$$

$$= \frac{1}{2}(0.74)$$

$$= 0.37$$

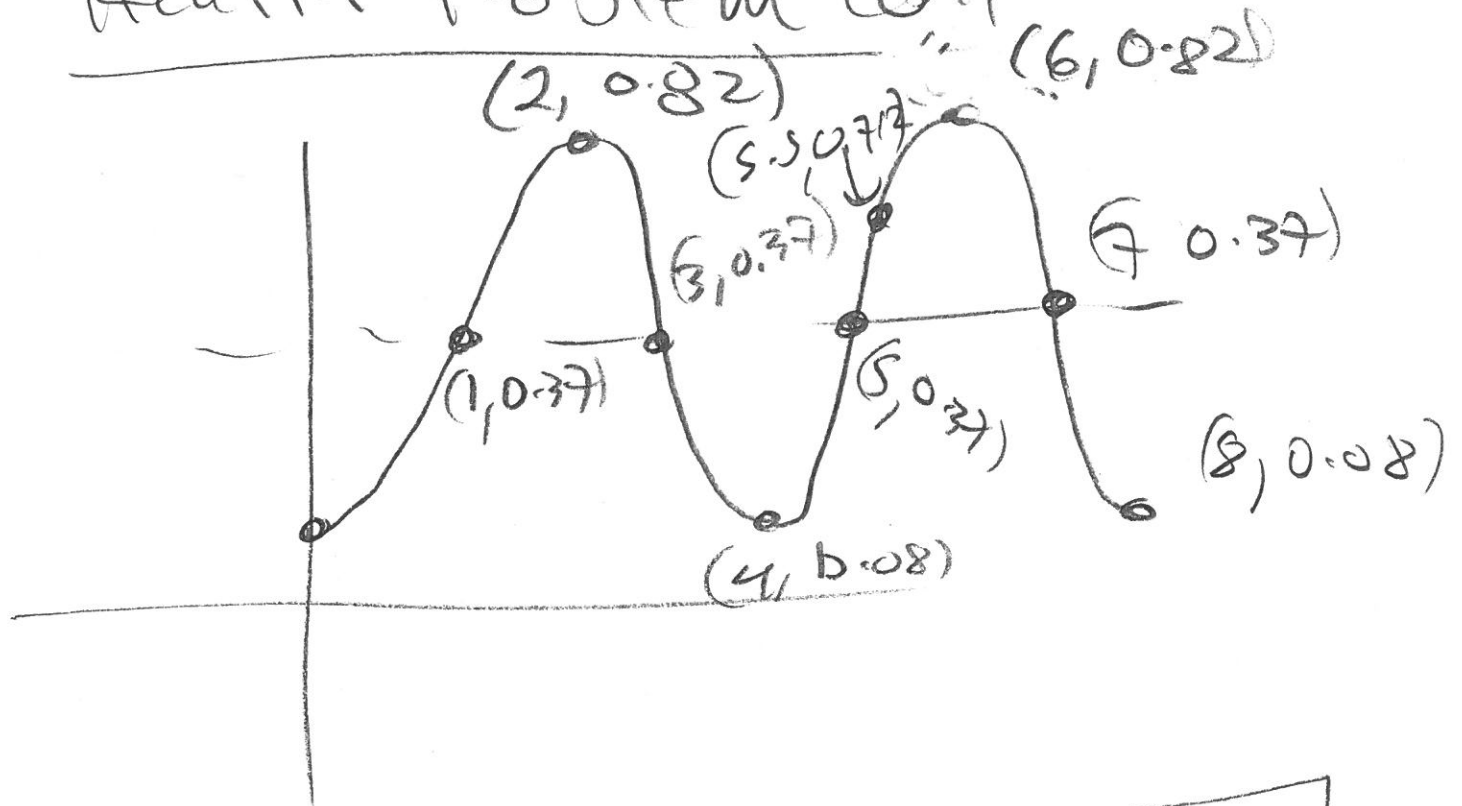
$$\text{amp} = 0.37$$

13b

PL=4

$$y = -0.37 \cos\left(\frac{2\pi}{4}(x-0)\right) + 0.45$$

Health Problem cont



$$f(x) = -0.37 \cos\left(\frac{2\pi}{4}x\right) + 0.45$$

(13b)

$$f(5.5) = -0.37 \cos\left(\frac{2\pi}{4}\left(\frac{11}{2}\right)\right) + 0.45$$

(13c)

$$= -0.37 \cos\left(\frac{22\pi}{8}\right) + 0.45$$

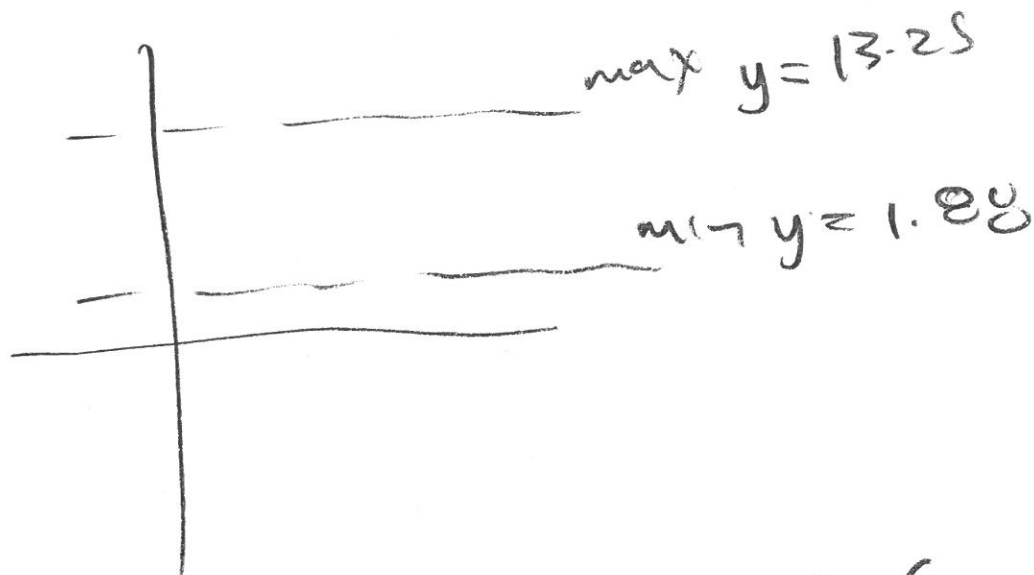
$$= -0.37 \cos\left(\frac{11\pi}{4}\right) + 0.45$$

$$= -\frac{37}{100} \cdot \frac{-\sqrt{2}}{2} + \frac{45}{100}$$

$$= \frac{+37\sqrt{2}}{200} + \frac{90}{200} = \frac{90 + 37\sqrt{2}}{200}$$

$$\boxed{20.712}$$

Problem 14) Total Problem 2



$$d = \frac{1}{2} (\max + \min) = \frac{1}{2} (13.25 + 1.88)$$

$$= \frac{1}{2} (15.13) = 7.565$$

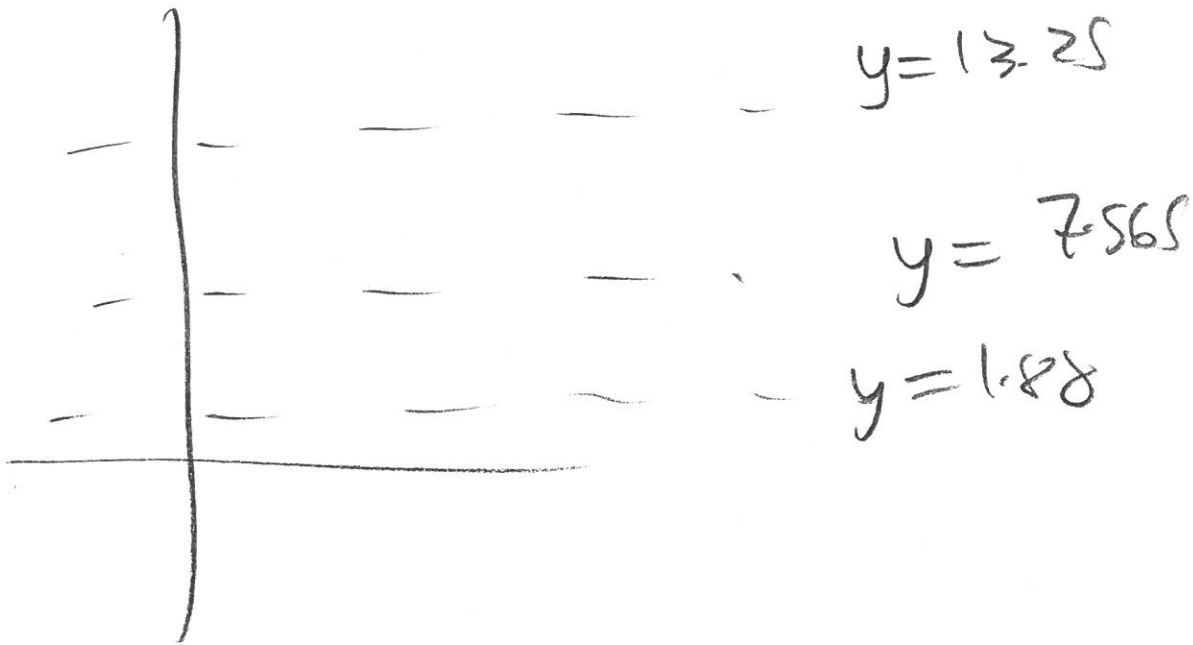
$$\text{amp} = \frac{1}{2} (\max - \min) = \frac{1}{2} (11.37) = 5.685$$

$$= \max - d = 13.25 - 7.565 = 5.685$$

$$= d - \min = 7.565 - 1.88 = 5.685$$

$$f(x) = \pm 5.685 \text{trig} \left(\frac{2\pi}{\text{period}} (x - \text{shift}) \right) + 7.56$$

Problem 14 cont



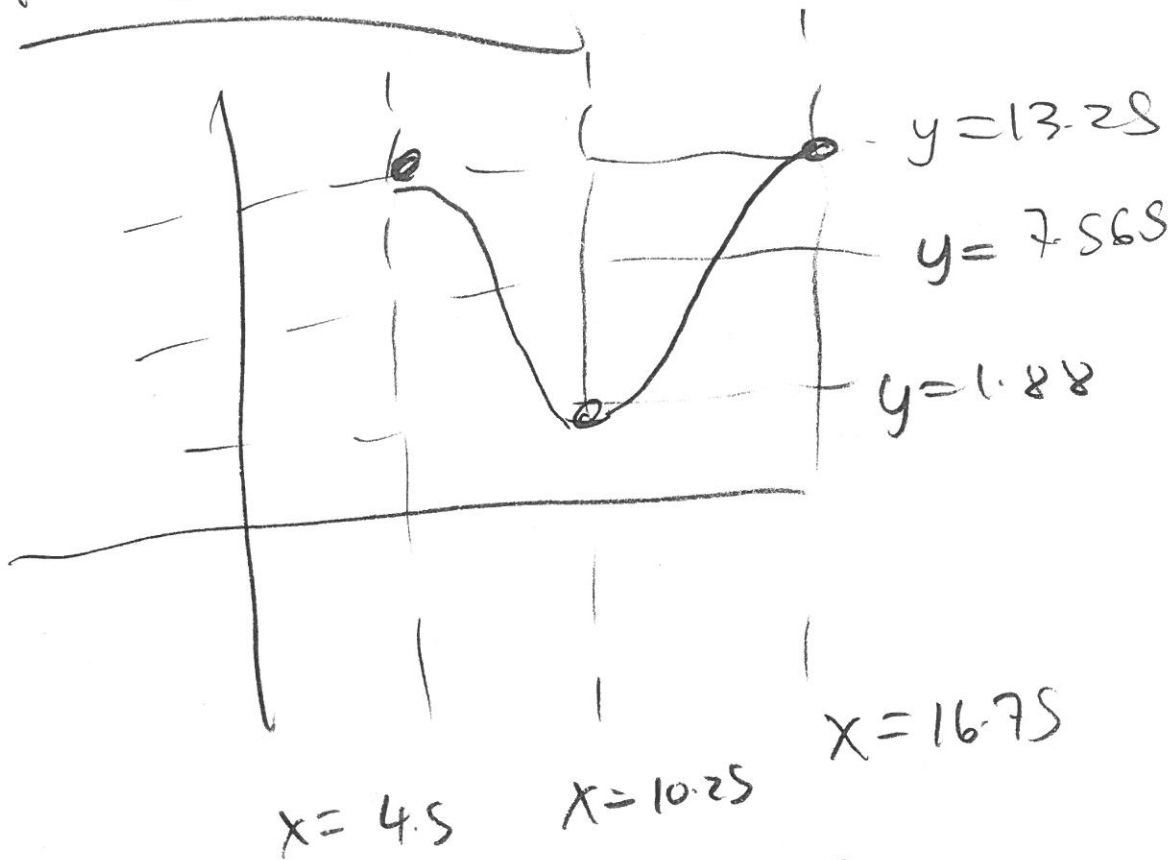
Time

4:30 am high tide = 13.25
4.5 hrs

10:15 am low tide = 1.88
10.25 hrs

4:45 pm high tide = 13.25
12 + 4.75
16.75 hrs

Problem 14 cont



not
Symmetrical