

	Model	Initial population	Change factor	Change rate as a decimal	Change rate as a percent	Growth or decay?	When does this model reach
1	$A = 100(0.023)^x$	100	0.023	0.977	97.7%	Decay	20 X = _____
2	$A = 200(1.12)^x$	200	1.12	0.12	12%	Growth	250 X = _____
3	$A = 900(0.66)^x$	900	0.66	0.34	34%	Decay	400 X = _____
4	$A(x) = 300(1.2)^x$	300	1.2	0.20	20%	Growth	650 X = _____
5	$A = 500(0.854)^x$	500	0.854	0.146	14.6%	Decay	325 X = _____
6	$A = 600(1.0025)^x$	600	1.0025	0.0025	0.25%	Growth	640 X = _____
7	$A = 700(3.1225)^x$	700	3.1225	2.1225	212.25%	Growth	2000 X = _____
8	$A(x) = 1700(2.22)^x$	1700	2.22	1.22	122%	Growth	5000 X = _____
9	$A = 800(3.25)^x$	800	3.25	2.25	225%	Growth	1200 X = _____
10	$A = 1200(0.982)^x$	1200	0.982	0.018	1.8%	Decay	1100 X = _____
11	$A = 1500(0.003)^x$	1500	0.003	0.997	99.7%	Decay	10 X = _____
12	$A(x) = 40000(0.002)^x$	40000	0.002	0.998	99.8%	Decay	1500 X = _____

- How does a change factor tell you the model is growth or decay?
- How does the model tell its growth or decay?
- How do you determine the change rate when your change factor is less than 1?
- How do you determine the rate of change as a percentage from the model?
- How do you determine the rate of change as a percentage from the change factor?
- How do you answer WHEN does this population occur problems?
- How do you determine the change factor when you know the change rate as a percentage and it is growth model?
- How do you determine the change factor when you know the change rate as a percentage and it is decay model?

Solve each equation

$5^x = 250$ $\log_5 250 = x$ $x \approx 3.431$	$x^5 = 250$ $x = \sqrt[5]{250}$ $\approx 3.017$	$\log_2 x = 6$ $2^6 = x$ $64 = x$	$\log_x 2 = 6$ $x^6 = 2$ $x = \sqrt[6]{2}$ $x \approx 1.122$
$2 \cdot 5^x = 250$ $5^x = 125$ $\log_5 125 = 3 = x$	$2 \cdot x^5 = 250$ $x^5 = 125$ $x = \sqrt[5]{125}$ $\approx 2.627$	$\log_6 x = 2$ $6^2 = x$ $x = 36$	$\log_x 6 = 2$ $x^2 = 6$ $x = \sqrt{6}$ $x \approx 1.049$
$\frac{4}{5} \cdot 5^x = 2500$ $5^x = \frac{2500 \cdot 5}{4}$ $5^x = \frac{12500}{4}$ $5^x = 3125$ $\log_5 3125 = 5$	$\frac{4}{5} \cdot x^{\frac{2}{3}} = 2500$ $x^{\frac{2}{3}} = 2500 \cdot \frac{5}{4}$ $x^{\frac{2}{3}} = \frac{12500}{4}$ $x^{\frac{2}{3}} = 3125$ $x = (3125)^{\frac{3}{2}}$ <del><math>x = 174692.811</math></del>	$3 \log_2 x = 12$ $\log_2 x = 4$ $2^4 = x$ $x = 16$	$3 \log_x 12 = 24$ $\log_x 12 = 8$ $x^8 = 12$ $x = \sqrt[8]{12}$ $\approx 1.364$

What if the directions stated that you needed the EXACT solution and NOT an approximation?

Solve #1

$$20 = 100 (0.023)^x$$

$$\frac{20}{100} = 0.023^x$$

$$\log_{0.023} \frac{20}{100} = x = \log_{0.023} \frac{1}{5} \approx 0.427$$

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Solve #2

$$250 = 200 (1.12)^x$$

$$\frac{250}{200} = 1.12^x$$

$$\log_{1.12} \left( \frac{250}{200} \right) = x = \log_{1.12} \left( \frac{5}{4} \right) \approx 1.969$$

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Solve #3

$$400 = 900 (0.66)^x$$

$$\frac{400}{900} = 0.66^x$$

$$\log_{0.66} \left( \frac{400}{900} \right) = x = \log_{0.66} \left( \frac{4}{9} \right) = 1.952$$

Solve #4

$$650 = 300(1.2)^x$$

$$\frac{650}{300} = 1.2^x$$

$$\log_{1.2} \left( \frac{650}{300} \right) = x = \log_{1.2} \left( \frac{13}{6} \right) \approx 4.241$$

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Solve #5

$$325 = 500(0.854)^x$$

$$\frac{325}{500} = 0.854^x$$

$$\log_{0.854} \left( \frac{325}{500} \right) = x = \log_{0.854} \left( \frac{13}{20} \right) \approx 2.730$$

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Solve #6

$$640 = 600(1.0025)^x$$

$$\frac{640}{600} = 1.0025^x$$

$$\log_{1.0025} \left( \frac{640}{600} \right) = x = \log_{1.0025} \left( \frac{16}{15} \right) \approx 25.848$$

Solve #7

$$2000 = 700 (3.1225)^x$$

$$\frac{2000}{700} = 3.1225^x$$

$$\log_{3.1225} \left( \frac{2000}{700} \right) = x = \log_{3.1225} \left( \frac{20}{7} \right) \approx 0.922$$

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Solve #8

$$5000 = 1700 (2.22)^x$$

$$\frac{5000}{1700} = 2.22^x$$

$$\log_{2.22} \left( \frac{5000}{1700} \right) = x = \log_{2.22} \left( \frac{50}{17} \right) \approx 1.353$$

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Solve #9

$$1200 = 800 (3.25)^x$$

$$\frac{1200}{800} = 3.25^x$$

$$\log_{3.25} \left( \frac{1200}{800} \right) = x = \log_{3.25} \left( \frac{3}{2} \right) \approx 0.344$$



Solve #10

$$1100 = 1200(0.982)^x$$

$$\frac{1100}{1200} = 0.982^x$$

$$\log_{0.982} \frac{1100}{1200} = x = \log_{0.982} \left( \frac{11}{12} \right) \\ \approx 4.790$$

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Solve #11

$$10 = 1500(0.003)^x$$

$$\frac{10}{1500} = 0.003^x$$

$$\log_{0.003} \left( \frac{10}{1500} \right) = x = \log_{0.003} \left( \frac{1}{150} \right) \approx 0.863$$

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Solve #12

$$1500 = 40000(0.002)^x$$

$$\frac{1500}{40000} = 0.002^x$$

$$\log_{0.002} \frac{1500}{40000} = x = \log_{0.002} \left( \frac{3}{80} \right) \\ = 0.899$$