

Radical Form = Exponential Form

$$\sqrt[n]{a^m} = a^{m/n}$$

① $\sqrt[3]{s^1 x^1 y^2} = \underbrace{s^{1/3} x^{1/3} y^{2/3}}_{\text{exponential form}}$

↓
radical form

② $\sqrt{14^1 x^5 y^1 w^7} = 14^{1/2} x^{5/2} y^{1/2} w^{7/2}$

Radical form

Exponential form

③ $2s^{1/3} x^{2/3} y^{4/3} = \overset{\leftarrow \text{index}}{\sqrt[3]{2s^1 x^2 y^4}} = y^1 \sqrt[3]{2s^1 x^2 y^2}$

index = 3
exponential form

Radical Form

Simplified Radical Form

④ $10^{7/2} x^{7/2} y^1 = y^1 \sqrt{10^1 x^7} = y^1 x^3 \sqrt{10^1 x^1}$

index of 2

Radical Form

Simplified Radical Form

$$\begin{aligned}
 \textcircled{5} \sqrt{100x^3y^4} &= (100)^{1/2} x^{3/2} y^{4/2} \\
 &= (10^2)^{1/2} x^{1\frac{1}{2}} y^2 \\
 &= 10^{2/2} x^{1+\frac{1}{2}} y^2 \\
 &= 10^1 x^1 x^{\frac{1}{2}} y^2 \\
 &= \boxed{10xy^2\sqrt{x}} \quad \text{correct}
 \end{aligned}$$

$$\begin{aligned}
 \text{OR} \quad \sqrt{100} \sqrt{x^3} \sqrt{y^4} &= 10 \sqrt{x^2} \sqrt{x} y^{4/2} \\
 &= 10 x^{2/2} \sqrt{x} y^2 \\
 &= 10x^1 \sqrt{x} y^2 \\
 &= \boxed{10xy^2\sqrt{x}} \quad \text{correct}
 \end{aligned}$$

Error Analysis

- ① last \sqrt{x} ?
- ② $\sqrt{100} \neq 50$

$$\begin{aligned}
 \textcircled{6} \quad \sqrt[3]{27x^9y^{12}} &= \sqrt[3]{3^3x^9y^{12}} \\
 &= 3^{3/3}x^{9/3}y^{12/3} \\
 &= 3^1x^3y^4 \\
 &= \boxed{3x^3y^4} \text{ correct}
 \end{aligned}$$

$$\begin{aligned}
 \sqrt[3]{27} \sqrt[3]{x^9} \sqrt[3]{y^{12}} &= 3x^{9/3}y^{12/3} \\
 &= \boxed{3^1x^3y^4}
 \end{aligned}$$

Error Analysis

$$\sqrt{27} \checkmark = 3$$

$$x^6 \neq \sqrt[3]{x^9}$$

$$y^{12} \neq \sqrt[3]{y^{12}}$$

subtracted instead of \div

subtracted instead of \div

$$\textcircled{+} \frac{1}{\sqrt[3]{s}} \neq \frac{1}{\sqrt[3]{s}} \cdot \frac{\sqrt[3]{s}}{\sqrt[3]{s}} \neq \frac{\sqrt[3]{s}}{s}$$

$$\begin{aligned} \frac{1}{\sqrt[3]{s^1}} &= \frac{1}{\sqrt[3]{s^1}} \cdot \frac{\sqrt[3]{s^2}}{\sqrt[3]{s^2}} = \frac{\sqrt[3]{s^2}}{\sqrt[3]{s^3}} = \frac{\sqrt[3]{s^2}}{s^{\frac{3}{3}}} \\ &= \frac{\sqrt[3]{2s}}{s} = \frac{\sqrt[3]{s^2}}{s} \end{aligned}$$

OR

$$\frac{1}{\sqrt[3]{s}} \cdot \frac{\sqrt[3]{2s}}{\sqrt[3]{2s}} = \frac{\sqrt[3]{2s}}{\sqrt[3]{12s}} = \left(\frac{\sqrt[3]{2s}}{s} \right)$$

Error analysis

need $\frac{1}{\sqrt[m]{x^1}} = \frac{\sqrt[m]{x^{m-1}}}{\sqrt[m]{x^m}}$

$$\frac{1}{\sqrt[3]{s^1}} \cdot \frac{\sqrt[3]{s^2}}{\sqrt[3]{s^2}}$$

instead of
①

OR

resulting
power

in
denominator

is

always = to index

$$\begin{aligned}
 \textcircled{8} \quad \sqrt{4x^{81}y^9} &= \sqrt{4} \sqrt{x^{80}} \sqrt{x^1} \sqrt{y^8} \sqrt{y^1} \\
 &= 2 x^{80/2} \sqrt{x^1} y^{8/2} \sqrt{y^1} \\
 &= 2 x^{40} \sqrt{x^1} y^4 \sqrt{y^1} \\
 &= \boxed{2x^{40}y^4\sqrt{xy}}
 \end{aligned}$$

Error Analysis

$$\sqrt{4} = 2$$

$$\sqrt{x^{81}} \neq x^9$$

$$\sqrt{y^9} \neq y^3$$

} took $\sqrt{\quad}$ of exponent

$$\begin{aligned}
 \textcircled{9} \quad \sqrt[3]{32 x^9 y^4} &= \sqrt[3]{8} \sqrt[3]{4} x^{9/3} \sqrt[3]{y^4} \\
 &= 2 \sqrt[3]{4} x^3 y^{9/3} \sqrt[3]{y^2} \\
 &= \boxed{2 x^3 y^3 \sqrt[3]{4 y^2}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{9} \quad \sqrt[3]{32 x^9 y^{11}} &= \sqrt[3]{2^5 x^9 y^{11}} \\
 &= 2^{5/3} x^{9/3} y^{11/3} \\
 &= 2^{1+2/3} x^3 y^{3+2/3} \\
 &= 2^1 \cdot 2^{2/3} x^3 y^3 y^{2/3} \\
 &= 2^1 x^3 y^3 2^{2/3} y^{2/3} \\
 &= 2 x^3 y^3 \sqrt[3]{2^2 y^2} \\
 &= \boxed{2 x^3 y^3 \sqrt[3]{4 y^2}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{10} \quad \sqrt[3]{-8x^6y^2} &= \sqrt[3]{-8} x^{6/3} \sqrt[3]{y^2} \\
 &= -2 x^2 \sqrt[3]{y^2} \\
 &= \boxed{-2x^2 \sqrt[3]{y^2}}
 \end{aligned}$$

$$\begin{aligned}
 \sqrt[3]{-8x^6y^2} &= \sqrt[3]{(-2)^3 x^6 y^2} = (-2)^{3/3} x^{6/3} y^{2/3} \\
 &= (-2)^1 x^2 y^{2/3} \\
 &= \boxed{-2x^2 \sqrt[3]{y^2}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{11} \quad \sqrt{1200x^4y^1w^8} &= \sqrt{400} \sqrt{3} \sqrt{x^4} \sqrt{y^1} \sqrt{w^8} \\
 &= 20\sqrt{3} x^{4/2} y^{1/2} w^{8/2} \\
 &= \boxed{20x^2y^{1/2}\sqrt{3}w^4}
 \end{aligned}$$

$$\begin{aligned}
 \sqrt{1200x^4y^1w^8} &= \sqrt{2^4 \cdot 3 \cdot 5^2} \sqrt{x^4} \sqrt{y^1} \sqrt{w^8} \\
 &= 2^{4/2} \cdot 3^{1/2} \cdot 5^{2/2} x^{4/2} y^{1/2} w^{8/2} = 2^2 \cdot 3^{1/2} \cdot 5^1 x^2 y^{1/2} w^4 \\
 &= 2^2 \cdot 5^1 x^2 w^4 \cdot 3^{1/2} y^{1/2} = \boxed{2^2 \cdot 5^1 x^2 w^4 \sqrt{3y}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{12} \quad \sqrt{\frac{25}{80xy^4}} &= \sqrt{\frac{25}{80}} \sqrt{\frac{1}{x}} \sqrt{\frac{1}{y^4}} \\
 &= \sqrt{\frac{5}{16}} \frac{1}{\sqrt{x}} \frac{1}{\sqrt{y^4}} \\
 &= \frac{\sqrt{5}}{\sqrt{16}} \cdot \frac{1}{\sqrt{x}} \frac{\sqrt{x}}{\sqrt{x}} \frac{1}{y^{4/2}} \\
 &= \frac{\sqrt{5}}{4} \frac{\sqrt{x}}{\sqrt{x^2}} \frac{1}{y^2} \\
 &= \frac{\sqrt{5x}}{4xy^2}
 \end{aligned}$$

$$\begin{aligned}
 \frac{\sqrt{25}}{\sqrt{80}} \frac{1}{\sqrt{x}} \frac{1}{\sqrt{y^4}} &= \frac{5}{\sqrt{16} \sqrt{5}} \cdot \frac{1}{\sqrt{x} \sqrt{x}} \cdot \frac{1}{y^{4/2}} \\
 &= \frac{5}{4\sqrt{5}} \cdot \frac{\sqrt{x}}{\sqrt{x^2}} \cdot \frac{1}{y^2} = \frac{5\sqrt{x}}{4xy^2\sqrt{5}} \\
 &= \frac{5\sqrt{x}}{4xy^2\sqrt{5}} \frac{\sqrt{5}}{\sqrt{5}} = \frac{5\sqrt{5x}}{4xy^2\sqrt{25}} = \frac{5\sqrt{5x}}{4 \cdot 5xy^2} \\
 &= \frac{5}{20} \frac{\sqrt{5x}}{xy^2} = \frac{1}{4} \cdot \frac{\sqrt{5x}}{xy^2} = \frac{\sqrt{5x}}{4xy^2}
 \end{aligned}$$

(12)

$$\sqrt{\frac{2s}{80xy^4}} = \sqrt{\frac{s^2}{2^4 s^1}} \sqrt{\frac{1}{xy^4}}$$

$$= \frac{\sqrt{s^1}}{\sqrt{2^4}} \frac{1}{\sqrt{x}} \frac{1}{y^{4/2}} = \frac{\sqrt{s}}{2^{4/2}} \frac{1}{\sqrt{x}} \frac{\sqrt{x}}{\sqrt{x}} \frac{1}{y^2}$$

$$= \frac{\sqrt{s} \cdot x}{2^2 \sqrt{x^2} y^2} = \frac{\sqrt{sx}}{4y^2 \cdot x}$$

(13)

$$\sqrt{\frac{3x^5y^4}{27x^1y^{41}}} = \sqrt{\frac{3}{27}} \sqrt{\frac{x^4}{1}} \cdot \sqrt{\frac{1}{y^{37}}}$$

$$= \sqrt{\frac{1}{9}} \frac{\sqrt{x^4}}{1} \sqrt{\frac{1}{y^{36}}} \frac{1}{\sqrt{y}}$$

$$= \frac{1}{3} \frac{x^{4/2}}{1} \frac{1}{y^{36/2}} \frac{1}{\sqrt{y}}$$

$$= \frac{1}{3} \frac{x^2}{1} \frac{1}{y^{18}} \frac{1}{\sqrt{y}}$$

$$= \frac{x^2}{3y^{18}\sqrt{y}} = \frac{x^2}{3y^{18}} \frac{1}{\sqrt{y}} \frac{\sqrt{y}}{\sqrt{y}}$$

$$= \frac{x^2\sqrt{y}}{3y^{18}\sqrt{y^2}} = \frac{x^2\sqrt{y}}{3y^{18}y^1} = \frac{x^2\sqrt{y}}{3y^{19}}$$

(13)

$$\sqrt{\frac{3x^5y^4}{27x^1y^4}} = \sqrt{\frac{3^1 x^5 y^4}{3^3 x^1 y^4}} \quad \frac{\sqrt{3x^4y^1}}{\sqrt{3x^0y^1}}$$

$$= \frac{\sqrt{3^2} \sqrt{x^6} \sqrt{y^5}}{\sqrt{3^4} \sqrt{x^2} \sqrt{y^4}}$$

$$= \frac{3^{2/2} x^{6/2} y^{5/2}}{3^{4/2} x^{2/2} y^{4/2}}$$

$$= \frac{3^1 x^3 y^{2\frac{1}{2}}}{3^2 x^1 y^2}$$

$$= \frac{1}{3} \frac{x^2}{1} \frac{y^2 y^{\frac{1}{2}}}{y^2}$$

$$= \frac{1}{3} \frac{x^2}{1} \frac{1}{y^1} \frac{y^{\frac{1}{2}}}{1}$$

$$= \frac{x^2 \sqrt{y}}{3 y^1}$$

(14)

$$\sqrt[3]{\frac{125x^{12}}{16x^{24}y^5}} = \frac{\sqrt[3]{125} \sqrt[3]{x^{12}}}{\sqrt[3]{8 \cdot 2} \sqrt[3]{x^{24}} \sqrt[3]{y^3} \sqrt[3]{y^2}}$$

$$= \frac{5x^{12/3}}{\sqrt[3]{8} \sqrt[3]{2} x^{24/3} y^{3/3} \sqrt[3]{y^2}}$$

$$= \frac{5x^4}{2 \sqrt[3]{2} x^8 y^1 \sqrt[3]{y^2}}$$

$$= \frac{5x^4}{2x^8y^1 \sqrt[3]{2y^2}}$$

$$= \frac{5}{2} \frac{1}{x^4} \frac{1}{y^1} \frac{1}{\sqrt[3]{2y^2}} \frac{\sqrt[3]{2^2y^1}}{\sqrt[3]{2^2y^1}}$$

$$= \frac{5}{2} \frac{1}{x^4} \frac{1}{y^1} \frac{1}{\sqrt[3]{8y^3}} \frac{\sqrt[3]{4y^1}}{1}$$

$$= \frac{5}{2} \cdot \frac{1}{x^4} \frac{1}{y^1} \frac{1}{2y^1} \frac{\sqrt[3]{4y^1}}{1}$$

$$\boxed{\frac{5 \sqrt[3]{4y}}{4x^4y^2}}$$

(14)

$$\sqrt[3]{\frac{125 x^{12}}{16 x^{24} y^5}} = \frac{\sqrt[3]{125}}{\sqrt[3]{16} \sqrt[3]{2}} \cdot \sqrt[3]{\frac{1}{x^{12}}} \sqrt[3]{\frac{1}{y^5}}$$

$$= \frac{5}{2 \sqrt[3]{2}} x^{12/3} \cdot \frac{1}{\sqrt[3]{y^3} \sqrt[3]{y^2}}$$

$$= \frac{5}{2} \frac{1}{\sqrt[3]{2}} x^4 y^{3/3} \frac{1}{\sqrt[3]{y^2}}$$

$$= \frac{5}{2} \frac{1}{x^4 y^1} \frac{1}{\sqrt[3]{2y^2}} \sqrt[3]{2^2 y^1}$$

$$= \frac{5}{2} \frac{\sqrt[3]{4y^1}}{x^4 y^1} \frac{1}{\sqrt[3]{y^2}}$$

$$= \frac{5}{2} \frac{\sqrt[3]{4y^1}}{x^4 y^1} \frac{1}{2y}$$

$$= \frac{5}{4} \frac{1}{x^4 y^2} \frac{\sqrt[3]{4y^1}}{1}$$

$$= \frac{5 \sqrt[3]{4y}}{4x^4 y^2}$$

$$(16) \quad \frac{3}{4} \cdot \frac{x^{\frac{3}{2}}}{x^{-\frac{1}{2}}} \cdot \frac{y^{-\frac{7}{2}}}{y^{-2}} \cdot \frac{2}{9} \cdot \frac{x^0}{x^{\frac{5}{2}}} \cdot \frac{y^3}{y^1}$$

$$\frac{3}{4} \cdot \frac{2}{9} \cdot \frac{x^{\frac{3}{2}} x^0}{x^{-\frac{1}{2}} x^{\frac{5}{2}}} \cdot \frac{y^{-\frac{7}{2}} y^3}{y^{-2} y^1}$$

$$\frac{6}{36} \cdot \frac{x^{\frac{3}{2}} x^{\frac{1}{2}} \cdot 1}{x^{\frac{5}{2}}} \cdot \frac{y^3 y^2}{y^{\frac{7}{2}} y^1}$$

$$\frac{1}{6} \cdot \frac{x^{\frac{4}{2}}}{x^{\frac{5}{2}}} \cdot \frac{y^5}{y^{\frac{9}{2}}}$$

$$\frac{1}{6} \cdot \frac{1}{x^{\frac{1}{2}}} \cdot \frac{y^{\frac{1}{2}}}{1}$$

$$\frac{\sqrt{y^1}}{6 \sqrt{x^1}} = \frac{\sqrt{y}}{6} \frac{1}{\sqrt{x}} \frac{\sqrt{x}}{\sqrt{x}} = \frac{\sqrt{x \cdot y}}{6 \sqrt{x^2}}$$

$$= \frac{\sqrt{xy}}{6x}$$

$$\textcircled{16} \quad \frac{3x^{\frac{3}{2}}y^{-\frac{7}{2}} \cdot 2x^0y^3}{4x^{-\frac{1}{2}}y^{-2} \cdot 9x^{\frac{5}{2}}y^1}$$

$$\frac{3}{4} \cdot \frac{2}{9} \cdot \frac{x^{\frac{3}{2}+0}}{x^{-\frac{1}{2}+\frac{5}{2}}} \cdot \frac{y^{-\frac{7}{2}+3}}{y^{-2+1}}$$

$$\frac{6}{36} \cdot \frac{x^{\frac{3}{2}}}{x^2} \cdot \frac{y^{-\frac{1}{2}}}{y^{-1}}$$

$$\frac{1}{6} \cdot \frac{1}{x^{\frac{1}{2}}} \cdot \frac{y^1}{y^{\frac{1}{2}}}$$

$$\frac{1}{6} \cdot \frac{1}{x^{1/2}} \cdot \frac{y^{1/2}}{1}$$

$$\frac{1}{6} \cdot \frac{1}{\sqrt{x}} \cdot \frac{\sqrt{y}}{1} = \frac{\sqrt{y}}{6} \cdot \frac{1}{\sqrt{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}}$$

$$= \frac{\sqrt{yx}}{6\sqrt{x^2}}$$

$$= \frac{\sqrt{xy}}{6x}$$