

# EVEN MORE PROPERTIES OF EXPONENTS

$$\begin{aligned}
 \textcircled{2} \quad (x^4)^{-3} 2^1 x^4 &= x^{-12} \cdot 2^1 \cdot x^4 \\
 &= 2^1 x^4 x^{-12} \\
 &= 2 \frac{x^4}{x^{12}} = \frac{2}{1} \frac{1}{x^8} = \boxed{\frac{2}{x^8}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{4} \quad (2^1 v^1)^2 2^1 v^2 &= 2^2 v^2 2^1 v^2 \\
 &= 2^2 2^1 v^2 v^2 = 2^3 v^4 = \boxed{8v^4}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{6} \quad \frac{2^1 y^3 \cdot 3^1 x^1 y^3}{3^1 x^2 y^4} &= \frac{2^1 \cdot 3^1}{3^1} \cdot \frac{x^1}{x^2} \cdot \frac{y^3 y^3}{y^4} \\
 &= \frac{6}{3} \cdot \frac{1}{x} \cdot \frac{y^6}{y^4} \\
 &= \frac{2}{1} \cdot \frac{1}{x} \cdot \frac{y^2}{1} \\
 &= \boxed{\frac{2y^2}{x}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{8} \quad \frac{3^1 x^2 y^2}{2^1 x^{-1} 4^1 y^1 x^2} &= \frac{3^1}{2^1 \cdot 4^1} \cdot \frac{x^2 x^1}{x^2} \cdot \frac{y^2}{y^1} \\
 &= \frac{3}{8} \cdot \frac{x^3}{x^2} \cdot \frac{y}{1} \\
 &= \frac{3}{8} \cdot \frac{x}{1} \cdot \frac{y}{1} = \boxed{\frac{3xy}{8}}
 \end{aligned}$$

$$\begin{aligned} \textcircled{10} \quad \frac{2^1 m^{-4}}{(2^1 m^{-4})^3} &= \frac{2^1 m^{-4}}{2^3 m^{-12}} = \frac{2^1}{2^3} \frac{m^{12}}{m^4} \\ &= \frac{1}{2^2} \frac{m^8}{1} \\ &= \boxed{\frac{m^8}{4}} \end{aligned}$$

$$\textcircled{12} \quad \frac{2^1 x^3}{(x^{-1})^3} = \frac{2^1}{1} \frac{x^3}{x^{-3}} = \frac{2^1}{1} \cdot \frac{x^3 x^3}{1} = \boxed{2x^6}$$

$$\begin{aligned} \textcircled{14} \quad x^4 y^3 \cdot (2^1 y^2)^0 &= x^4 y^3 2^0 y^0 = x^4 y^3 \cdot 1 \cdot 1 \\ &= \boxed{x^4 y^3} \end{aligned}$$

$$\begin{aligned} \textcircled{16} \quad (2^1 x^0 y^2)^{-3} \cdot 2^1 y^1 x^3 &= 2^{-3} x^0 y^{-6} \cdot 2^1 y^1 x^3 \\ &= \frac{2^1}{2^3} \frac{x^0 x^3}{1} \frac{y^1}{y^6} \\ &= \frac{1}{2^2} \frac{x^3}{1} \frac{1}{y^5} = \boxed{\frac{x^3}{4y^5}} \end{aligned}$$

$$\begin{aligned} \textcircled{18} \quad \frac{(x^{-3})^4 x^4}{2^1 x^{-3}} &= \frac{x^{-12} x^4}{2^1 x^{-3}} = \frac{1}{2} \frac{x^4 x^3}{x^{12}} \\ &= \frac{1}{2} \frac{x^7}{x^{12}} = \frac{1}{2} \frac{1}{x^5} = \boxed{\frac{1}{2x^5}} \end{aligned}$$

$$\begin{aligned}
 \textcircled{20} \quad \frac{(2^1 x^3 z^2)^3}{x^3 y^4 z^2 x^{-4} z^3} &= \frac{2^3 x^9 z^6}{x^3 y^4 z^2 x^{-4} z^3} \\
 &= \frac{2^3}{1} \frac{x^9 x^4}{x^3} \frac{1}{y^4} \frac{z^6}{z^2 z^3} \\
 &= \frac{8}{1} \frac{x^{13}}{x^3} \frac{1}{y^4} \frac{z^6}{z^5} \\
 &= \frac{8}{1} \frac{x^{10}}{1} \frac{1}{y^4} \frac{z^1}{1} \\
 &= \boxed{\frac{8 x^{10} z^1}{y^4}}
 \end{aligned}$$

$$\textcircled{22} \quad \frac{(2^1 h^1 j^2 k^{-2} \cdot h^4 j^{-1} k^4)^0}{2^1 h^{-3} j^{-4} k^{-2}} = \frac{2^0 h^0 j^0 k^0 h^0 j^0 k^0}{2^1 h^{-3} j^{-4} k^{-2}}$$

$$= \frac{1}{2} \frac{1}{h^{-3}} \frac{1}{j^{-4}} \frac{1}{k^{-2}}$$

$$= \frac{1}{2} \frac{h^3}{1} \frac{j^4}{1} \frac{k^2}{1}$$

$$= \boxed{\frac{h^3 j^4 k^2}{2}}$$